Lecture note on Geotechnical Engineering

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CHAPTER-1

INTRODUCTION

INTRODUCTIONOFSOIL

The word "Soil" is derived from the Latin word solium which, according to Webster's dictionary, means the upper layer of the earth that may be dug or plowed specifically, the loose surface material of the earth in which plants grow. The above definition of soil is used in the field of agronomy where the main concern is in the useof soil for raising crops.

In geology, earth's crust is assumed to consist of unconsolidated sediments, calledmantleorregolith,overlyingrocks. The term 'soil' is used for the upper layer of mantle which can support plants. The material which is called soil by the agronomist or the

geologist is known as top soil in geotechnical engineering or soil engineering. The top soil contains a large quantity of organic matter and is not suitable as

a construction material or as a foundation for structures. The top soil is removed earth's surface before the construction of structures.

 $The term `soil' in Soil Engineering is defined as an unconsolidated material, \ composed \ or \ an unconsolidated material.$

particles can be separated by such mechanical means as agitation in water.

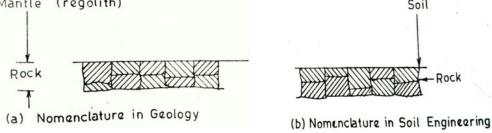


Fig.shows a cross-section through the earth's surface, indicating thenomenclature used in geology, and in Soil Engineering.

SOILANDSOILENGINEERING:-

The term 'soil mechanics' was coined by Dr. Karl Terzaghi in 1925 when his book Erdbaumechanic on the subject was published in German.

According to Terzaghi, 'Soil mechanics is the application of the laws of mechanics and hydraulics to engineering problems dealing with sediments and other unconsolidated accumulations of solid particles produced by the mechanical and chemical disintegration of rock, regarding ofwhether or not they contain anadmixture of organic constituents.

Soil mechanics is, a branch of mechanics which deals with the action of forceson soil and with the flow of water in soil.

The soil consists of discrete solid particles which are neither strongly bonded as in solids nor they are as free as particles of fluids. Consequently, the behavior of soil is somewhat intermediate between that of a solid and a fluid. It is not, therefore, surprising that soil mechanics draws heavily from solid mechanics and fluid materials. Asthesoilisinherently aparticulate system. Soil mechanics is also particulate mechanics.

DEFINITION OF SOIL ENGINEERING AND GEOTECHNICAL ENGINEERING:-

Soil Engineering in an applied science dealing with the applications of principles of soil mechanics to practical problems. It has a much widers cope than soil mechanics, as it details with all engineering problems related with soils. It includes site investigations, design and construction of foundations, earth-retaining structures and earth structures.

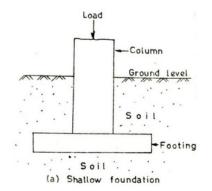
SCOPEOFSOILMECHANICS:-

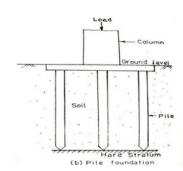
SoilEngineeringhasvastapplicationintheconstructionofvariousCivil Engineering works. Some of the important applications are as under.

(1) **Foundations:** – Everycivilengineeringstructure, whether it is abuilding, a

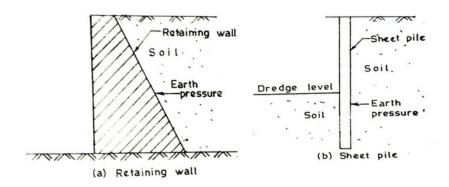
bridge, or a dam, is founded on or below the surface of the earth. Foundations are required to transmit the load of the structure to soil safely and efficiently.

A foundation is termed shallow foundation when it transmitted the load to upper strata of earth. A foundation is called deep foundation when the loadis transmitted to strata at considerable depth below the ground surface. Pile foundation is a type of deep foundation. Foundation engineering is an important branch of soil engineering.

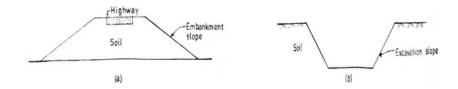




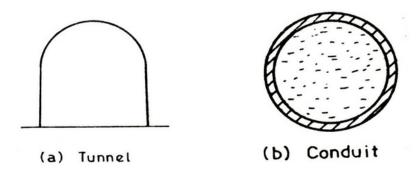
(2) **Retaining Structures:** – When sufficient space is not available for a massof soil to spread and form a safe slope, a structure is required to retain the soil. An earthretaining structure is also required to keep the soil at different levels on its either side. The retaining structure may be rigid retaining wallorasheet pile bulkhead which is relatively flexible (Fig. 1.3). Soil engineering gives the theories of earth pressure on retaining structures.



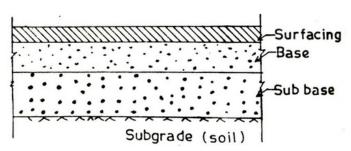
(3)**Stability of Slopes:** – If soil surface is not horizontal, there is a component of weight of the soil which tends to move it downward and thus causes instability of slope. The slopes may be natural or man-made Fig. 1.4 shows slopes in filling and cutting. Soil engineering provides the methods for checking the stability of slopes.



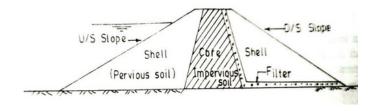
(4)**Underground structures:** – The design and construction of underground structures, such as tunnels, shafts, and conduits, require evaluation of forces exerted by the soil on these structures. These forces are discussed in soil engineering. Fig. 1.5 shows a tunnel constructed below the ground surface and a conduit laid below the ground surface.



(5)**PavementDesign:**–Apavementishardrustplacedonsoil(subgrade) for the purpose of proving a smooth and strong surface on which vehiclescanmove. Thepavementconsists ofsurfacing, suchasabitumenlayer, base and subtheme (Fig. 1.6). The behavior of sub grade under vicious conditionsofloadingandenvironmentchangeisstudiedinsoil engineering.



(6)**Earth Dom:** – Earth dams are the structures in which soil is used as a constructionmaterial. The earth dams are built for creating water reservoirs. Since the failure of an earth dam may cause widespread catastrophecare is taken in its designand construction. It requires thorough knowledge at soil engineering.



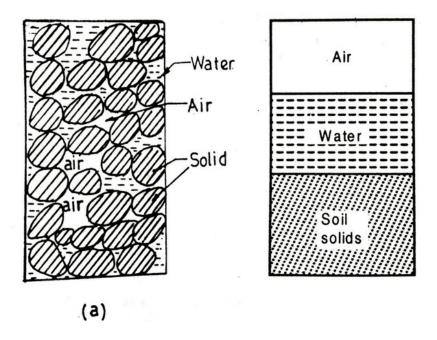
(7)**Miscellaneous soil:** - The geotechnical engineer has sometimes to tackle miscellaneous problems related with soil. Such as soil heave, soilsubsidence, frost heave, shrinkage and swelling of soils.

