LECTURE NOTES ON

CIRCUIT THEORY



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In general, network is a combination of element. Electronic network is a combination of element.

1) Active elements.

2) Passive elements.

1) Active elements: -

Euments which can generate energy or has ability to Supply energy are known as active elements.

En: Battery & generatores (voltage Sources). current Sources. BITS, FETS, OPAMPS etc.

The behaviour of active elements cannot be described by ohm's low.

a) Passive elements:

Elements which cannot generate energy but can absorb consume, store or dissipate et are known as passive elements.

Er: Resistors, inductor, capacitores, diodes, theremistores

3) Linear elements:

Linear elements elways abey a straight lêne low i.e. linear elements shows a linear relationship between - Voltage and current.

A circuit element is linear if the prenciple of Superposition holds and relation between current and
voltage involves a constant coefficient e.g. Incase of
resistance, inductance of capacitance the relation between voltage and current are given by

V = IR $V = L \frac{d^2}{dt}$ $V = \frac{1}{c} \int i dt$

4) Montinear : exements:-

A nonlinear cercuit element is one in which the current does not change linearly with the change in applied voltags.

In nonlineare elements the preinciple 04 superposition. facts.

Ex: diodes, transitores, temperature dependent resstors (theremeston), voltage depende dependent capacitore cvaractor),

5) Unitateral & elements: -

when the property or characteristic of elements change with respect to direction of woment flow i.e when the polarity of the applied voltage is changed then the element are known as unitational elements.

Enc: - P-N junctione déodes, SCR etc.

6) Bilatural elements:-

when the property or characteristics of elements remains constant with respect to direction of current 410W i.e innespective of polarity of the applied voltage then the elements are known as belaterral elements.

Ex: - Resistors, transmission lines etc

A circuit is a closed conducting path through which circuit: an electrice comment either flows on is intended to circuit consists of active and passive elements in it. Flow.

Panameters: -

The voirieurs elements of an electric circuit are called parcameters like resistance, inductance and capacitance.

The parameters may be lumped on distributed.

L'incare circuit:-

A linear circuit is one whoes parameters are constant with time also they do not change with voltage on whent and the incent obeys ohm's law.

Non-linear circuet: It is that cercuit whole parameters change with voltage on winnert.

Bilateral cruet:

4 bilateral circuit is one whoes properties or characteristice une the same in either direction. The usual transmission line is bilaterral, because It can be made to parcform Its function equally well in either dérection.

Unilateral circuit:

It is that circueit whoes properties on characteristics change with the direction of its operation.

A déode rectifier is a unélateral cércuit : because it cannot percform rectification in both directions.

Electrice Network: -

A combination of various electrice elements, connected in any manner whatsover, is called an electric Network.

Passive Network: -

It is the one which contains no source of EM.Finit Active Metworck:

It is the one which contains no source one or more than one source of e.m.f along with passive elements.

It is a point in a the circuit where two or more circuit elements are connected together.

Branch:

It is that part of a Network which lies between two nodes.

Loop :-

It is a closed path in a circueit in which no element or node is encountered more than Once.

Mesh:-

It is a loop that contains no other loop within it.

Kerchhoff's point law on current law (Met)

Kirchhoffs Laws:-

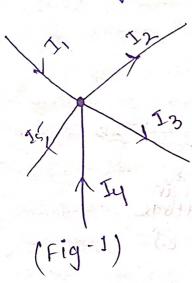
It is used

- 1) En determening the equivalent rasisfance of a complicated network of conductors.
- a) for calculating the current flowing in the various conductores

1) Kirchhoff's point law on eurrent law (kel):
In any electrical network, the algebraic sum of the currents meeting at a point (or junction) is zero.

Jotal current reaving a junction is equal to the total current entering that junction.

It is obviously true because there is no accumulation of charge at the junction of the network.



$$\frac{1}{1}$$

$$\frac{1}{R_1}$$

$$\frac{1}{R_2}$$

$$\frac{1}{R_3}$$

$$\frac{1}{R_2}$$

$$\frac{1}{R_3}$$

$$\frac{1}{R_2}$$

$$\frac{1}{R_3}$$

$$\frac{1}{R_3}$$

$$\frac{1}{R_3}$$

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$$\frac{1}{R_3}$$

$$\frac{1}{R_3}$$

$$\frac{1}{R_3}$$

From Jig-1

$$I_1 + (-I_2) + (-I_3) + (I_4) + (-I_5) = 0$$

$$\Rightarrow$$
 I, $+$ Iy = I₂ + I₃ + I₅
In coming wherealts = outgoing wherealts

from Yog - 2

FOR mode-A $I + (-I_1) + (-I_2) + (-I_3) + (-I_4) = 0$ $\Rightarrow I = I_1 + I_2 + I_3 + I_4$

2) Kinchhoff's Mest Law on voltage law: The algebraic Sum of the products of currents and resistances in each of the conductors in any closed poeth (or mesh) En a network plus the algebraic Sum of emits in that part path is zero ZIR + 2 e.m.4 = 0 Determination of voltage Sign:

(a) vign of Battery E.M.7:

A mêse in voltage should be given a tre sign and a fall in voltage a -ve sign.

* It is clear that as we go From the -ve terminal of a butterry to its +ve terminal these is a reese in potential, hence this voltage should be given

a tre sign.

* On the other hand, we go to trom the terminal to -ve terminal. then there is a fall in potential, hence, this voltage shall be proceded by a - ve sugh sign.

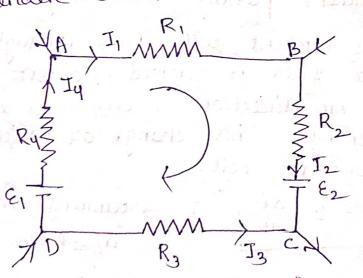
(b) Sign 04 TR Drop: current A tymm - B (Fall in voltage) (-V = - IR)

(Rise in . voltage) (tv=tIR) * If we go through a resistor in the same direction as the werent, then there is a fall in potential because current flows from higher to a lower potential. Hence, this voltage fall should be taken negative to a (-ve).

* However if we go in la dérection opposite to that of the current then there is a ruse in voltage.

Hence this voltage ruse should be given a positive sign

It is clear that the sign of voltage drop act to across a resistor depends on the direction of current through that resistore but is independent of the polarity of any other source of e.m.f in the circuit under consideration.



 I_1R_1 . is -ve (fall in potential) I_2R_2 is -ve (fall in potential) I_3R_3 is +ve (ruse in potential) I_4R_4 is -ve (fall in potential) E_2 is -ve (fall in potential) E_1 is +ve (fall in potential)

using kts Wirchhoff's voltage law I_1R_1 - I_2R_2 - I_3R_3 - I_4R_4 - E_2 + E_1 = 0

=> IIR, + IaR2 - I3R3 + I4R4 = E1 - E2

The state of the second second some some Lanz's law!

THE THE THE VENT OF THE STATE OF THE THE This law states that
Electromagnetically induced current always flow in suy dérection that the action of the magnetic field sot up by direction it tends to oppose the very couse which P. M. & HAMILTON 1917 produces it.

unis politice the Energy storred in Inductor & Capacitor:

Inductance :-

- The Asian depote the state of Inductance is the property of a material by vertee of which it opposes any change of magnétule on direction 04 electrice control passing the through the conductor.

As soon as current will flow through the will, on electromagnetic field is formed. However, with any change of year on direction of current, the electromay netél iffeld changes. This change of field induces a voltage (v) across the coil.

V= L di ? > current through inducto.

The voltage across the inductor would be zero it the current through it remains costant. This means that an inductor behaves as a short circuited- coil En steady state, when dercet steady current flows through it.

fore a menute change en current withen zero tême (dt =0) gives an infinite voltage across the Inductor which is impossible

power absorbed by Enductor $p = V \times c = L' \frac{dc}{dt}$ watts Energy absorbed by the inductor

$$W = \int_{0}^{t} P dt = \int_{0}^{t} L^{2} \frac{d^{2}}{dt} = \frac{1}{a} L^{2}$$

The inductor can store finite amount of energy, even the voltage across it may be nic

A pure inductore does not dissipate energy, but -Only storces it.

Capa citance: -

It is the capability of an element to storce electric change wethin it.

A capaciton stones electric energy in the form of electrice field being established by the two pala polarities 04 charges on the two electrodes of a capacitor.

capacitance is a measure of charge per unit voltage that can be storted in an element.

$$\begin{array}{c}
C = \frac{9}{2} \\
C = \frac{9}{2}
\end{array}$$

$$\begin{array}{c}
c \rightarrow \text{capacitance} \\
c \rightarrow \text{potential difference}.$$

$$\begin{array}{c}
i = c \frac{dv}{dt} \\
\end{array}$$

$$\begin{array}{c}
i = \frac{dq}{dt}
\end{array}$$

$$\frac{dv}{dv} = \frac{1}{c} \text{ idt}$$

$$\Rightarrow vt \int dv = \frac{1}{c} \int \text{idt}$$

$$\Rightarrow v_t - v_0 = \frac{1}{c} \int \text{idt}$$

> Vt = 1 colt + vo

vo > initial voltage of capaciton vt > final voltage of capaciton

The power absorbed by the capacitor is given by $p = vi = v \in \frac{dv}{dt}$

Energy storred by the capacitors is

$$\omega = \int_{0}^{t} P dt = \int_{0}^{t} v \frac{dv}{dt} dt = \frac{1}{2} cv^{2}$$

$$\left[\omega_{c} = \frac{1}{2} cv^{2}\right]$$

The voltage across the capacitor being constant.

This means that the capacitor on application of de voltage and with no initial charge first act as short circuit but as soon as the full charge it retains, the capacitor behaves an open circuit.

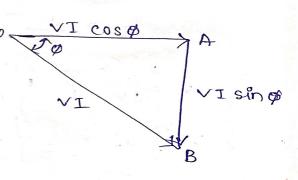
- => Also a capacitore nevere déssipates energy ét only etores it.
- => It can storce finite amount of energy; even it the current through it is zero.

Types of Electric power:-

- y Active power (watts on Kw)

 p = VI cos \$\phi\$
- a) Reactive powers (VAR. OTC KVAR)

 P = VI Sing
- 3) Apparent power (VA OR KVA)
 P = VI

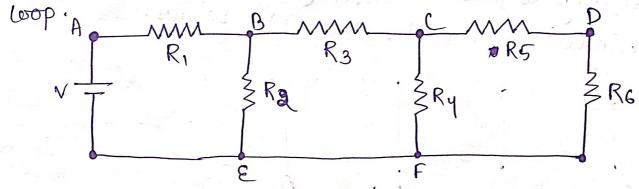


Power Factor (P4) = cos \$ = active power apparent power

A wop is a closed path in which no elements y podes nodes are repeated.

There must not be any sub loop.

Mesh: Mesh is a wop which consists of more than one



1) Nodes + A, B, C, D, E, F

a) Breanch - AB, BC, CD, DF; BE; CF, AE

3) Loop > ABEA, BCFEB, CDFC . (3 No. 04 Loops)

4) Mesh > ACFEA, BDFEB, ADFEA (3NO. 07 Mesh)

pources:

Depending on the type of sources we can classify both voltage y virtuent sources furether i.e.

1) Dependent Source 2) Independent Source

1) Dependent Socerce:

The source that depends on some other curwitelements & {R,L,c} in a given circult.

2) Independent Source: -

The independent source doesn't depend on any other circuit elements.

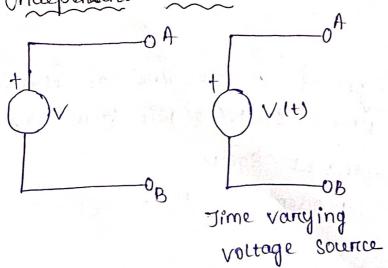
Dependent source is furthere divided into voltage source.

1) voltage dependent 2) current dependent voltage Source

wirrent source 3) Voltage dependent

4) current dependent current source.

Independent Source: -



1) Et j OB

Time verying Current Socerce

Independent sources actually exist as physical entities such as a battery and a d.c. generator and an outernator etc.

But dependent sources are parts of moders that are used to represent electrical properties of electronic devices such as operational amplifier y transistores etc.

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J. J. L.

Cercuit Clements:

1) Resistance: -

Electrical resistance is the property of a material by vertue of which it opposes the flow of electrons through the materical.

Thus resistance restricts the Flow of electrons through the materical.

S.9 unit a = 0 hm (1)

$$R = \frac{V}{I}$$

R=V

The material.

T > current in ampere

when an electrice current flows through any conductore, heat is generated due to collision of face electrons with atoms.

94 I = strength of current in Amp. V = Potential difference in volts across the conductor.

The power absorbed by the resistor.

The energy lost in the resistance in Form of heat is then enpressed as b.

$$W = \int_{0}^{t} P_{t} dt = Pt = \int_{0}^{a} Rt = \frac{V^{2}}{Rt}$$

2) Inductance:

Indutance is the property of a material by virtue of which it opposes any changes of magnitude or direction of electric everrent passing through the conductor.

8.7 unit of inductance = Henry.

It is given by faraday's laws of Electromagnetic — Induction. Inductance is said to be one henry when current through a coil of conductors changes at the rate of one emperce per second inducing one volt across the coil.

A wêre of finite length, when twisted into a coil, it becomes a simplest inductor.

As soon as current will flow through the coil, an electromagnetic field is formed. However, with any change of flow or direction of current the electromagnetic field changes. This change of field enduces a voltagery across the coil given by

V = L di _ 0

where i i is the current through the inductor in compare.

It may be noted from abow equation that voltage across the inductor would be zerro if the current through it remains constant. This means that an inductor behaves as a short circuited coil in steady state, when direct steady current flows through it However for any small change in current strength or change in direction, inductance will appear.

16

Thus an inductor behaves as oper cercuit just after so swithing across de voltage, as short circuit at steady state.

The power absorbed by the inductor will thus
is given by

$$P = V \times i = Li _{at}$$
 watter a

Energy absorbed by the Inductor will thus be

Thus From egn - 2 & 3 it is evident that the inductor can store finite amount of energy, even the voltage across it may be nil.

A purce Enductore does not dissipate energy but only

3) Capacitance !-

It is the capability of an element to stone electrical charge within it.

A capacitor stores electric energy in the Form of electricis field being established by the two - polarities of charges on the two electrodes of a capacitor.

manne i mande on

Tetroine

Quantitatively capacitance it is a measure of charge per unit voltage that can be storted in an element.

unot of capacitance = Farad (F)

C= 2 capacitance of the capacitor

C= 2 capacitance of charge that can be

Stored.

V > Potential clifference

i.e $i = c \frac{dv}{dt}$ [:: $i = \frac{dq}{dt}$] $dv = \frac{1}{c} i dt$

 $\frac{dv}{dv} = \frac{1}{C} \int_{0}^{\infty} dt$

 $\Rightarrow v_t - v_0 = \frac{1}{C} \int_0^t i dt$

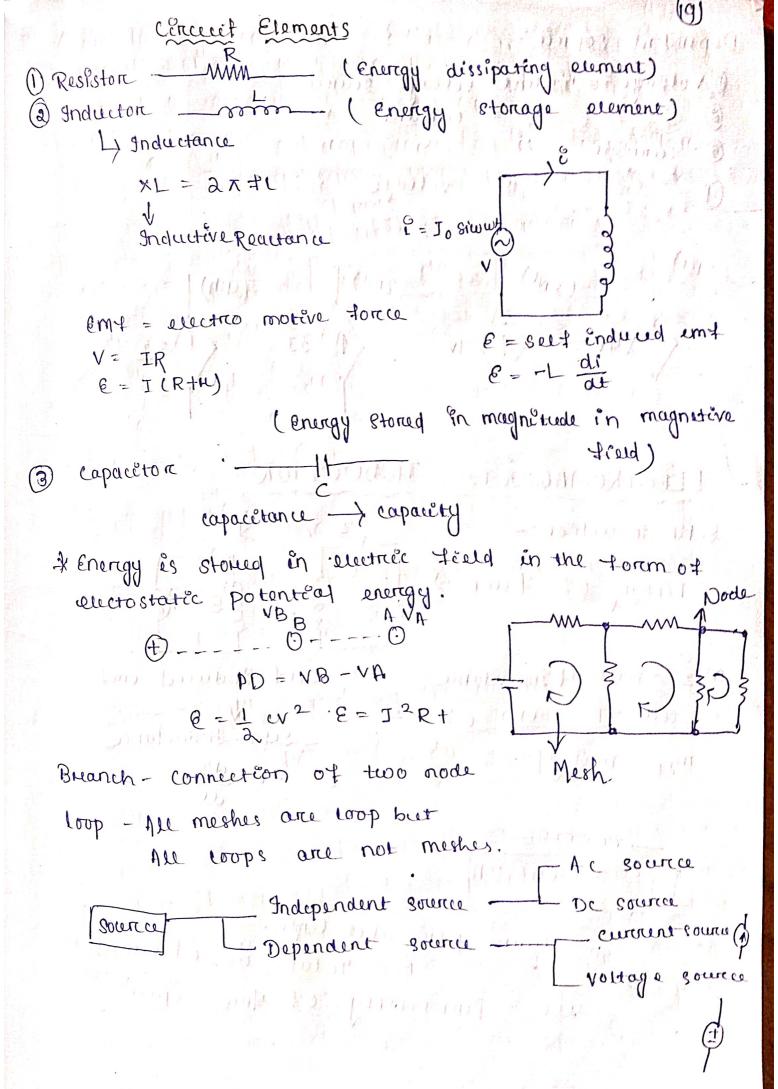
 $\Rightarrow V_t = \frac{1}{c} \int_{c}^{c} dt + V_0$

The power absorbed by the capaciton is $p = vi = v \cdot \frac{dv}{dt}$

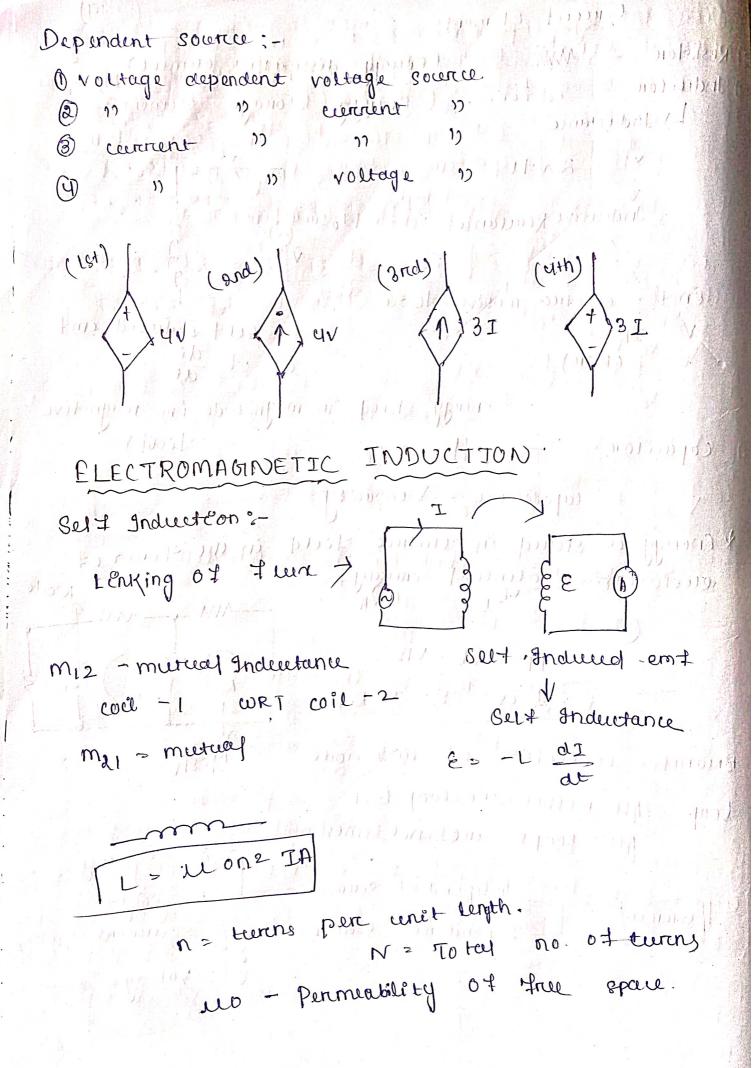
The energy storced by the capacitor $w = \int_{0}^{t} P dt = \int_{0}^{t} v c \frac{dv}{dt} dt = \int_{0}^{t} cv^{2}$

Thus we observe that the voltage across the - capacitore being constant, current through it is zero capacitore, on application of de This means that the capacitore, on application of de voltage and with no initial charge first acts as voltage and with no initial charge first acts as short circuit but as soon as the Full charge it retains, the capacitore behaves can open circuit.

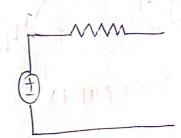
glores it. It can store finite amount of energy over even it the current through it is zero. E - Halle years of the koll, worth, by the

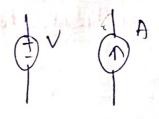


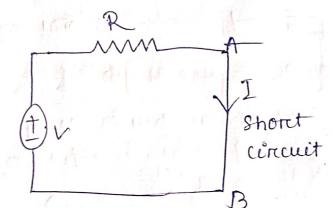
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Source conversion:-



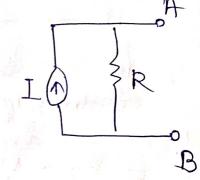




$$V = IR$$

$$I = V$$

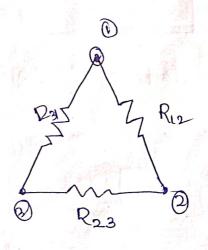
$$R$$



Stare Deta Transformation:-

$$R_{23} = R_2 + R_3 + \frac{R_3}{R_1}$$

$$R_{31} = R_{3} + R_{1} + R_{3}R_{1}$$



△ > Y (Dalta to 8 tare)

$$R_{1} = \frac{R_{1} R_{2} \times R_{3} R_{1}}{R_{1} R_{2} + R_{2} R_{3} + R_{3} R_{1}} = \frac{R_{12} \times R_{31}}{R_{12} + R_{23} + R_{31}}$$

$$R_{2} = \frac{R_{2}R_{3}XR_{1}R_{2}}{R_{1}R_{2} + R_{2}R_{3} + R_{3}R_{1}} = \frac{R_{23}XR_{12}}{R_{12} + R_{23} + R_{31}}$$

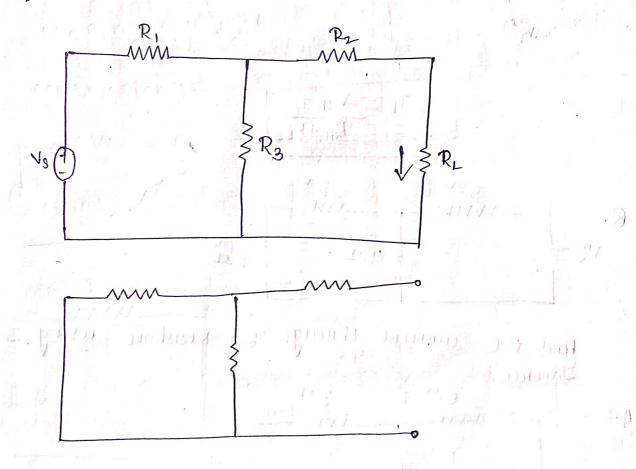
$$\frac{R_{3} = R_{2}R_{3} \times R_{3}R_{1}}{R_{1}R_{2} + R_{2}R_{3} + R_{3}R_{1}} = \frac{R_{23} \times R_{31}}{R_{12} + R_{23} + R_{31}}$$

ER,

Therenen's Theoreem:-

Statement :-

Any two terminal bilatral sineare DC cercuet can be respected by an equivalent circuit consisting of a voltage Source and a servier resistor.