CHAPTER-2 PRELIMINARYDEFINATIONAND RELATIONSHIP

SOILASATHREEPHASE:

Asoilmassconsistsofsolidparticleswhichfromaporousstructure. The voids in the soil mass may be filled with air, with water or partly with air and partlywith water. In general, a soil mass consists of solid particles, water and air. The three constituents areblended together toform acomplex material (Fig.2.1. a) . However, for convenience, all the solid particles are segregated and placed in the lower layer ofthe three-phase diagram (Fig. 2.1b). Likewise, water and air particles are placed separately, as shown. The 3-phase diagram is also known as Block diagram.

Itmaybenotedthattheconstituentscannot be

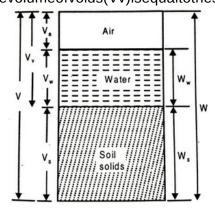


Actually segregated, as shown. A 3-phase diagram is an artifice used for easy understand and convenience in calculation.

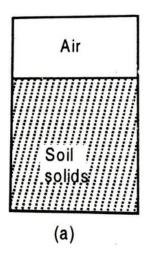
Although the soil is a three-phase system, it becomes a two-phase system in the following two cases:(1) When the soil is absolutely dry, the water phase disappears(Fig. 2.2a). (2) When the soil is fully saturated three is no air phase (Fig.2.2b). It is the relative proportion of the three constituents and their interaction that governs the behavior and properties of soils. The phase diagram is a simple, diagrammatic representation are alsoil, Itisextremely useful for studying the various terms used in soil engineering and their interrelationships.

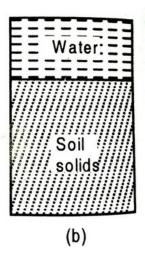
In a 3-phase diagram it is conventional to write values on the left side and the mass on the right side (Fig.2.3a). The mail simple of a gives soil mass in designated as V. It is equal to the sum of the volume of solids (V1), the volume of water (F) and the volumeofair(Va). The volume of volume

and air

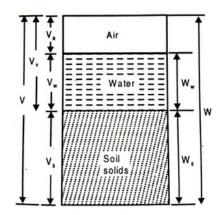


Thesoilmassofthesoil...isrepresentedasM.themassofair(ma)is very smalland is neglected. Therefore, the social mass of the soil is equal to the mass of solids (M2)andthemassofwater(Mw).Fig.2.36showsthe3-phasediagraminwhichthe weights are written on the right side.





WEIGHTVOLUME RELATIONSHIPS:



WATER CONTENT: - The water content (w) is defined as the ratio of the mass water to the mass of solids.

$$W = \frac{Ww}{Ws}$$

Thewatercontentisalsoknownasthemoisturecontent(m). It is expressed as a percentage, but whenever used in equation used as a decimal.

The water content of the fine-grained soils, such as silts and clays, in generally more than that of the coarse grained soils, such as gravels and sands.

The water content of some of the fine-gained soils may be even more than 100%, which indicates that more than 50% of the total mass is that of water. The water content of a soil is an important property.

SPECIFICGRAVITY(G):-

The specific gravity of solid particles (G) is defined as the ratio of the mass of a given volume of solids to the mass of an equal volume of water at 40C. Thus, the specific gravity is given by $G = \frac{\rho s}{\rho w}$

*Themassdensityofwater pwat40Cisonegm/ml,1000kg/m3or1 Mg/m3.

Thespecificgravityofsolidsformostnaturalsoilsfallsinthegeneralrange of 2.65to2.80,thesmallervaluesarefor thecoarse-grainedsoils. Tablegives the average values of specific gravityfor different soils. It may be mentioned that the specificgravityofdifferent particles in a soil mass may not be the same. Whenever

the specific gravity of a soil mass is indicated, it is the average value of all the solid

particlespresentinthesoilmass. Specific gravity of solids is an important parameter. It is used for determination of void ratio and particle size.

Table:TypicalValuesof G

Sl.No.	SoilType	SpecificGravity
1	Grevel	2.65-2.68
2	Sand	2.65-2.68
3	Sands	2.66-2.70
4	Slit	2.66-2.70
5	InartisticClays	2.68-2.80
6	OrganicSoils	Variable,mayfallbelow2.00

Besidesthefollowingtwotermsrelatedwiththespecificgravityarealso used.

(1) MassSpecificGravity(Gm):- Itisdefinedastheratioofthemass density of the soil to the mass density of water.

The value of the specific gravity of solids.

The mass specific gravity is also known as the apparent specific gravity or thebulk specific gravity.

(2)Absolute Specific Gravity (Ga):- The soil solids are not perfect solids but contain voids. Some of these voids are permeable through which water canenter, whereas others are impermeable. Since the permeable voids get

filledwhenthesoil is wet, these are in reality a part ofvoid spacein the total mass and not apart of soil solids. If both the permeable and impermeable voids are excluded from the volume ofsolids ,the remaining volume is the true orabsolute volume of the solids.

The mass density of the absolute solids is used for the determination of the absolute specific gravity of solids.

VOIDS RATIO: - It is defined as the ratio of the volume of voids to the volume of solids.

The void ratio is expressed as a decimal, such as 0.4,0.5, etc. For coarse-grained soils, the void ratio is generally smaller than that for fine-grained soils. For some soils, void ratio may have a value even greater than unity.

POROSITY:-Itisdefinedastheratioofthevolumeofvoidstothetotal volume.

$$n = \frac{Vv}{v}$$

ThePorosityisgenerallyexpressedaspercentage.However,inequations,it is is used as a ratio. For example; a porosity of 50% will be used as 0.5 in equations. The porosity of a soil cannot exceed 100% as it would mean Vv is greater than V, which is absurd. Porosity is also known as percentage voids.

Both porosity and void ratio are measures of the denseness (or looseness) of soils.

More Asthesoilbecomesmoreandmoredense, theirvaluesdecrease, Thetermporosityis commonly used in other disciplines such as agricultural engineering. In soil engineering, thetermvoidratioismorepopular. It is more convenient to usevoid ratio than porosity. When the volume of a soil mass changes, only the numerator (i.e. Vv) in the void ratio changes and the denominator (i.e. Vs) remains constant.

However, if the term porosity is used, both the numeration and the denominator change and it become inconvenient.

Relationshipbetweenthevoidratioandtheporosityas under.

$$\frac{1}{\mathbf{H}} = \frac{V}{V} = \frac{VVVV}{V}$$

$$\frac{1=1+}{\pi}$$
 $\frac{1}{6}=\frac{1+6}{6}$

$$n = \frac{1}{e_{1+}}$$
 (1)

$$\frac{1}{e} = \underline{1} = \underline{1}$$

Theporosityshouldbeexpressedasaratio(andnotpercentage).

PERCENTAGEOFAIRVOIDS(na):-

Itistheratioofthevolumeofairtothetotal volume.

Itisrepresentedasapercentage.

AIR CONTENT (ac): - Air content is defined as the ratio of the volume of air to the volume of voids.

$$ac = \frac{Va}{Vv}$$

The Aircontentisus ually expressed as a percentage. Both aircontent and the percentage air voids are zero when the soil is saturated (Va= 0).

Relationship between the percentage air voids and the air content can be obtained.

$$na = \frac{Va}{V} = \frac{VaVv}{Vv} \frac{V}{V}$$

na=nxac

Degree of Saturation (S) - The degree of saturation (S) is the ratio of the volume of water to the volume of voids.It is also represents as Sr.

$$S = \frac{Vw}{Vv}$$

Thedegreeofsaturationisgenerally expressed as a percentage.