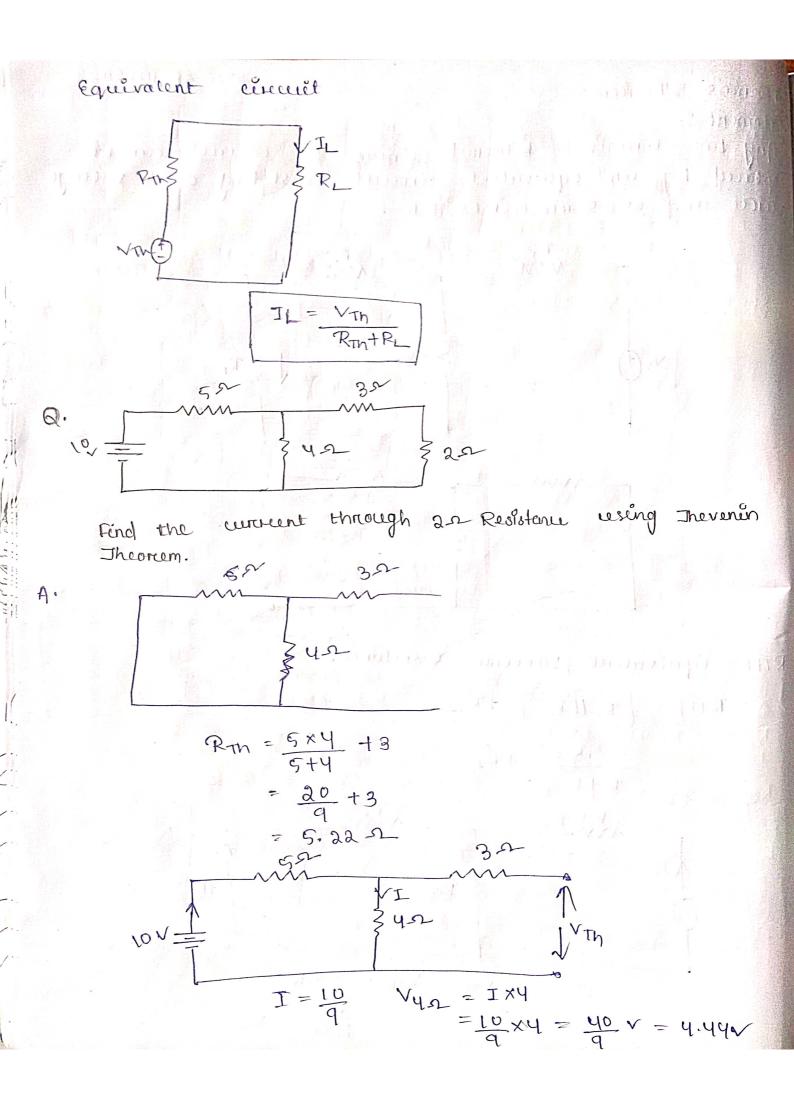


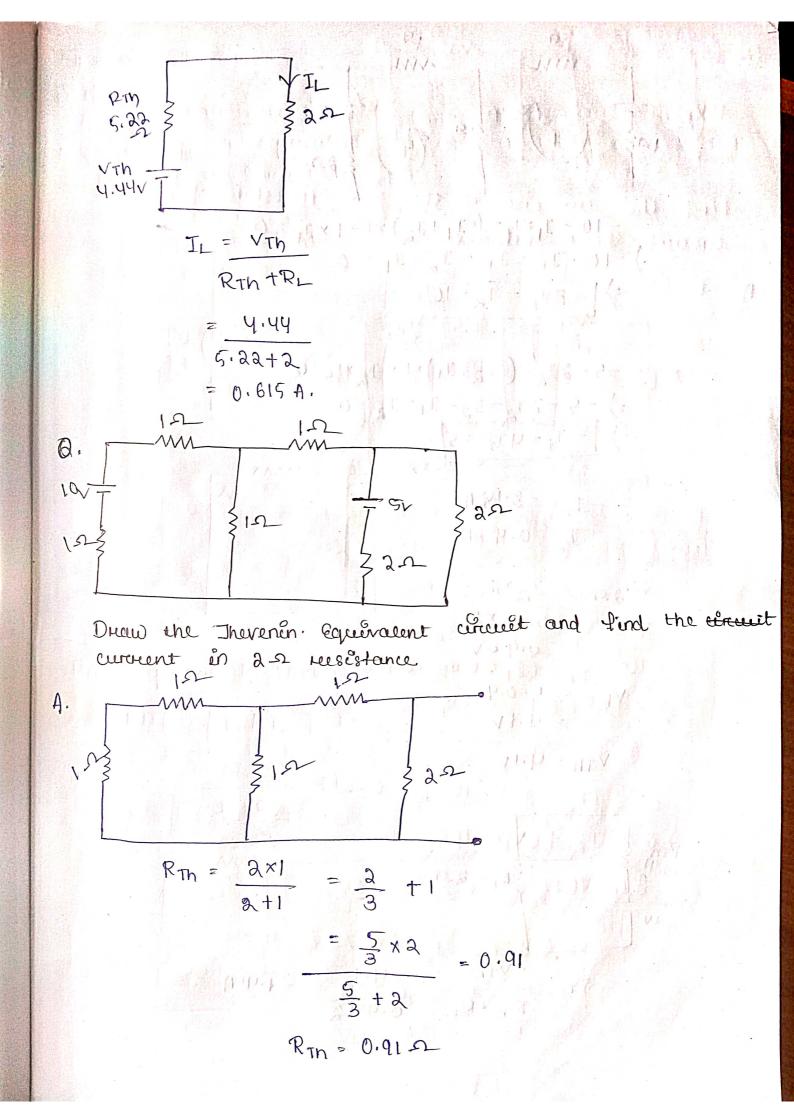
RTH = Equévalent Therenins Resistante.

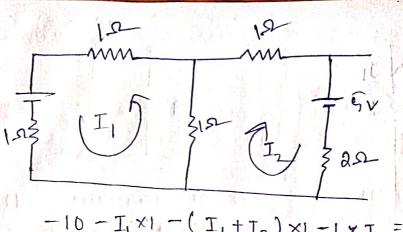
$$RTH = \begin{bmatrix} R_1 & L & R_2 \\ \hline R_1 & L & R_2 \\ \hline R_1 & + R_3 \\ \hline R_1 & + R_3 \\ \hline \\ XI & XI \\ \hline \\ XR_3 & VIH \\ \hline \\ XR_4 & VIH \\ \hline \\ XR_5 & VIH \\ \hline$$

$$V_{0C} = V_{Th} = I \times R_3$$

$$= \frac{V_3}{R_1 + R_3} \times R_3$$







$$\begin{array}{l} -10 - I_{1} \times 1 - (I_{1} + I_{2}) \times 1 - 1 \times I_{1} = 0 \\ -10 - I_{1} - I_{1} - I_{2} - I_{1} = 0 \\ \hline \\ -3I_{1} - I_{2} = 10 \end{array}$$

$$-5 - 2I_{2} - (I_{2} + I_{1}) \times I - I_{2} \times I = 0$$

$$= -5 - 2I_{2} - I_{2} - I_{1} - I_{2} = 0$$

$$= -5 - 2I_{2} - I_{2} - I_{1} - I_{2} = 0$$

$$I_1 = -3.18A$$
 $I_2 = -0.45A$

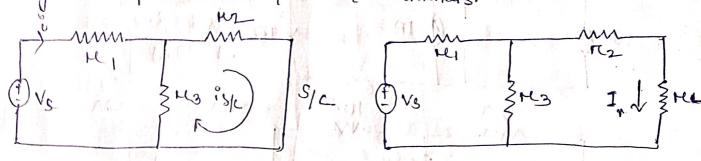
$$\begin{array}{c|c}
R_{TN} \\
= 0.91 \\
> V_{Th}
\end{array}$$

$$\begin{array}{c|c}
V_{Th} \\
\downarrow \\
V_{Th}
\end{array}$$

$$IL = \frac{VTh}{R_{Th} + R_L} = \frac{4.1}{0.91+2} = 1.41A$$

Nouton's Theoreem:Statement: A Linear cutive dependant voltage network stamonts

A linear active network consisting of independent & ondependant voltage and current sources and linear bilateral
network elements can be repeated by an equivalent circuit
consisting of a current source in parallel with a tessistance, the current source being the shoret circuited
current across the road terminal and the mesistance
being the internal mesistance of the source network working
through the open circuited road terminals.



In original to find the everteent through his the load resistance by Nore ton's theorem, let us replace the by Short circuit-

$$\frac{2}{12} = \frac{V_9}{12}$$

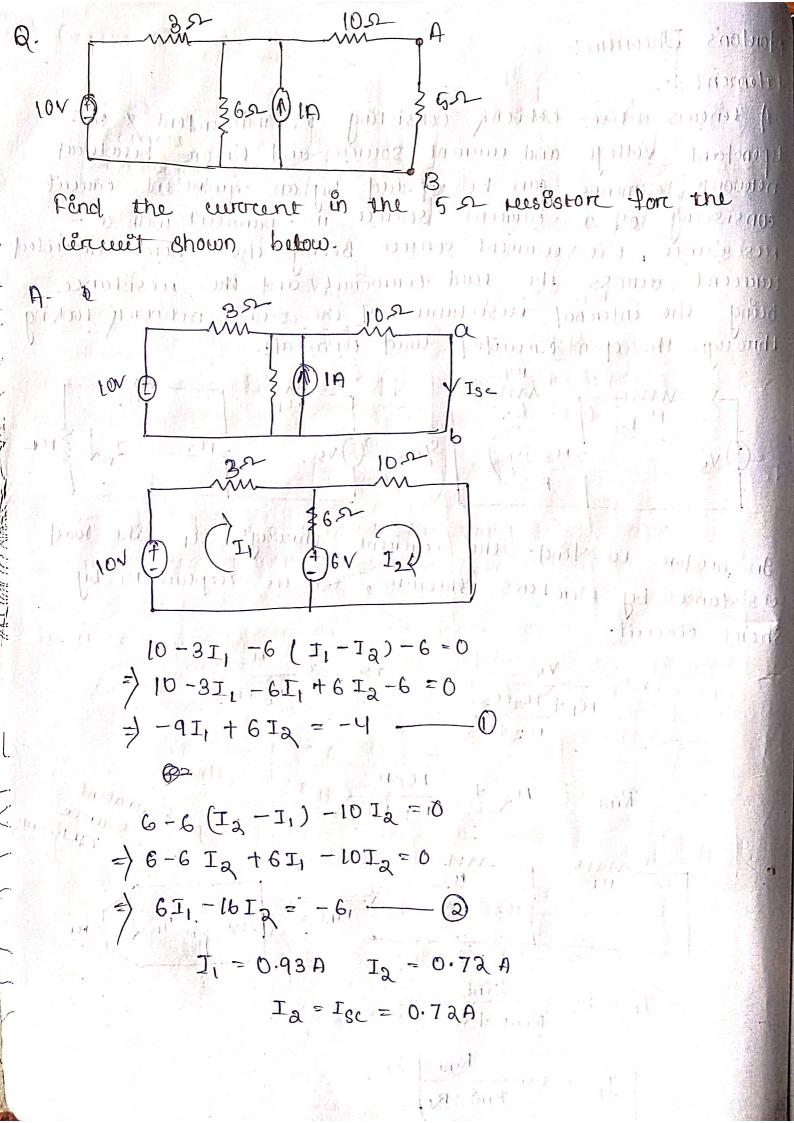
$$\frac{2}{12} = \frac{V_9}{12}$$

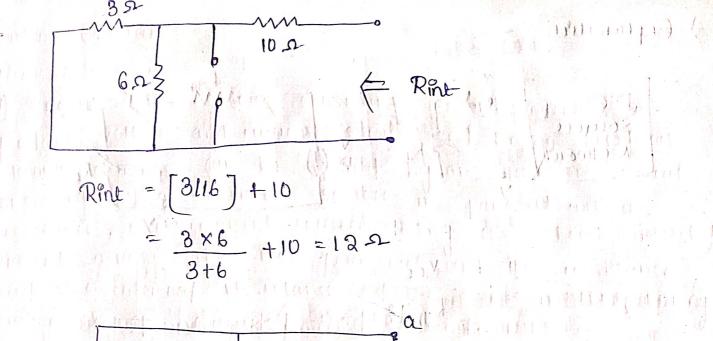
$$\frac{2}{12} = \frac{V_9}{12}$$

$$\frac{2}{12} = \frac{2}{12}$$

$$\frac{2}{12} = \frac{2}{12}$$

$$\frac{2}{12} = \frac{2}{12}$$





$$0.12A(n) \text{ In}$$

$$\begin{cases}
Rint = 12.9 \\
8.9
\end{cases}$$

$$\begin{cases}
Rint + 5
\end{cases}$$

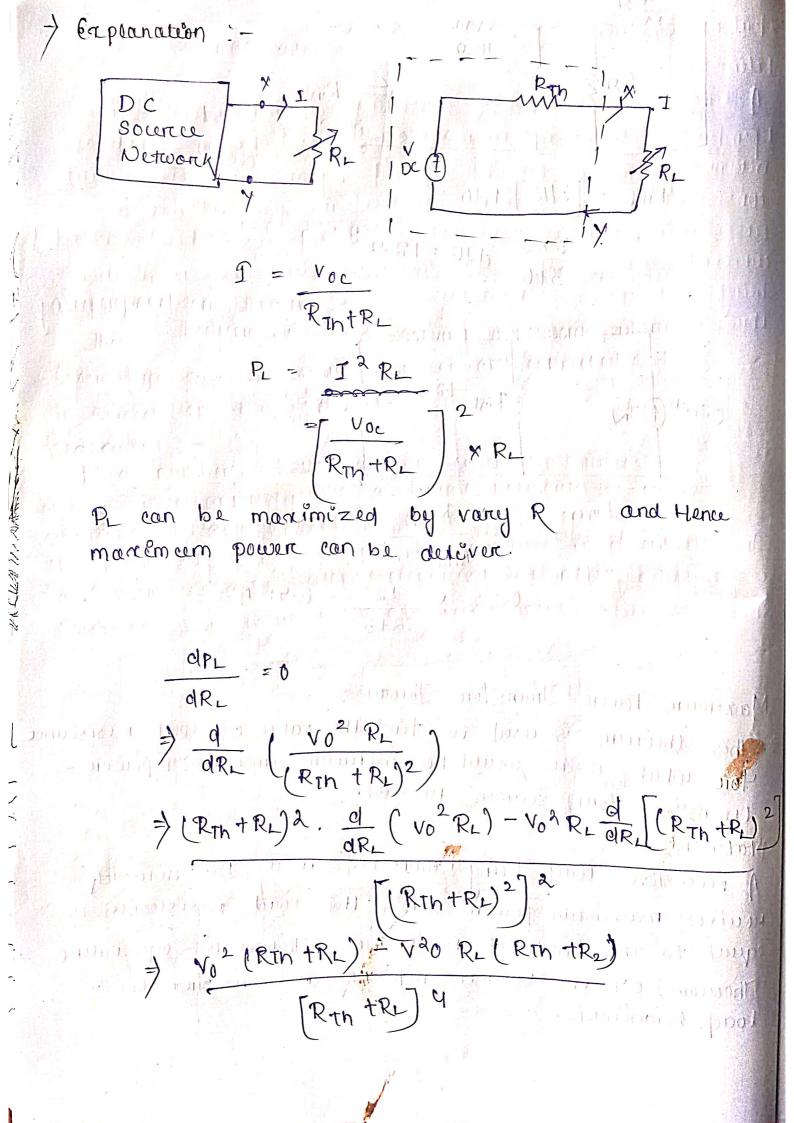
$$= 0.72 \times \frac{12}{12+5} = 0.51 \text{ A}$$

Menumum Power Transfer Theorem:-

-X This theorem is used to find the value of load resistance for which their would be marinum amount of power - treansfer form source to load.

Statement 3-10

A resistère load bring connected to a Dc network receives marcinem powere when the Load resistance is equal to the internal resistance (Therenon's equeralent Theorem) of the source network as soon from the Load terminals.



$$V_0^{2} \left(R_{Th} + R_{L} \right) \left(R_{Th} + R_{L} \right) - 2R_{L} \right)$$

$$\left(R_{Th} + R_{L} \right)^{3}$$

$$V_0^{2} \left(R_{Th} - R_{L} \right) = 0$$

$$\left(R_{Th} + R_{L} \right)^{3}$$

$$V_0^{2} \left(R_{Th} - R_{L} \right) = 0$$

$$\left(R_{Th} + R_{L} \right)^{3}$$

$$\left(R_{Th} + R_{L} \right)^{2}$$

$$\left(R_{Th} + R_{Th} \right)^{2}$$

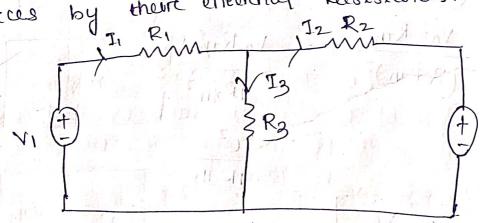
$$\left(R_{Th}$$

Superpositeon Theorem:-

Thes Theorem is used in solving a network where their are two or more sources and connected not In sercies ore o'in parallel.

Statement: -

94 a number of voltage on current sources are acting simultaniously in a linear network the resultant evererent in any branch is the algebraic sum of the currents that would be produce in it when each sources acts alone replacing are other independent Sources by their enternal resistences.



$$T_{1} = V_{1}$$

$$Req = [R_{2} | R_{3}] + R_{1}$$

$$= R_{2} R_{3} + R_{1}$$

$$R_{2} + R_{3}$$

$$T_{1} = V_{1}$$

$$R_{2} + R_{3}$$

$$T_{2} = T_{1} \times R_{3}$$

$$R_{3} = T_{1} \times R_{2}$$

$$R_{2} + R_{3}$$

$$R_{3} = T_{1} \times R_{2}$$

$$R_{4} = [R_{1} | R_{3}] + R_{2}$$

$$R_{1} = [R_{1} | R_{3}] + R_{2}$$

$$R_{2} + R_{3}$$

$$R_{1} = [R_{1} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{2} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

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$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{1} | R_{3}] + R_{2}$$

$$R_{1} = [R_{2} | R_{3}] + R_{2}$$

$$R_{2} = [R_{3} | R_{3}] + R_{3}$$

$$R_{1} = [R_{3} | R_{3}] + R_{3}$$

$$R_{2} = [R_{3} | R_{3}] + R_{3}$$

$$R_{3} = [R_{3} | R_{3}] + R_{3}$$

$$R_{1} = [R_{3} | R_{3}] + R_{3}$$

$$R_{2} = [R_{3} | R_{3}] + R_{3}$$

$$R_{3} = [R_{3} | R_{3}] + R_{3}$$

$$R_{4} = [R_{3} | R_{3}] + R_{4}$$

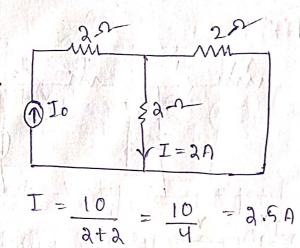
$$R_{3} = [R_{3} | R$$

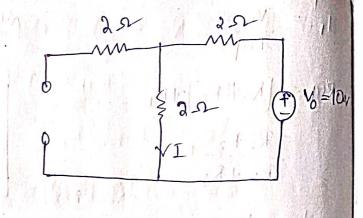
From the above circuit, $v_0 = I_0$, I = 2A

Lond I when vo =100 111111 min

30PM.

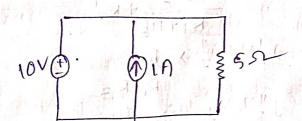
A. When $V_0 = 0$ T = 24



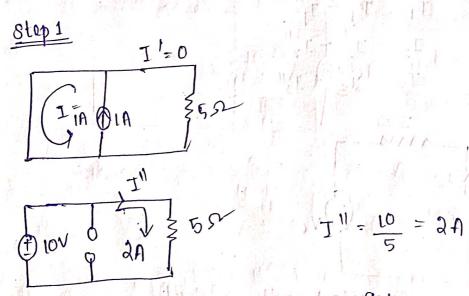


.. Net current through the required resistor. ?. $\Gamma = 2 + 2.5 = 4.5 A$

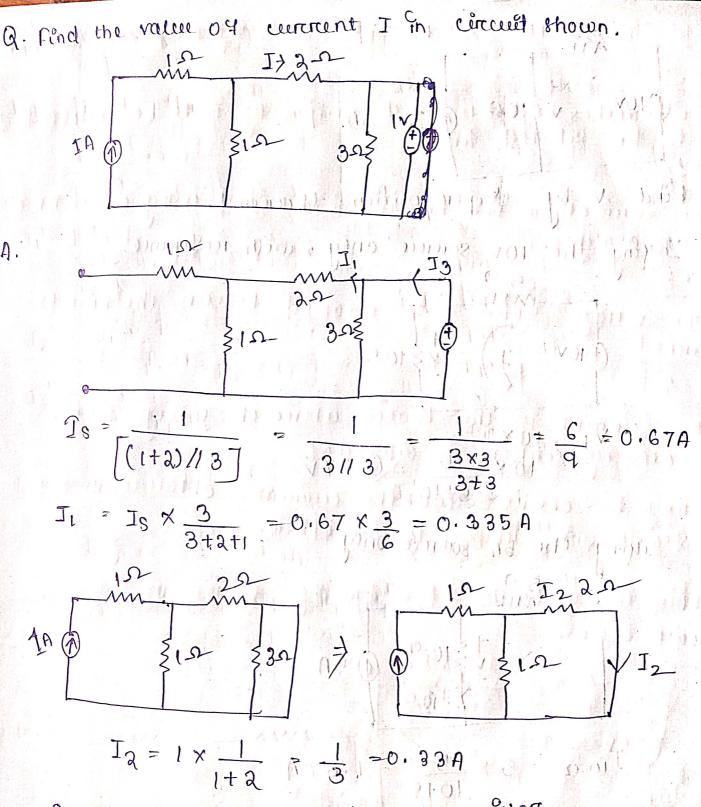
Q. In the circuit shown find the current through the 52 resistor using the prenciple of superposition.



A .

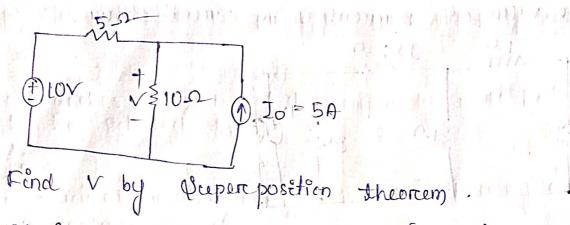


current through 5 of Resistor

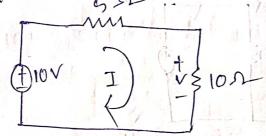


So the current through
$$22$$
 resistor
$$I = I_3 - I_2 = 0.335 - 0.33$$

10.005A



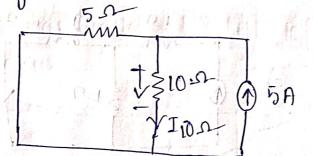
A Laying the LOV source only, with reference



$$V_1 = 10 \times I$$

= $10 \times \frac{10}{5+10} = 6.67 \times 10$

Jaying the 5A source only



$$I_{10-2} = 5 \times \frac{15}{10+5} = 1.67A$$

 $V_2 = 1.67 \times 10 = 16.70V$

By superposition theorem $v = V_1 + V_2 = 6.67 + 16.70 = 28.37 V$

Statement Of Reciprocity Theorem: -In any branch of a network, the current (II) due to a single Source of voltage (V) else cohere in the network is equal to the current through the branch in which the source was Drigonary peaced when the source is placed in the branch En which the current (I) was Originally obtained with Explanation: home of anichal brigation fait st ER3 Ammeter & Ro (F) Ammetery, por (JV) 100 (13)0100 3 In simple pense, the location of the voltage sounce and

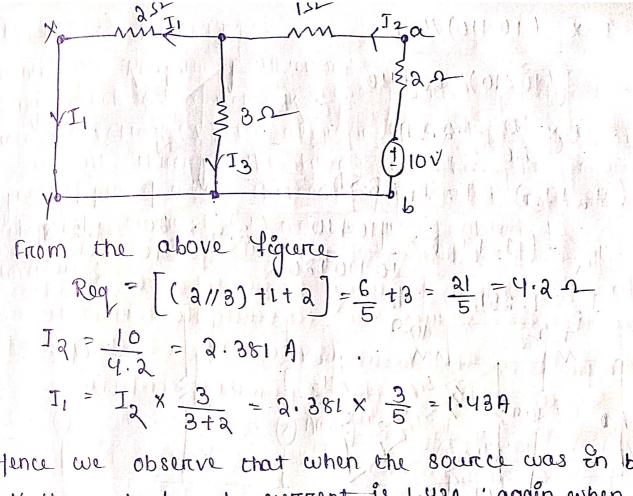
the through current may be interchanged without a change in 1cerrent.