It is equal to zero when thesoil is absolutely dry and 100%when thesoil is fully saturated. Degree of saturation is used as a decimal in expressions.

DENSITYINDEX:-

Itthemostimportantindexpropertyofacohesionless soil.

It is also known as Density Index (ID). It is also known as relative density or degreeofdensity. It is used to express the relative compactness of an atural soil deposit.

It is the ratio of the difference between voids ratio of the soil in its loosest state and its natural voids ratio to the difference between voids ratio in the loosest anddensest states.

Whereemax= Maximum void ratio of the soil in the loosest condition.

emin= Minimum void ratio of the soil in the densest condition.

e=voidratioofthesoilinthenatural state.

emaxwill found out from ymin i,e in the loosest condition. eminwill found out from ymax i,e in the densest condition.ewill found out from yd i,e in the natural

Dr=
$$\gamma_{\overline{e}}$$
1 $\frac{\overline{Gvwvmin}}{1+\frac{7}{7s}} = \frac{\overline{Gyw}}{1+e}$

$$d = \frac{\overline{Gyw}}{1+e}$$

emaxThe relative density of a soil gives a more clear idea of the denseness than does the void ratio.

BULKUNITWEIGHTY:-

Thebulkunitweightisdefinedasthetotalweightpertotal volume.

$$y = \frac{W}{V}$$

It is also known as total unit weight (yt) or wet unit weight.

In SI units it is express as N/mm3 or KN/mm3

DRYUNITWEIGHT:-

Thedryunitweightisdefinedastheweightofsolidspertotal volume.

$$yd = \frac{W_s}{}$$

SATURATEDUNITWEIGHT:-

The saturatedunit weight is the bulk unit weightwhen the soil is fully saturated.

$$\gamma$$
sat = $\frac{W_{sat}}{V}$

SUBMERGEDUNITWEIGHT: -

Whenthesoilexistsbelowwaterthanitiscalled submergedcondition.

The submerged unit weight (γ') of the soil is defined as the submerged weight per total volume.

ysub =
$$\frac{W_{sub}}{V}$$

RelationbetweenG,S,e, y&yw:-

$$\gamma = V = V_S + W_W G V_S y_W + V_W y_W Y_S + V_V = V_S + V_V$$

DividingVsbothnumerator& denominator

$$Or, y = \underbrace{\frac{Gyw + (\frac{1}{7}yw\underline{7}w}{1 + \frac{7w}{7s}}}_{1 + \frac{7w}{7s}} = \underbrace{\frac{(G + xx)yyw}{1 + \frac{7w}{7s}}}_{1 + \frac{7w}{7s}} = \underbrace{\frac{(G + Se)yw}{1 + 7s}}_{1 + 7s}$$

Or,
$$\gamma = (G+Se)yw1$$
....(3)

Asthedegreeofsaturationis100%forasaturatedsoil,thentheS= 1

Or,
$$\gamma$$
sat= $\frac{(G+e)\gamma w1}{+e}$(4)

Similarly, yd=
$$\frac{Ws}{v} = \frac{Ws}{v_{s+Vv}} = \frac{GVsyw}{v_{s+Vv}}$$

DividingVsbothnumerator& denominator

$$yd = \frac{Gyw}{1+7s} = \frac{Gyw}{1+e} \dots (5)$$

Weknownthatysub=ysat-yw

$$=\frac{(G + e)yw}{1 + e}$$
 -VW= $(G_{T_1})yw$

$$\begin{split} \text{Weknownthatw=} & \frac{w_w}{w_s} & \text{(Asyw=} & \frac{w_w}{v_w} \& ys = \frac{w}{s} \text{)} \\ & = \frac{v_{wyw}}{v_{sys}} \\ & = \frac{v_w}{v_v} x \frac{v_v}{v_s} x \frac{y_w}{y_s} \\ & = S.e. \frac{1}{G} & \text{(AsS=Vw} \frac{v_w}{v_w} \& G = \frac{v_w}{v_w} \text{)} \end{split}$$

w.G=S.e
e=
$$\frac{\text{w.G}}{\text{s}}$$

Relationbetweene.S&na:-

$$na = \frac{Va}{V} = \frac{Vv}{VwVv}$$

DividingVsbothnumerator& denominator

$$\frac{7x - 7w}{-7s} \qquad \frac{7x 7x}{-7s} \qquad e-Se$$

$$\frac{7s 7s}{-7s} \qquad 0 \qquad 7v \qquad 7s$$

$$n_{a=} \frac{1}{(1-S)e} \frac{1}{1+e} \frac{1}{7575}$$

RelationbetweenS&ac:-

$$a_{c=} \frac{v_a}{v_v} = \frac{v_v}{v_w} = 1 - \frac{v_w}{v_v} = 1 - S....(8)$$

RelationbetweenNa,ac & n:-

$$\text{na} = \begin{cases}
 \text{va} \\
 \text{va} \\
 \text{va}$$

$$\text{vavv} \\
 = \frac{\mathbf{vv}}{\mathbf{v}} -$$

RelationbetweenG.na.e.yd&yw:-

$$1=\nabla^{V_{s}} + \frac{V_{v}}{V} + \frac{V_{w}}{V} = \nabla^{V_{s}} + \frac{V_{v}}{V} + n_{a}$$

$$1-n \quad V_{s} \quad V_{v} \quad W_{s}/G_{\gamma w}W_{w}/\gamma w} + \frac{1}{V} + \frac{V_{w}}{V} + \frac{V_{w$$

Relationbetweenw, y d& y:-

$$W = \frac{Ww}{Ws}$$

$$Or,1+w=1+ \frac{Ww}{Ws} = Ws+Ww$$

$$Or,Ws = \frac{W}{1+w}$$

$$Or,yd.V = \frac{W}{1+w}$$

$$Or,yd. = \frac{W(1}{+w)V} = \frac{y}{(1+w)}$$

$$Or,yd. = \frac{y(1}{+w)} = \frac{y}{(1+w)}$$

$$Or,yd. = \frac{y(1)}{+w} = \frac{y}{(1+w)}$$

$$Or,yd. = \frac{y}{(1+w)} = \frac{y}{(1+w)}$$

CHAPTER-3 DETERMINATIONOFINDEX PROPERTIES

WATERCONTENTDETERMINATION:

- ☐ Thewatercontentofasoilisanimportantparameterthatcontrolsits behaviour.
- T Itisaquantitativemeasureofthewetnessofasoilmass.
- ☐ Thewatercontentofsoilmasscanbedeterminedbythefollowingmethods:
- 1. Ovendryingmethod
- 2. Pycnometermethod

(1) Ovendryingmethod:

- Theovendryingmethodisastandardlaboratorymethodandthisisavery accurate
- method.
- Inthismethodthesoilsampleistakeninasmall,non-corrodible,airtight container.
- Themassofthesampleandthatofthecontainerareobtainedusingan accurate weighing balance.
- Thesoilsampleinthecontaineristhendriedinanovenatatemperatureof 110°c ± 5°c for 24 hours.

Thewatercontentofthesoilsampleisthencalculatedfromthefollowing equation:

W=Mw/Ms

$$= \frac{M2-M}{M_3-M_1} \times 100$$

WhereM1=massofcontainerwithlid

M2 = mass of container, lid and wet soil

M3=massofcontainer, lidanddry soil

(2) Pycnometermethod:

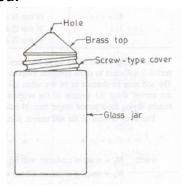


Figure 3.1 Pycnometer

A pycnometer is a glass jar of about 1 litre capacity and fitted with a □ brass conical cap by means of screw Thecaphasasmallholeof6mmdiameteratitsapex.Arubberorfibre washer is placed between the cap and the jar to prevent leakage. There is a mark on the cap and also on the jar. The cap is screwed down to the same mark such that the volume of the pycnometer used in the calculations remains Thepycnometermethodforthedeterminationofwatercontentcanbeused only if the specific gravity of solid particle is known. A sample of wet soil about 200 to 400 gm is taken in the pycnometer and weighed. ☐ Wateristhenaddedtothesoilinthepycnometertomakeitabouthalffull. The contents are thoroughly mixed using a glass rod to remove the entrappedair. More and more water is added and stirring process continued till the pycnometer is filled flush with the hole in the conical cap. ☐ Thepycnometeriswipeddryandweighed. The pycnometer is then completely emptied. It is washed and filled with water,

mass of pycnometer + wet soil

M3=massofpycnometer+wetsoil+ water

M4=massofpycnometerfilledwithwater only

LetM1=massofpycnometer M2 =

ThemassM4isequaltomassM3minusthemassofsolidsMsplusthemassofan equal volume of

flush with the top hole. Thepycnometeriswipeddryandweighed.

$$\begin{array}{lll} & \underset{d}{\text{Mas}} = \text{MS} + \underset{d}{\text{Ms}} = \text{MS} + \underset{d}{\text{Ms}$$

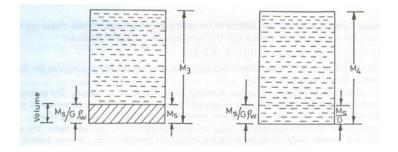


Figure 3.2

PycnometermethodDerivation

Thismethodforthedeterminationofthewatercontentissuitableforcoarse grained soils from which the entrapped air can be easily removed.

SPECIFICGRAVITY:

- Thespecificgravityofsoilsolidscanbedeterminedby:
 - (i) A50mldensitybottleor
 - (ii) A500mlflaskor
 - (iii) Apycnometer
- Thedensitybottlemethodisthemostaccurateandissuitableforalltypesof soil.

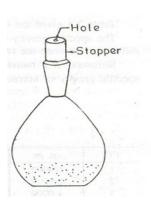


Figure 3.3

Densitybottle

- Theflaskorpycnometerisusedonlyforcoarsegrained soils.
- $\begin{tabular}{ll} \hline \end{tabular} \begin{tabular}{ll} The density bottlemethod is the standard method used in the laboratory. \end{tabular}$
- ☐ Intheabovethreemethodsthesequenceofobservationis same.
- ☐ ThemassM1oftheempty,dry,bottleisfirsttaken.
- Asampleofovendriedsoilcooledinadesiccatorisputinthebottleandthe mass M2 is taken.

The bottle is then filled with distilled water gradually removing the entrappedair
either by applying vacuum or by shaking the bottle.
\Box Finally,thebottleisemptiedcompletelyandthoroughlywashedandclean water is
ightharpythesisticisempletesythathoroughlywashedandelean water is
IfthemassofsolidMsissubtractedfromM3andreplacedbythemassof water equal to
the volume of solid the mass M4 is obtained.
M4=M3-Ms+ Mshw
Gpw
Or,Ms(1- $\frac{1}{G}$)=M3-M4
ButMs=M2–M1
Therefore(M2–M1)(1- $\frac{1}{}$)=M3–M4
Therefore(M2–M1)(1- $\frac{1}{G}$)=M3–M4 Or($\frac{1}{M}$ 2–M1)=(M2–M1)–(M3– M4)
Or G = $\frac{M2-M}{M}(M2-$ (i)
M(I)
AlternativelyG=(ii)
Ms+M4-M3 Equation(1)givesthespecificgravityofsolidsatthetemperatureatwhichthetest was
conducted.
Specificgravityofsolidsisgenerallyreportedat27°Corat4°C.Thespecificgravity at 27°C
and 4°C can be determined from the following equation
G27=Gt×specificgrayityofwaterate/C
And G4 = Gt × specific gravity of water at t°C
Where G27 = specific gravity of particles at 27°C
G4 = specific gravity of particles at 4°C
Gt=specificgravityofparticlesat t°C
PARTICLESIZEDISTRIBUTION:
Д The percentage of various sizes of particle in a given dry soil sample is
found by a particle size analysis or mechanical analysis.
Mechanicalanalysismeansseparationofasoilintoitsdifferentsize fractions.
Themechanicalanalysisisperformedintwostages
(i) Sieveanalysis
(ii) Sedimentationanalysisorwetmechanicalanalysis
The first stage is meant for coarse grained soil only while the second
\blacksquare stage is performed for fine grained soils.

In general a soil sample may contain both coarse grained particles aswell as fine Particles and hence both the stages of the mechanicalanalysis may

be necessary.

SieveAnalysis:

	_	In the Indian standard the sieves are designated by the size of the aperature in mm.	
		The sieve analysis can be divided into two parts i.e the coarse analysis	
	ш	and fine analysis. Anovendriedsampleofsoilisseparatedintotwofractionsbysieving it through	
		a 4.75 mm I.S sieve.	
		Theportionretainedonitistermedasthegravelfractionandiskept for the coarse analysis while the portion passing through it is subjected fine sieve analysis. The following sets of sieves are used for coarse sieve analysis: IS: 100,	
	_	63, 20, 10 and 4.75 mm.	
		The sieves used for fine sieve analysis are: IS: 2 mm, 1.0 mm, 600,425, 300, 212, 150 and 75 micron.	
		Sieving is performed by arranging the various sieves one over the otherin the order of their mesh openings – the largest aperature sieve being kept at the top and the smallest aperature sieve at the bottom.	
	11	A receiver is kept at the bottom and a cover is kept at the top of whole assembly.	
		The soil sample is put on the top sieve and the whole assembly is fitted	
	п	on a sieve shaking machine.	
		The amount of shaking depends upon the shape and the number of	
	_	particles. Atleast10minutesofshakingisdesirableforsoilswithsmall particles.	
	_	Theportionofthesoilsampleretainedoneachsieveisweighed.	
	_	The percentage of soil retained on each sieve is calculated on the basisof the total mass of soil sample taken and from this percentage passing through each sieve is calculated.	
SedimentationAnalysis:			
	_	In the wet mechanical analysis or sedimentation analysis the soilfraction finer than 75 micron size is kept in suspension in a liquid (usually water) medium.	
	_	The analysis is based on stokes law according to which the velocity at which grains settle out of suspension, all other factors being equal, is dependent upon the shape, weight and size of the grain.	
	_	However in the usual analysis it is assumed that the soil particles are	
		spherical and-have the same specific gravity.	
		With this assumption the coarser particles settle more quickly than the finer ones.	