However the polariety of the voltage source should have a the And Edenticality With the derection of branch current in

each position.

The limitation of this theorem is that it is oppleable only to single source networks and not in much source network! Moreover, the network where reciprocity theorem is applied should be a linear one and containing resistor, inductors, capacitons & coupled cércuits. The network should not have any time vil element.

Steps for Solving a Network willing Reciprosity Theorem A Manney Land Manney Manney Landers Otep-1 The branches between which receptocity is to be established are to be selected forest. Stop 2011 of the children of depend all appoints promises The current in the breanch is obtained using conventioned complete the form the property of the final former network analysis! Step-3 The voltage source is interchanged between the branches concerned. Ostop -4 The current in the branch where the voltage source was enisting earlier is calculated. It may be observed that the current obtained in step-2 and step-4 are identical to each other. Q. show the application of reciprocity theorem in the network shown betow all lymphillip of por this appoint $\frac{1}{2}$ $\frac{1}{m}$ $\frac{1}$ pino problem hard the villa by the control of the problem of the p Equivalent Resistance across XY Req = [(2+1) (1/3] + 2 = 3.5-210 $I_{1} = \frac{10}{3.5} = 2.86 \, \text{A}_{10} \, \text{Mod for the property }$ $J_2 = 2.86 = x \frac{3}{3+2+1} = 1.43A$

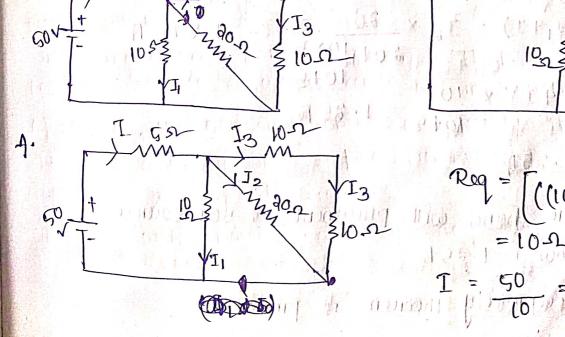


Hence we observe that when the source was in branch X-Y the a-b branch current is 1.434; again when the source is in branch at the X-Y branch current becomes 1.43A.

This proves the Reciprocity theorem

Q. shown the validity of reciprocity theorem in the Figure
given below.

1552 13,10,2



$$Req = [((10+10)/120)/110]+5$$
= 10-2

$$I_{L} = I \times \frac{(10+10)/(20)}{(10+10)/(20)}$$

$$= 5 \times \frac{10}{20} = 2.54$$

$$\therefore (J_{2} + J_{3}) = I - J_{1} + 2.54$$

while
$$I_{2} = (I_{2}+I_{3}) \times \frac{10+10}{10+10+20} = 2.5 \times \frac{20}{40} = 1.25 \text{ A}$$

Equivalent resistance across the 50 V source

$$Roq = \left[\frac{10 \times 5}{10 + 5}\right] / (10 + 10) + 20 = (3.33/120) + 20$$

$$= 2.855 + 20$$

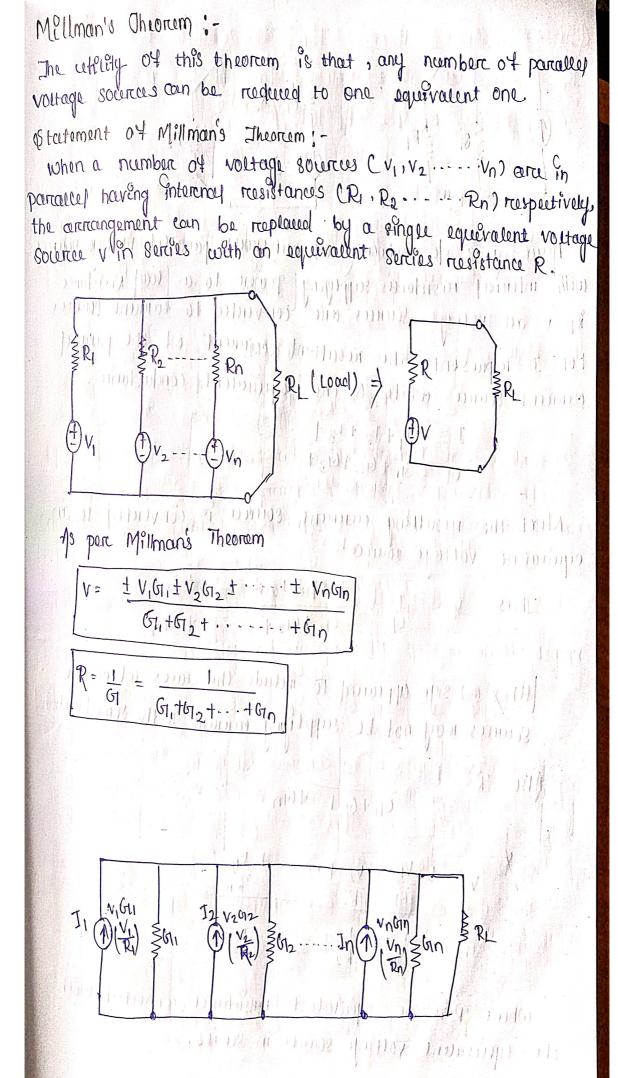
$$= 22.86 - 1$$

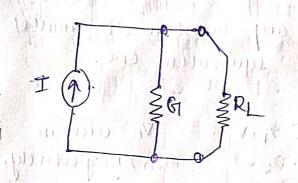
$$I_{a} = \frac{50}{24.8.6} = 2.187A$$

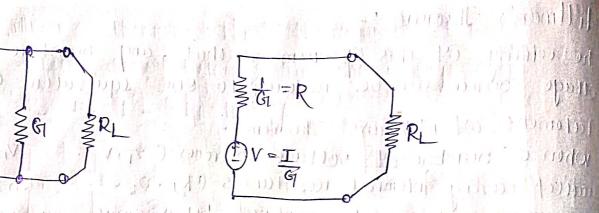
This gives (I₁+I) = $I_{a} \times \frac{20}{40 + \frac{10 \times 5}{10 + 5}} = 1.875A$
 $I = (I_{1}+I) \times \frac{10}{10 + 5} = 1.25A$

On the other hand with placement of 50 v source in Iz branch now I = 1.25 A

Thus the Reciprocity theorem is proved.







Assuming a de network of numerous parallel voltage source with interchal rusistanus supplying power to a load Rusistance Re 1 au voltage sources are converted to eurnant sources Let I représents the resultant current of the parallel current sources where of the jaquealent conductance.

Next the resulting current source is converted equévalent voltage source

Thus
$$V = \frac{I}{G} = \frac{\pm I_1 \pm I_2 \pm \cdots \pm I_n}{G_1 + G_2 + \cdots + G_n}$$

[41 & (-) sign appeared to include the cases where the sources may not be supplying current in the somedimentary

Also
$$R = \frac{1}{G} = \frac{1}{G_1 + G_1 + G_2 + \cdots + G_n}$$

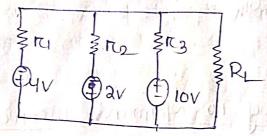
$$V = \frac{1}{R_1} + \frac{V_1}{R_2} + \cdots + \frac{V_n}{R_n}$$

$$\frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_n}$$

where Ris the equevalent resistance connected with the equivalent voltage source in services.

Thee finally V= t Vion + V2012+ 11 --- -- to Vacin No Maria Cont Grat to the contract Si Gik = Thy Oteps for solving problems Relating to Millman's Theorem: Following steps can be enewted to get a direct solution of the problems relationed Milmon's Theorem. Otepi :- Inquiring Obtain the conductance (C1, G12----) 04 each voltage source (V1, V2).) and Find G1, the equivalent conductance Apply Milman's theorem to sind v, the equivalent voltage Cource given by. V= V1611 + V2612 + + Vn61n Cont G2 to retan Otep-3 Determine (R), the equivalent sercies rusislance with the equivalent Voltage source (V) Step-4 (Val) light sil is held in a sil the sile of th The current through the load is then I given by IL = V ; R being the load resistance.

Q. Using Milman's theorem, Hind the current through Re in the circuit shown below & find the voltage drop



Here V = -V, G1 -V2 G2 + V3G3

$$R = \frac{1}{G_1} = \frac{1}{G_1 + G_2 + G_3} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$V = \frac{-4 \times \frac{1}{4} - 2 \times \frac{1}{4} + 10 \times \frac{1}{4}}{\frac{1}{4} + \frac{1}{4} + \frac{1}{4}} = \frac{-1 - \frac{1}{2} + \frac{5}{2}}{\frac{3}{4}} = \frac{4}{3} \times \frac{1}{3}$$

the equévalent cercueit déagram

$$\frac{9}{\frac{4}{3}+10} = \frac{4}{3} \times \frac{3}{34} = 0.124$$

The current through 10-2 resistor is thus 0-12A while the drop across to 2 resistor

Find the current through the In resistor using Millman's Theorem. THE POPULATION OF A PROPERTY OF THE PROPERTY O 1 2 I, t I2 = 5+3 = 8 A 1111 1 1110 1 1 1 10 3 11 1 いいり 「いけいとこれ」はないこれのかりといいいいいいいいいかりかりとう converting current source to an equivalent voltage source -1-121-01 mile profession mile in demonstr Current through 152 resistor Ira = V = 8 = 18 = 4A FO IN DE TRUITED AND E TRUIT Theologian to the

Average value of sinusoidal current (Targ)

The half -cycle average value of a.c. is that value of Steady current (d-c) which would send the same amount of change through a concert for half the 19me period of a.c as 98 send by the a.c through the some circuet in the some time.

RMS OR Effetive value:-

The effective on r.m.s value of a an altranating werrent is that steady current (dc) which when 410wing through a given resistance for a given time produces the some amount by heat as produced by the altreanating current when flowing through the some resistance for the same time.

Trems =
$$\sqrt{\frac{i^2 + i^2 + i^2 + \cdots + i^2}{2}}$$

Vrems = $\sqrt{\frac{V_1^2 + V_2^2 + V_3^2 + \cdots + v_n^2}{2}}$

Trems =
$$\frac{\text{Im}}{\sqrt{2}}$$
 on $\frac{1}{\text{rems}} = 0.707. \text{Jm}$

$$V_{rcms} = \frac{V_m}{\sqrt{2}}$$
 orc $V_{rcms} = 0.707 V_m$

Form factor. -The nation of nimes value to the average value of an alternating quantity is known as yourn factor.

The form factore gives a measure of the provinces of the wave form. The propiet the wave, the greater is its form factore x vice-versa.

Triangural wo her form factor 2 1:15

The ratio of maximum value to the rims value of an alternating quantity is known as peak factor.

Peak factor = Man. value

RMS Value

The value of peak factor also depends upon the wave form of the alternating quantity for an atternating voltage or current varying since sordally, worth its value is 1.414.

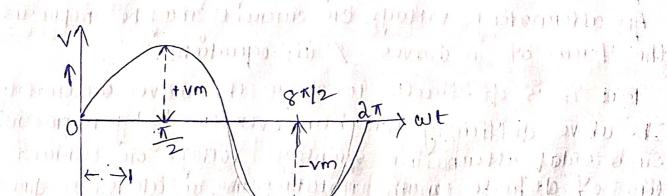
For a sinusordal voltage or current

Peak factor = Mar. value = 1.410

Thomas bis sparing potential Pro 18 of according

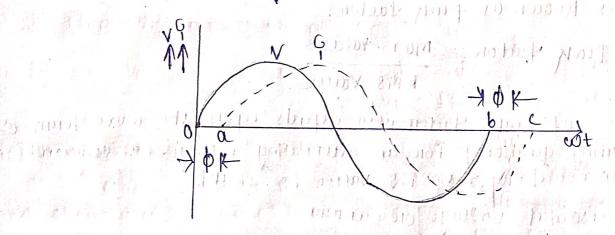
The peak factor is also called levest factor or amplitude factor.

Phase: -



Phase of a particular value of an alternating quantity is the fractional part of time partiod or cycle through which—the quantity has advanced from the soluted zero position of reference.

Phase défference: when two auternating quantity of the same frequency how défferent zero points, they are said to have a phase différent. The angle between zero points is the angle of phase défference of. It is generally measured in degrees on radians.
The quantity which passes through its zero point earlier. Is said to be leading while the other is said to be lagging



 $v = Vm \sin \omega t$ $C = Im \sin (\omega t - \phi)$

The above seens indicates that current is logging behind the voltage by phase angle ϕ .

Representation of Alternating voltages and currents:

An alternating voltage on current may be represented in the forces of in waves & iii, repeations.

But it is defficult to chaw the wave accurately. The above difficulty has been overcomed by representing sin usoidal alternating quantity voltage on current by a line of definite rength rotating in anticlockwise direction at a constant angular velocity (w). Such a rotating whe is called a phasonor.

The length of the phasor is taken equal to the maximum value of the atternating quantity and angular velocity equal to the angular velocity of the alternating quantity

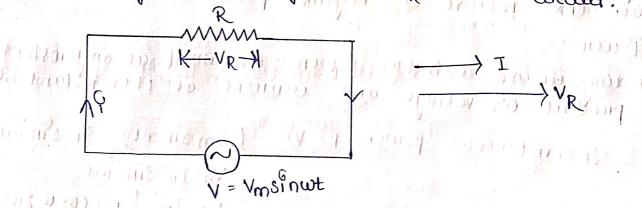
Instantoneous power supplied to a circuit is simply the The instantoneous power supplied to a circuit is simply the product of the instantoneous voltage and instantoneous current.
The instantoneous tottage power is always expressed in watts,
increspective of the type of circuit resed.

The instantoneous power may be positive or negative.

A positive value means the power flows from the source to the load, consequently, a negative value means that power flows from the load to the source

Ac circulit containing Resistance only:

when an alterenating voltage is applied across pure resistance, then free electrons flow (i.e.) consent in one
derection fore the ferst harf -cycle of the supply and then
flow in the opposite direction during the next harf eyele,
thus constituting afternating executed, in the arcuit.



conséder a cércuét containing a pure respotance of RA connected across an alternating voltage source.

As a result of this voltage of an afternating current? will flow in the circuit. The applied voltage has to overcome the drop in the resistance only i.e.

Dinurgor meril

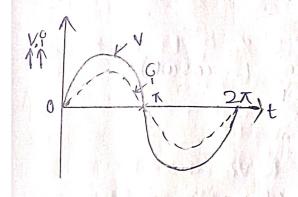
=> 8 = 1 V

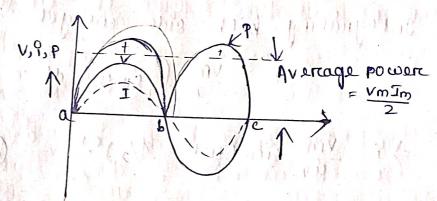
Substituting the value of V.

Y = Vm 8m wt _____ (u) The value of & will be maringum tottere (f. e Im) when oin wt =1 $Im = \frac{Vm}{R}$ Egn-D becomes 6= Im 8 in wt In terms of r.m.s values $\frac{Vm}{\sqrt{2}} = \frac{Tm}{\sqrt{2}} \times R$ => V=VR=IR (P) Phase angle: -9+ 98 com clear from eqn-0 & @ that the applied voltage and the conceent are in phase with each other G. C. they pass through their zero values at the same instant and attain their positive and negative peaks at the same instant. (11) Power :-In any circulat, electric power consumed at any instant is the product of voltage and wererent at that instant i.l. Instantaneous power p= Vi = (Vm sinwt) (Im sin wt) Vm Im Sin2 wt 2 Vm Im (1-0000 2wt) Vm Im - vm Im cos 2 cot Thus power consists of two parts, a constant part Vm In and a fluetuating part vm Im was a wt. since power is a scalar quantity overage power over a complete eyel 18 to be considered, 000. . Power consumed $P = \frac{1}{2\pi} \int_{0}^{\infty} \frac{v_{m} T_{m}}{\lambda} d(wt) + \frac{1}{2\pi} \int_{0}^{\infty} \frac{v_{m} T_{m}}{\lambda} d(wt)$

$$\Rightarrow p = \frac{Vm fm}{2} + 0 = \frac{Vm}{\sqrt{2}} \times \frac{Jm}{\sqrt{2}}$$

where V= VR = rems value of the applied voltage I = rms value of the circuit current





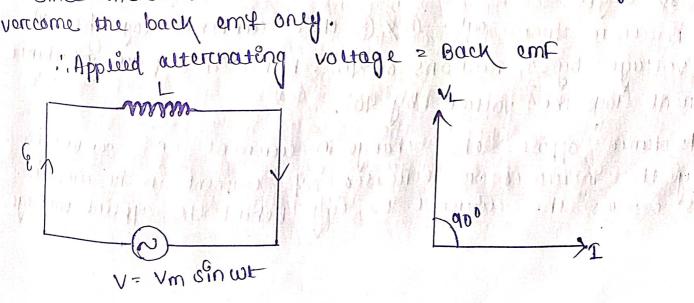
Average power $P = \frac{Vm \text{ Im}}{2} = \frac{Vm}{\sqrt{2}} \times$

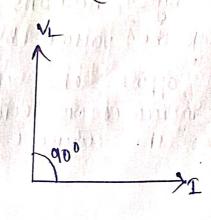
A.C elecuit containing pure Inductance Only

when an atternating current flows through a pure inductors inductive cost a back emy (= L di) is induced due to the inductance of the coil. This back emil at every instant opposes the change in writtent through the coil.

Since there is no ohmic drop, the applied voltage has to

overcome the back ent only.





consider an atternating voltage applied to a pierre indultant 04 L henory. Let the equation of the applied atternating voltage be.

clearly $V = Vm \sin \omega t = 0$ $d^2 = Vm \sin \omega t = 1$ $d^2 = Vm \sin \omega t = 0$

entegrating both sides we get

E = Vm coswt)

 \Rightarrow $\frac{G}{V} = \frac{Vm}{\omega_L} \sin(\omega t - \frac{\pi}{2}) - 2$

The value of & will be mariemen (i. e Im) when sin (wt-1).
Gs unity.

 $I_{m} = \frac{V_{m}}{\omega L}$

Substituting the value of $\frac{Vm}{\omega L} = Im \sin \omega q^n - \mathfrak{D}$ $\mathcal{E} = Im 8in (\omega t - \sqrt{2}) - \mathfrak{D}$

XL = WL

E) Phase angle:

He voltage by T readfons on 90°. Hence in a pure indulance current logs the voltage by 90°.

Inductance opposes the change in current and serves to delay the increases or decreases of current in the circuit. This causes the current to eag behind the applied voltage

(P) Inductive reactance:

Inductance not only causes the werent to log behind the grade but it also limets the magnitude of were in the writing but Im = $\frac{V_m}{\omega_L}$ $\frac{V_m}{I_m} = \omega_L$

The quantity whis called the inductive reactance XL of the coof.

$$Im = \frac{Vm}{\sqrt{NL}}$$

$$\Rightarrow \frac{Vm}{\sqrt{NL}} = \frac{VL}{\sqrt{NL}}$$

$$\Rightarrow I = \frac{VL}{\sqrt{NL}} \quad (V = NL)$$

$$\Rightarrow \times L = \frac{Vm}{\sqrt{NL}} \Rightarrow \Lambda + L$$

when an atterementing voltage is applied across the plates of a capacitor, the capacitor is changed in one -

The result is that electrons more to and tro arround the circulat, connected connecting, the plates, thus

constituting atternating current.

Or capacitance c farad.

Let the equation of the applied to a capacitor of tapa.

Voltage be

v = Vm sin wt _____

As a result of this afternating voltage, afternating -

Let at any Enstant & be the current & q be the charge on the plates.

charge on capacétore q = cv = cvm sinut

i. circueët current = d cq1 = d (cvm sinut)

= w c vm cos wt

 $\Rightarrow \& = \omega c \vee m \quad \text{sin} \quad (\omega t + \frac{T}{2}) \quad = \quad \textcircled{a}$

The value of & will be maramum (f. e.Im) when sin (at + 3)

Im = wcvm

Substituting the value we vm = Im in eq. - a

It is war from eq. - 1) & 3 that writer hads the voltage by it radian on 900.

by 90° capacitance opposes the change in voltage and serves to delay the increase or decrease of voltage across the capacitar. This causes the voltage to lay behind the variant.

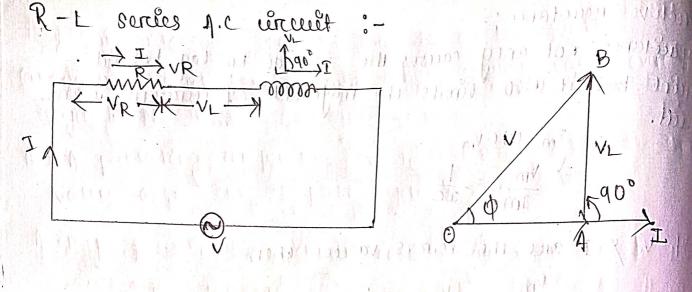
anning per Formis

Capacotore reactance: capacitance not only causes the voltage to lag behind current but it also limits the magnitude of current in the circuit. Im=WCVm $\Rightarrow \frac{V_m}{Im} = \frac{1}{\omega c}$ If Ve & I are the rim.s values then $\frac{V_{m}}{I_{m}}$ $\frac{V_{c,n}}{I_{m}}$ $\frac{V_{c,n}}{I_{m}}$ $\frac{V_{c,n}}{I_{m}}$ $\frac{1}{I_{m}}$ $\frac{V_{c,n}}{I_{m}}$ $\frac{V_{c,n}}{I_{m}}$ clearly the opposition offered by capacition current flow 9811-100 This quantity 1/we is called the Coepacetére reacteurce xe 04, the capacetor I = Venous id in initialis of the many ib THE PRIMARY FOR STATE OF STATE Drooms AH Than IN VATUE WATER WATER Power :-Instanton low power P = Ve = Vm showt x Im sho (wt + 1/2)

= Vm Im showt coswt => P = vm Im sin awt. Average power P = Average of Pover one yell = 0 Hence power obsorbed in a pierre capacitance is zero.

mile it both him of 193 and Marining

The Siland of the Mark Co



Let V = rams value of the applied voltage. T = rams value of the applied voltage. $V_R = IR$ where V_R is in phase with T. $V_L = TXL$ where V_L leads T by $q0^\circ$.

Jaking wortent as the reference phasor, the phasor - diagram of the circust can be drown.

The prostage alrep $V_R = TR$ is in phase with wherent and is represented in magnitude and direction by the phasor of.

The voltage drop $V_L = T_{XL}$ leads the current by qooland. The voltage drop $V_L = T_{XL}$ leads the current by qooland is represented in magnitude and direction by the phasor is represented in magnitude and direction by the phasor AB.

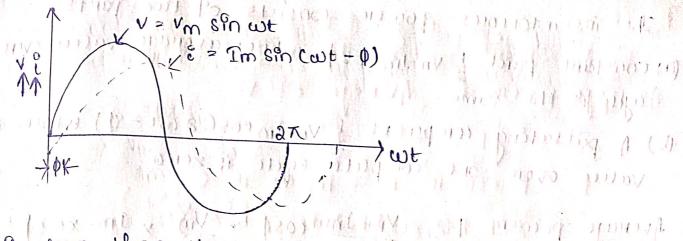
V2 $V_R^2 + V_L^2$ is $V_R^2 + V_L^2 +$

 $\Rightarrow \boxed{1} = \frac{V}{\sqrt{R^2 + \chi L^2}}$

The quarkity $\sqrt{R^2 + xL^2}$ offers opposition to current show and 98 called impedance of the circuit.

The quarkity $\sqrt{R^2 + xL^2}$ offers opposition to current show and 98 called impedance of the circuit.

The quarkity $\sqrt{R^2 + xL^2}$ offers opposition to current show and 98 called impedance of the current show and 98 called impedance of 18 measured in ohms (2) and 20 m



It is cleare from the phason diagram that circuit concrent I lags behind the applied voltage v by go.

$$\frac{1}{\sqrt{R}} = \frac{1}{\sqrt{R}} = \frac{1$$

V= Vm sin wt c° = Im sin (cut - a) where Im = Vm Z

The angle of log (i.ep) is greater than 0° but less than 90° 310

It is determined by the rate of inductance inductive reactance to responde.