☐ If v is the terminal velocity of sinking of a spherical particle it is given by

$$V = \begin{cases} 2r\frac{2\gamma s - \gamma w}{9} & \Pi \\ 1\frac{D2\gamma s - \gamma w}{1} & \Pi \end{cases}$$
Orv= 18 Π

Where r = radius of the spherical particle (m)

D = diameter of the spherical particle (m)

v=terminalvelocity (m/sec)

ys=unitweightofparticles(KN/m³)

y=uni tweightofliquidorwater(KN/m²)

- = viscosity of liquid or water (KN s/m2) = μ /g μ
- = viscosity in absolute units of poise

g=accelerationdueto gravity

Ifwaterisusedasthemediumforsuspensionis qualto 9.81 KN/rh. Similarly

ys=Gyw.Substitutingthisweget

The above formula should be expressed in the consistent units of meters, seconds andkilo newton.

Ifthediameter(D)oftheparticlesisinmmwe have

$$v = \frac{{}^{1}_{18}(D/1000)2G-1)\gamma w}{{}^{1}_{11}}$$
$$= \frac{{}^{1}_{12}\gamma w(G-}{1)18\times106}\mu$$

Takingy=9.81KN/m3 Wegetv= $^{D2}(G-1)$

D=
$$\sqrt{\frac{\frac{1.835 \times 106 \text{µ18} \times}{106 \text{µV}}}{\frac{106 \text{µV}}{\text{µV}}}}$$
mm

D=1355
$$\sqrt{\frac{\pi v}{G-1}}$$
 mm

It should be noted that 1poise is equivalent to 0.1 Ns/m2 or to 10-4 KN s/m2If a particle ofdiameter D mm falls through a height of He cm in t minutes.v = He/60t cm/sec

=He/6000tm/sec

	reequationwe	

$$D = \sqrt{\frac{(G-1)\gamma w \times 6000t}{\frac{3000u}{(G-1)\gamma w}} \sqrt{\frac{H_e}{t}}}$$

$$D = 10F \sqrt{\frac{H_e}{t}}$$

Where F=105 $\sqrt[3000\overline{\mu}]{(G-1)\gamma w}$ is a constant factor for given values of μ and μ .

D2(G-1)

At 27°C, the viscosity μ of the distilled water is approximately 0.00855 poise. Since 1 poise is equivalent to 10-4 KN-s/m2

We have $\mu = 0.00855 \times 10-4 \text{ KN-s/m2}$

TakinganaveragevalueofG=2.68

Puttingthesevalueinv=
Wegev= $\frac{D^{0.81)} (2.68-1)^{0.1835 \times 10^{0.1}}}{18 \times 106 \times 0.0085 \times 10-4}$ =1.077D2(m/sec)

Thisisanapproximatieversion of Stoke's lawand can be easily remembered for determination.

- Thesedimentationanalysisisdoneeitherwiththehelpofhydrometer or a pipette.
- In both the methods a suitable amount of oven dried soil sample, finer than 75 micron size is mixed with a given volume V of distilled water.
- The mixture is shaken thoroughly and the test is started by keeping thejar containing soil water mixture, vertical.
- Atthecommencement of sedimentation test soilparticles are assumed to be uniformly distributed throughout the suspension.
 - After any time interval t, if a sample of soil suspension is taken from a height He (measured from the top level of suspension), only those particleswillremain in thesuspensionwhichhavenotsettledduring this time interval.

particles sizes retained at this depth He.

 $\begin{tabular}{ll} \hline \square & The greater the time interval tallowed for suspension to settle, the $$\Box$ & are the $$$

Hence sampling at different time intervals, at this sampling depth He

would give the content of particles of different sizes. If at any time interval t, MD is the mass, per ml, of all particles smaller than the diameter D still in suspension at the depth He the percentage

 $N = \frac{MD}{Md/V} \times 100$ finer than D is given by

WhereN=percentagefinerthanthediameter D

Md = total dry mass of all particles put in the suspension

V = volume of suspension

Thuswiththehelpofaboveequationswecangetvarious diameter Dandthe percentage of particles finer (N %) than this diameter.

Limitationofsedimentationanalysis:

- (1)The sedimentation analysis gives the particle size in terms of equivalent diameter, which is less than the particle size given sieve analysis. The soil particles are not spherical. The equivalent diameter is close to the thickness (smallest dimension) rather than the length or width.
- (2)Asthespecificgravityofsolidsfordifferentparticlesisdifferent,theuse of averagevalueofG is asourceof error. However as the variation of the values of G is small the error is negligible.
- (3)Stokeslaw is applicable only when the liquid is infinite. The presence of walls of the jar affects the result to some extent.
- (4)Instokeslawithasbeenassumedthatonlyonespheresettleandthereis no interface from other spheres. In the sedimentation analysis as many particles settle simultaneously there is some interface.
- (5) The sedimentation analysis cannot be used for particles larger than 0.2 mmas turbulent conditions develop and stokes law is not applicable.
- (6)The sedimentation method is not applicable for particles smaller than 0.2μ because Brownian movement takes place and the particles do not as per Stokes law.

PIPETTEMETHOD:

- ☐ Thepipettemethodisthestandardsedimentationmethodusedinthe laboratory.
- Theequipmentconsistsofapipette, ajarandanumber of sampling bottles.
- \square Generallyaboilingtubeof500mlcapacityisusedinplaceofajar.

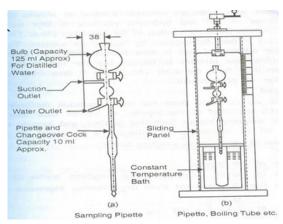


Figure 3.4

	_	The figure shows a pipette for extracting samples from the jar from a desired depth (He).
	_	The pipette consists of a 125 ml bulb with stop cock for keepingdistilled
		water, a three way stop cock, suction and waste water outlets,
	_	sampling
		Pinethe phylometre of 10 cm (He) atvarious The methodognalists indrawing of some based of 10 cm (He) atvarious The methodognalists indrawing of some based of 10 cm (He) atvarious
		Therecommended time intervals are: ½, 1, 2, 4, 8, 15 and 30 minutes
	_	and 1, 2, 4, 8, 16 and 24 hours reckoned from the commencement of the test.
	_	The pipette should be inserted in the boiling tube about 25 seconds
		before the selected time interval and the time taken for sucking the
		sample should not be more than 10 to 20 seconds.
		Each sample so taken is transferred into suitable sampling bottles and
	□	dried in an oven.
		ThemassMDofsolidspermlofsuspensionisthusfoundbytaking the dry mass and dividing it by 10.
Methodof		paringsoilsuspension:
	_	In the sedimentation analysis only those particles which are finer than 75
	_	micron size are included.
	_	About 12 to 30 gm of oven dried sample is accurately weighed and mixed with distilled water in a dish or beaker to form a smooth thin
		paste. To have proper dispersion of soil a dispersing agent is added to the soil. Some of the common dispersing agents are sodium oxalate, sodium
		silicate and sodium polyphosphate compounds such as tetra sodium
		pyrtippin osphate, sodium hexametaphosphate and
		tripolyphosphate.
	_	IS2720recommendstheuseofdispersingsolutioncontaining33gm of the
		sodium hexametaphosphate and 7 g of sodium carbonate in distilled
		water to make one litre of solution.
	_	25 ml of this solution is added to the dish (containing the soil and distilled water) and the mixture is warmed gently for about 10 minutes.
	_	The contents are then transferred to the cup of a mechanical mixer, using
		a jet of distilled water to wash all traces of the soil out of the evaporating
		dish.
	_	Thesoilsuspensionisthenstirredwellfor15minutes.
	_	The suspension is then washed through 75 micron IS sieve, using jet of distilled water and the suspension, which has passed through the sieve is
		distilled water and the suspension, which has passed through the sieve, is transferred to the 500 ml capacity boiling tube (sedimentation tube).
	_	Thetubeisthenfilledtothe500mlmarkbyaddingdistilledwater.
		, ,

0	Thetubeisthenputinaconstanttemperaturewaterbath. Whenthetemperatureisthentubehasbeenstabilisedtothe temperature of the bath, the soil suspension is thoroughly shaken by inverting the tube several times, and then replaced in the bath. The stop was
	then started and the soil samples are collected at various time intervals with the help of pipette.
Calculation	ofDandN:
_ _ _	10 ml samples are collected from the soil suspension (sedimentation tube)fromadepthof10cm,withthehelpofthepipetteatvarious time intervals. The samples are collected into the weighing bottles (sampling bottles) and kept in the oven for drying. The mass MD, per ml of suspension so collected is calculated as under:
-	ss of sample in the weighing bottle/VP Jumeofthepipette
	volume of sample collected in the weighing bottle = 10 ml
•	ge finer is calculated from the following expression
N'=M m D-7×10	00
MD_ 7	nass of dispersing agent present in the in the total suspension of
volumeV	idos of dispersing agent present in the in the total suspension of
V = v	rolume of suspension = 500 ml
N' =	percentage finer based on MD
HYDROMET	ERMETHOD:
0	The hydrometer method of sedimentation analysis differs from thepipette analysis in the method of taking observation.
Ц	In the pipette analysis the mass MD per ml of suspension is founddirectly by collecting a 10 ml sample of soil suspension from the samplingdepthHe.HoweverinthehydrometeranalysisMDis
	indirectly by reading the density of the soil suspension at a depth He at various time intervals.
	In the pipette test the sampling depth He is kept constant while in the hydrometer test, the sampling depth He goes on increasing as theparticles settle with the increase in the time interval. It is therefore necessary to calibrate the hydrometer.

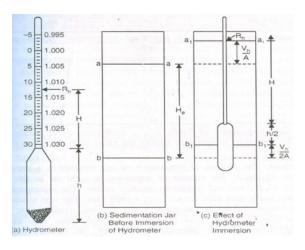


Figure 3.5

Calibrationofhydrometer:

- The readings on the hydrometer stem give the density of the soil suspension situated at the centre of the bulb at any time.
- For convenience, the hydrometer readings are recorded aftersubtracting 1 and multiplying the remaining digits by 1000. Such a reduced reading is designated as Rh.
- For example, if the density reading at the intersection of horizontal surfaceofsoilsuspensionwiththestemis1.010,itisrecordedas10 i.eRh=10.
- As indicated in figure the hydrometer reading Rh is increase in the downward direction towards the hydrometer bulb.
- Let H be the height in cm between any hydrometer reading Rh and the neck, and h the height of the bulb.
- Figure(b)showsthejarcontainingthesoilsuspension.
 - When the hydrometer is immersed in the jar as shown in figure (c) the waterlevelaarisestoa1a1,therisebeingequaltothevolumeVhof thehydrometer dividedby theinternal areaofcrosssectionA ofthe jar.
- ☐ Similarly the level bb rises to b1b1, where bb is the level situated at a depth He below the top level aa, at which the density measurements of the soil suspension are being taken.
- ☐ Therisebetweenbbandb1b1willbeapproximatelyequaltoVh/2A.
- The level b1b1 is now corresponding to the centre of the bulb, but the soil particles at b1b1 are of the same concentration as they were at bb. Thereforewehave

$$H = \begin{pmatrix} h & V & \Pi \\ H + + & hV \end{pmatrix} - h$$

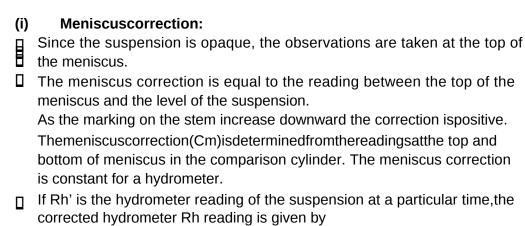
$$e & \frac{1}{2} & \frac{1}{2} A \qquad A$$

$$= H + \frac{1}{2} (h - \frac{1}{2} h)$$

	_	In the above expression there are two variables: the effective depth He and the depth H which depends upon the hydrometer
		reading Rh. Therefore by selecting various hydrometer reading
		Rh, the depth H can be measured with the help of an accurate scale and the
		corresponding
		depth He can be found.
·	_	Theheighthofthebulbisconstant.SimilarlyVhandAareconstant.
Testproce	du	Tofindthevolumeofthehydrometer it isweighed accurately. The re:
	_	mass of
		The hydrodrothe paration of spilothers in the sandwashydrometen the spilothers.
		Howeverthevolumeofsuspensionis1000mlinthiscaseandhence doubles the
		quantity of dry soil and dispersing agent is taken.
		Thesedimentationjarisshakenvigorouslyandisthenkeptvertical over a
		solid base.
		Thestopwatchisstartedsimultaneously.
İ		Thehydrometerisslowlyinsertedinthejarandreadingsaretakenat
		½,1and2minutestimeinterval.Thehydrometeristhentakenout.
		Morereadingsarethentakenatthefollowingtimeintervals:4,8,15, 30 minutes and 1, 2, 4 hours etc.
		To take the reading, the hydrometer is inserted about 30 seconds before
		thegiventimeinterval, so that it is stable at the time when the reading is to be
		taken.
		Sincethesoilsuspension isopaquethereading istaken corresponding to the upper level of the meniscus.