The greater the value of this roots, the greater will be the phase congle \$ & vice-versa.

I'mpedance:-

The total opposition offered to the flow of alternating current by a cercult 9s called impedance Zot the cercult!

I then the light of the sent of the POWER :-Instantoneous power p=ve=vm sin wt x 2m sin (wt-4)

$$P = \frac{1}{2} \text{ Vm Im} \left[2 \sin \omega t + 8 \sin (\omega t - \phi) \right]$$

$$= \frac{1}{2} \text{ Vm Im} \left[\cos \phi - \cos (a\omega t - \phi) \right]$$

$$= \frac{1}{2} \text{ Vm Im} \cos \phi - \frac{1}{2} \text{ Vm Im} \cos(2\omega t - \phi)$$

The instantoneous power consists of two parts.

(a) constant paret 1 vm Im cost whoes average value over a cycle is the same

value over one complete eyele is zero.

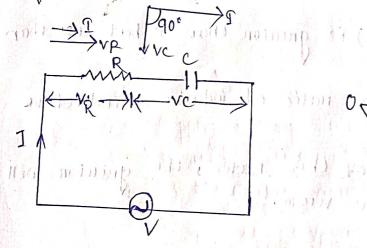
Average power
$$P = \frac{Vm \text{ Im}}{2} \cos \phi = \frac{Vm}{\sqrt{2}} \times \frac{Im}{\sqrt{2}} \times \cos \phi$$

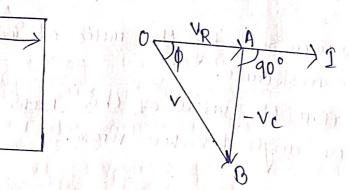
$$\Rightarrow P = VI \cos \phi$$

$$\cos \phi = \frac{IR}{IZ} = \frac{R}{Z}$$

$$P = VI \cos \phi = (IZ) \text{ It } R(Z) = I^2 R$$

R-c series Aic circuét 1-





In sercies with a capacitor of a forced of R ohms connected

Let $V \rightarrow \mathbb{R}$ roms value of applied voltage $T \rightarrow \text{roms}$ value of circuest current $V_R \rightarrow I_R \rightarrow \text{where} \ V_R$ is in phase with I $V_C \rightarrow T_R \rightarrow \text{where} \ V_C$ logs T by q_0 .

Jaking current as the reference phasons the phason diagram of the circuit can be drawn.

The voltage drop [VR = IR] is in phase with current and Ps respresented in magnitude and direction by the phason OA.

The voltage drop $v_c = I_{Xc}$ logs behind the current by gos and is represented in magnetude and direction by the phasoir on.

The voltage drop IV is approved in the specific of the second of the sec

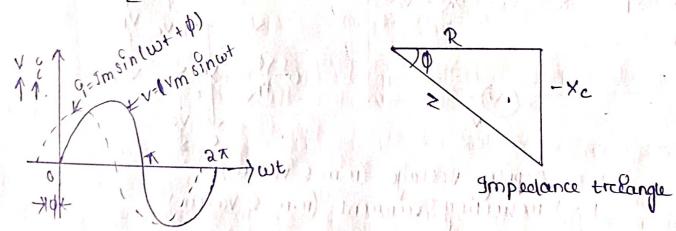
The applied voltage vis the phasor, seen 04, these two drops.

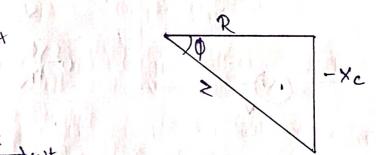
$$V = \sqrt{\frac{2}{R^2 + (-V_C)^2}} = \sqrt{(R^2) + (-I_X | C)^2} = I \sqrt{R^2 + X_C^2}$$

$$= \sqrt{\frac{1}{R^2 + X_C^2}}$$

The quantity \R^2+x_2 offers, opposition to current flow and is called impedance of the circuit.

$$I = \frac{V}{Z}$$
 where $Z = \sqrt{R^2 + x_c^2}$





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Phase angle:

It is clear Forom the phasor d'agram that circuit current I reads the applied vollage v by do.

$$tan \phi = \frac{-V_{C}}{V_{R}} = \frac{-Ix_{C}}{IR} + \frac{x_{C}}{R}$$

Since current is taken as the reference phasons negative phase angle implies that voltages egs behind the wirent.

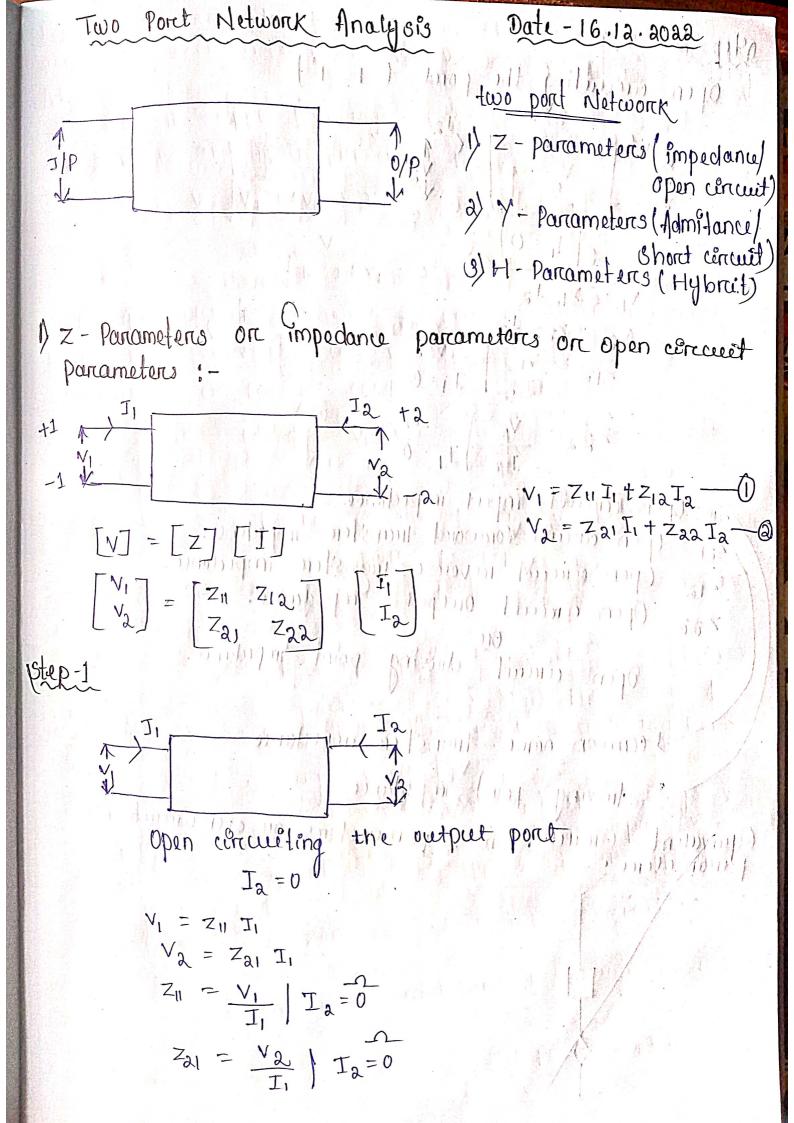
It the applied voltage is $V = V_m sin \omega t$ then wrowest current $E = I_m sin C \omega t + 0$

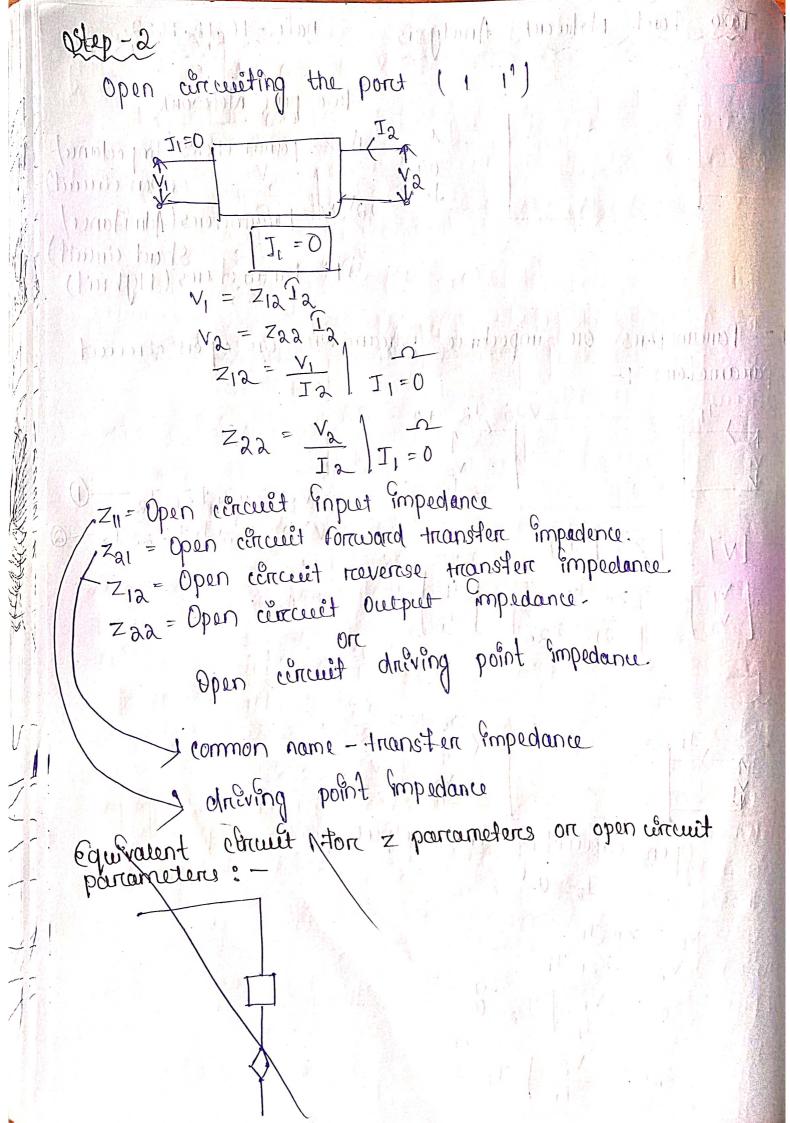
where Im = Vm

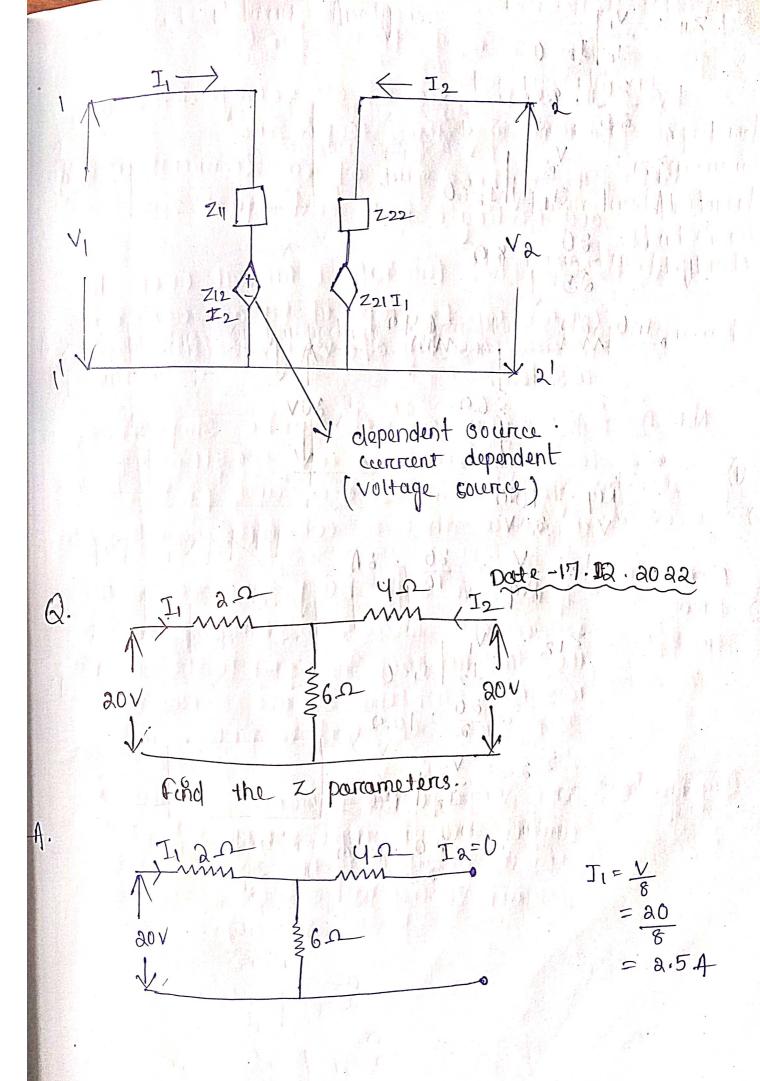
11 Property Value of the Value Power :-(10 V = Vm sin wt) R = Im sin (wt t p) Averigge power P = Averiage of ve P = Power in R + Power in C = I2R+0 = IR XI = IR X -VIXP = VI cos \$ Series A.C cenceet: -V -> supply voltage (r.m.s value) I -> resulting current (r.m. s value) VR -> voltage drop across raspetor VR = IR (VR is in phase with I) VL7 vourage drop across Enductor VL = IXL (VL Leads I by 90°) Ve -> voltage drop avross capacétore Vc = IXC (Vc logs I by 90°) current is taken as the reference phasor. OA respresents VR, AB represents VL & Ac Prepresent It may be seen that 1/2 is in phase opposition to ve Jet. It follows that the sercesst can either beeffectively inductive on capacetère depending upon which voltage drop (VL or Ve) is prodemina