Correctiontothehydrometer reading:

Thehydrometerreadingsarecorrectedas under:



Rh=Rh'+ Cm

		The hydrometer is generally calibrated at 27°C. If the temperature of suspension is different from 27°C a temperature correction (Ct) is		
		required for the hydrometer reading. If the temperature is more than 27°C, the suspension is lighter and the actual reading will be less than the corrected reading. The temperature		
		correction is positive. On the other hand, if the temperature is less than 27°C the temperature correction is negative.		
	(iii)	Dispersionagentcorrection:		
		Addition of the dispersing agent to the soil suspension causes anincrease in the specific gravity of the suspension.		
		Thereforethedispersingagentcorrectionisalwaysnegative. The dispersing agent correction (Cd) can be determined by noting the		
		hydrometer reading in clear water and again in the same water after adding the dispersing agent.		
		ThusthecorrectedreadingRcanbeobtainedfromtheobserved reading Rh' as under		
R=Rh'+Cn	n±C	Ct-Cd		
	(iv	CompositeCorrection:		
		Insteadoffindingthecorrectionindividually, it is convenient to find one composite correction.		
The composite correction (C) is the algebraic sum of all the correction. Thus $R = Rh' \pm C$				
		The composite correction is found directly from the readings taken in a comparison cylinder, which has distilled water and the dispersing agent in the same concentration and has the same temperature.		
Computat	ComputationofDandN:			
		TheparticlesizeDiscalculatedfromthefollowingformula		
D=10 - F√	e ^H -			
		Tocompute the percentage of the soil finer than this diameter, the mass MD permlof suspensionate ffective depth Heis first computed as under Since the hydrometer readings have been recorded by subtracting 1 from the density (b) readings and multiplying them by 1000, we have		
R=(þ-1)10	00	2 2 2 2 3 (F) (2222gc 2g 2g 2g 2g) 2000; 100 100 100 100 100 100 100 100 100		

(ii)

Temperaturecorrection:

Or,þ=1+R/1000(i)
Where \flat is the density reading actually marked on the hydrometer and R is the
hydrometer reading corrected for the composite correction.
Now let us consider 1 ml of soil suspension at a time interval t
at the effective depth He. IfMD is the mass ofsolids in this 1 ml
suspensionthe
T1-oMtalDm/Grassoff m/stexpionits with-be
Henced to the second of the se
Herice ensity of the suspension $=_{M_D}$ G $=$ G $+M$ $=$ $+M$
Equatingequation(i)and(ii)we get
$1 + R/1000 = \frac{M_{-}}{1 PC}$
1-DG $+MD$
$MD = \frac{R}{1000G-1}$
WhereG=specificgravityofsoil solids
Substitutingthesevaluesinequation = D×100
MD/7
WegetN' = $\frac{10000G}{Md/V}$ (1)×100
TakingV=1000mlweget
N'=
Md(G-1)
Where N' = percentage finer with respect to Md ThusforvariousvaluesofR,N'canbe calculated
mass of soil originally taken (before sieving it over 2mm sieve) the
overall percentage finer N is given by
N=N'× ^{M'}
M
Where M' = cumulative mass passing 2 mm sieve
M = total dry mass of soil sample Ifthesoilsampledoesnot containparticles coarserthan 2 mmsize, N andN'willbe equal.
·
CONSISTENCYOFSOIL:
Consistencymeanstherelativeeasewithwhichsoilcanbedeformed.
Consistencydenotesdegreeoffirmnessofthesoilwhichmaybe termed as
_ soft, firm, stiff or hard.
\square Finegrainedsoilmaybemixedwithwatertoformaplasticpaste which can be
moulded into any form by pressure.
Theadditionofwaterreducesthecohesionmakingthesoilstilleasier to mould
Furtheradditionofwaterreducestheuntilthematerialnolonger retains its
shapeunder its own weight, but flows as a liquid.

- Enoughwatermaybeaddeduntilthesoilgrainsaredispersedina suspension.
- Ifwaterisevaporatedfromsuchasoilsuspensionthesoilpassesthrough various stages or states of consistency.
 - Swedish agriculturist Atterberg divided the entire range from liquid tosolid state into four stages:
 - (i) Liquidstate
 - (ii) **Plasticstate**
 - (iii) Semi-

solidstate (iv)

Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimitsk Power Education Hesetsarbitrarylimits He terms of water content

- Thusconsistencylimitsarethewatercontentatwhichthesoilmass passes from one state to the next.
- TheAtterberglimitswhicharemostusefulare:
 - Liquidlimit (i)
 - **Plasticlimit** (ii)
 - (iii) Shrinkagelimit

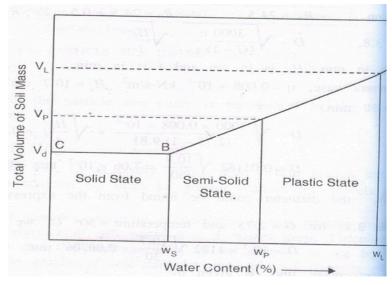


Figure 3.6

Different states of soil

LiquidLimit:

- ☐ Liquid limit is the water content corresponding to the arbitrary limit between liquid and plastic state of consistency of a soil.
- It isdefined as the minimum water content at which the soil is still in the liquid state but has a small shearing strength against flowing which can be measured by standard available means.

Dlacticli		the minimum water content at which a part of soil cut by a groove of standarddimension, willflowtogetherforadistanceof12mmunder an impact of 25 blows in the device.
Piasticiii		impact of 20 blows in the device.
		Plastic limit is the water content corresponding to an arbitrary limit
		between the plastic and the semi-solid state of consistency of a soil.
	_	Itis definedas the minimumwatercontent at whicha soilwill just begin to crumble when rolled into a thread approximately 3 mm in diameter.
Shrinkaç	geli	
		Shrinkage limit is defined as the maximum water content at which a reduction in water content will not cause a decrease in the volume of a soil mass.
		Itis lowest water content at which a soil can still be completely saturated.
Plasticity	- Ind	lex:
		Therangeofconsistencywithinwhichasoilexhibitplasticproperties is called
	_	plastic range and is indicated by plasticity index.
		Plasticityindexisdefinedisdefinedasthenumericaldifference between the
صبد استحما		liquid limit and the plastic limit of a soil Whenplasticilmit annot be determined, the plasticity indexis reported as NP
lp=wl-wp	B	(Non plastic). Whentheplasticlimitisequaltoorgreaterthantheliquidlimitthe plasticity index is reported as zero.
Plasticity	/ :	
		Plasticity is defined as that property of a soil which allows it to be deformed rapidly, without rupture, without elastic rebound and without volume change.
Consiste	ncy	Index:
		The consistency index or the relative consistency is defined as the ratiooftheliquidlimitminusthenaturalwatercontenttotheplasticity index of soil
$I = \frac{wc_{1-w}}{Ip}$		
1	sthe	naturalwatercontentofthe soil
		Ifconsistencyindexofasoilisequaltounity,itisattheplasticlimit.
		SimilarlyasoilwithIcequaltozeroisatitsIiquidlimit.
		IfIcexceedsunitythesoilisinasemi–solidstateandwillbestiff.

A negative consistency index indicates that the soil has natural water contentgreaterthantheliquidlimitandhencebehavesjustlikea liquid.

Liquidityindex:

The liquidity index or water plasticity ratio is the ratio, expressed as a percentage, of the natural water content of a soil minus its plastic limitto its plasticity index:

w w_p |= | Ip

Wherewisthenaturalwatercontentofthe soil.

Example-1

	Duringatestforwatercontentdeterminationonasoilsamplebypycnometer,
_	the following observations were taken

☐ Massofwetsoilsample =1000gm

☐ Massofpycnometerwithsoilandfilledwithwater =2000gm

☐ Massofpycnometerfilledwithwateronly=1480gm

☐ Specific gravity of solids =2.67

Determine the water content.