for the case considered $V_L > V_c$ so that net voltage drop across L-c combination is $V_L - V_c$ and is represented by AD. Theseforce the applied voltage vis the phason sum of Thoseforce The and is represented by DD. $V = V_R^2 + (V_L - V_C)^2 = \sqrt{(IR)^2 + (IX_L - IX_C)^2}$ $= I = \frac{V}{R^2 + (X_1 - X_2)^2}$ The quantity R2+(xL-xc)2 offers opposition to current Flow and is called impedance of the concert. concert power factor $\cos \phi = \frac{R}{Z} = \frac{K}{[R^2 + (X_L - X_L)^2]}$ $tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R}$ Power consumed = [P = VI cos o] OR $p = I^2R$ we have seen that the impedance of a R-L-c serves cencuet is given by Z = \R2+(XL-Xc)2 (i) When $X_L - X_C$ is Posticye (i. 1 $X_L > X_C$), Phase angle ϕ is positive and the concept will be inductive. Will larg behind in Such case the concept to the applied voltage v by Q. (1) When XL-Xc is negative (i.e Xc >XL), phase angle \$ is nagative and the circulit with be 9s capacitère. The conceet current I and app leads the applied -(iii) when $x_L - x_C$ is zerro (i.e $x_C = x_L$) the certain is -The dreceet current I and applied voltage voil be in phase i.e. $\phi = 0^{\circ}$. The cercuit will then have unity power Factor.

gp V = Vm sin wt & = Im sin (wt ± 0) where Im = Vm/z . IN JACT XL V IV (XCXXL) mount of assistance in the second of the sec Philippin in principal in principal in principal in the works nation with the property V Drunt Grand Hotel While for the first work out 1. has placed 2 hours 110 hours 15 hours of Linder of the Art of the Ser Ben / Shuttill to ...







$$Z_{11} = \frac{V_{1}}{I_{1}} I_{2} = 0$$

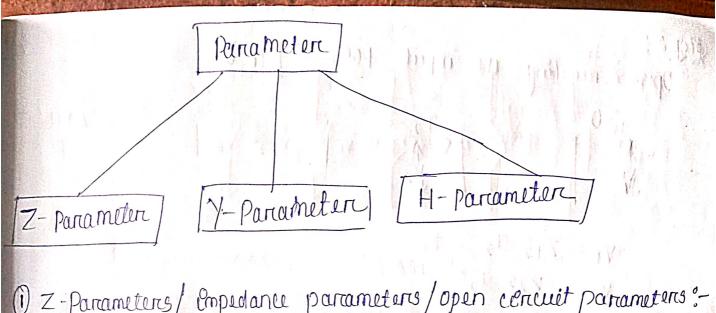
$$= \frac{20}{4.5} = 80$$

$$= \frac{20}{0.5} = \frac{20}{10} = 24$$

$$= \frac{20}{10} = 100$$

$$= \frac{20}{0.5} = 100$$

$$= \frac{20}{0.5} = 100$$



1) Z-Parameters/ Empedance parameters/open cencuit parameters:

$$V_1 = Z_{11}I_1 + Z_{12}I_2$$

 $V_2 = Z_{21}I_1 + Z_{22}I_2$

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

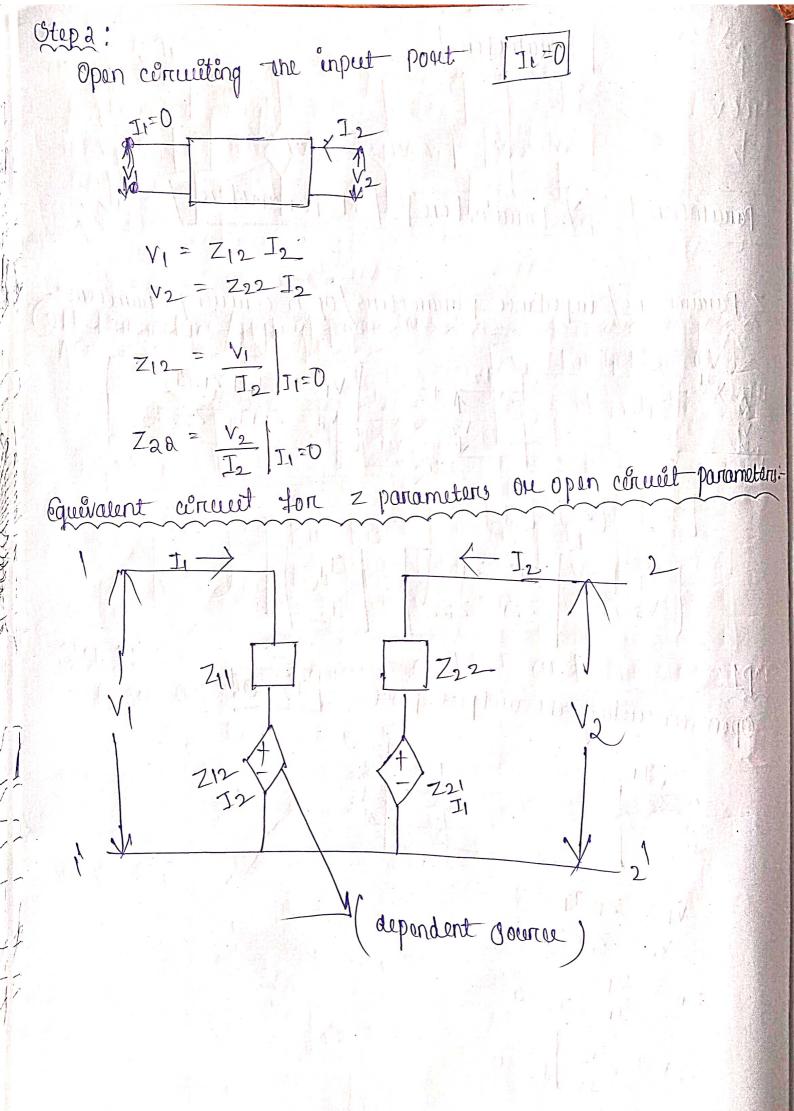
Otep1:

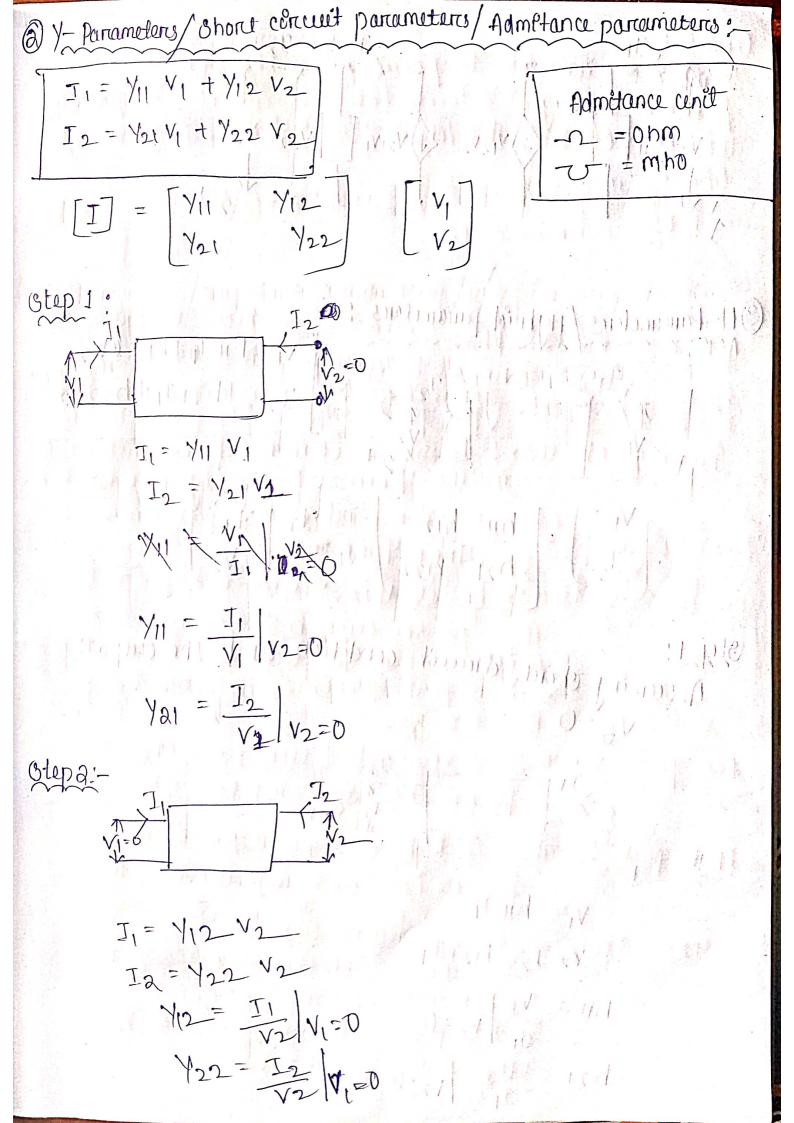
Open erruiting the output post [I2=0]

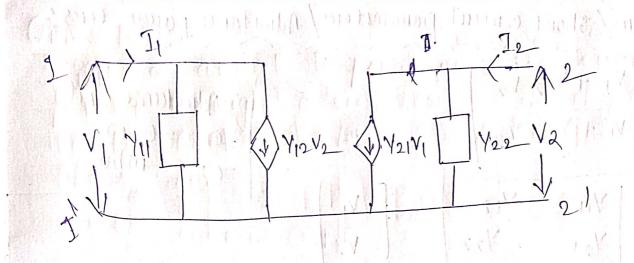
$$\begin{array}{c|c}
\hline
J_2=0 \\
\hline
V_2 \\
\hline
V_2
\end{array}$$

$$Z_{11} = \frac{V_1}{I_1} \mid I_2 = 0$$

$$Z_{21} = \frac{V_{2}}{I_{1}} | I_{2} = 0$$







3H-Parameters / Hybrid parameters :-

$$\begin{array}{c|c}
I_1 & I_2 \\
I_2 & I_3 \\
I_4 & I_4 \\
I_5 & I_6 \\
I_7 & I_7 \\
I_7 & I_8 \\
I_8 & I_9 \\
I_9 & I_$$

$$\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} = \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$$

Assuming short circuit condition and the output Otep 1:

$$\begin{array}{c|c}
\hline
 & \overline{12} & 2 \\
\hline
 & \overline{12} & 2$$

$$V_1 = h_1 I_1$$
 $V_2 = h_2 I_1$
 $h_1 = V_1 | V_2 = 0$
 $h_2 = I_2 | V_2 = 0$