Solution:

Weknowthatw=[($\frac{M2-M1}{M3-M4}$ G/ $\frac{1}{G}$)-1]×100

=
$$\left[\frac{\frac{1000}{(2000-1480)} \times \frac{2.67-1}{(2000-1480)} -1\right] \times 100$$

=20.28%

Hencewatercontentofthesampleis20.28%.

Example2:

The massof an empty gas jar was 0.498 Kg.When completely filled with water itsmass was 1.528 Kg. An oven dried sample of soil mass 0.198 Kg was placed in the jar and water was added to fill the jar and its mass was found to be1.653 Kg.Determinethe specific gravity of particle.

(Ans)

Solution: weknow that

$$G = \overline{M_{1'}-M_{1(M2-1)}}$$

$$= \frac{0.198}{0.198-(1.653-1.528)}$$

=2.71

Hencespecificgravityofthesampleis

2.71.

Example3:

Asoilsampleconsistingofparticlesofsizerangingfrom0.5mmto0.01mm,isput on the surface of still water tank 5 metres deep. Calculate the time of settlement coarsestandthefinestparticleofthesample,tothebottomofthetank.Assume average specific

gravity of soil particles as 2.66 and viscosity of water as 0.01 poise.

Solution:

$$v = \frac{\frac{D2 \text{ yw (G-1)}}{18 \times 106 \text{ µ}}}{18 \times 106 \text{ µ}}$$

$$= \frac{\frac{D2(G-1)}{1.835 \times 106 \times \text{µ}}}{1.835 \times 106 \times \text{µ}}$$

HereG=2.66andц=0.01×10-4=10-6KN-s/m2

$$V = \frac{D2 \times 2.66-1}{1.835 \ 106(10-6)}$$

=0.905D2

Where v is in m/sec and D is in mm

ForcoarsestparticleD = 0.5mm v=

0.905(0.5)2 = 0.2263 m/sec

t = h/v = 5/0.2263 = 22.1 secondsfor

the finest particle, D = 0.01

mmv=0.905(0.01)2=9.05×10-5m/sec

 $t = 9.05 \times 10^{-5} = 55249 \text{sec} = 115 \text{ ours} = 20 \text{ min} = 49 \text{ seconds}.$

Example4:

50gramsofovendriedsoilsampleistakenforsedimentationanalysis. The hydrometerreadingina 100 mlsoils uspension 30 minutes after the commencement of sedimentation testis 24.5. The effective depth for Rh=25, found from the calibration curve is 10.7 cm. The meniscus correction is found to be +0.5 and the composite correction as – 2.50 at the test temperature of 30°C. Taking the specific gravity of particles as 2.75 and viscosity of water as 0.008 poise, calculate the smallest particle size which would have settled during this interval of 30 minutes and the percentage of particles finer than this size.

Solutio

n:

R=24.5-2.5=22

Rh'=
$$24000 \text{ He}_{-}$$

D= $\sqrt{\frac{1}{(G-1)\gamma w}}$

Where D is in mm, He is in cm and t is in minute.

Here $\mu = 0.008 \times 10-4 \text{ KN-s/m}$ 2

He=10.7cm

G = 2.75 and yw = 9.81

KN/m3t = 30 min.

$$D = \sqrt{\frac{\frac{3000 \times 0.008 \times 10 - 4}{\times \sqrt{10.7}}}{(2.75 - 1)9.81}} \frac{10.7}{30}$$

=7.06×10-3mm

=0.00706mm

Thepercentagefinerisgiven by

$$N' = \frac{100 \text{GRM}}{100 \text{GrM}} \text{d}(G - G)$$

WhereMd=massofdrysoil=50gm
N'=
$$\frac{100 \times 2.75}{50(2.75-1)}$$
 ×22
=69.1%.

(Ans)

Example5: A soil has a liquid limit of 25 % and plastic limit is 15 %. Determine the plasticityindex.

If the water content of the soil in its natural condition in the field is 20 liquidity index and relative consistency.

Solution:

Liquidityindex=II=
$$^{\frac{W-W}{p}}$$
 × 100

$$= \frac{0.2-0.15}{0.10} \times 100 = 50\%$$
Relative consistency = IC = $\frac{10.25-0.2}{0.10} \times 100 = 50\%$
(Ans)

CHAPTER-4 CLASSIFICATIONOF SOIL

Purposeofsoilclassification:

The purpose of soil classification is to arrange varioustypes of soil into specific groups based on physical properties and engineering behavior of the soils with the objective of finding the suitability of soils for different engineering application , such as in the construction of earth dams , highway , and foundations of building , etc.

For different areas of applications and withthe need for simplicity and acceptable terminology, several soil classification system s have been developed over the year s, three of which are listed below.

- 1. Highwayresearch boardclassificationsystem
- 2. Unifiedsoilclassificationsystem
- 3. Indianstandardsoilclassification.

HighwayResearch Board(HRB)classificationSystem:

Group A-1, is divided into two sub groups A-1 and A-1 and group A-2 into four sub groups, A-2-4 , A-2-5 , A-2-6 and A-2-7. A characteristic group indexisused to describe the performance of a soil as sub gradematerial.

Groundindexis notusedto place a soilin aparticular group; it is

actually meansofratingthevalueofsoilasasubgradematerialwithinitsowngroup. Thehi gher the value of the group index, the proper is the quality of the material.

Thegroupindexofasoildepends upon.

- (i) Amountofmaterialpassingthe75-micronsieve,
- (ii) Liquid limit
- (iii) Plasticlimit

Groupindexisgivenbythefollowing equation:

Group

index=0.2a+0.005ac+0.01bd

Where

a=that portion of percentage passing 75 micron sieve greater than 35 and not exceeding 75 expressed as whole number(0 to 40)

b=thatportionpercentagepassing75micronsievegreatert han15and not exceeding55 expressed as whole number(0 to 40)

c=thatportionofthenumericalliquidlimitgreaterthan40and not exceeded 60 expressed as a positive whole number (0 to 20)

d=that portion of the numerical plasticity index greater than 10 and not exceeding 30 expressed as a positive whole number (0 to 20).

To classify a given soil, sieve analysis data, liquid limit and plasticity index are obtained and we proceed from left to right in the Table 4.1 and first by Process of elimination find the groupfromintowhichthetestdatawillfit. This gives the correct Classification. The eplasticity index of A-7-5 subgroup is equal to or less than liquid limit minus 30. The plasticity index of A-7-6 subgroup is greater than liquid limit minus 30.

Note: The PRA system was introduced in 1928 and revised in 1945 as HRB system. It is known as AASHTO system since 1978 after adoption by American Association of State Highway and Transportation Officials.

Unifiedsoilclassification System

TheUnifiedsoilclassificationsystemisbasedontheAirfieldClassificationsyste mthatwas developed by A Casagrande .the system basedon both grain size and plasticity characteristic of soil. The unified Soil classification (USC)system was adopted jointly by the CorpsofEngineers, U.S. army and U.S. Bureau of Reclamationduring 1950s.

- 1.Coarse-grained soils if more than 50% by Weighty is retained on No. 200 ASTM sieve.
 - 2. Fine-grainsoil-ifmorethan50%byweightpassesthroughNo.200ASTM sieve
- 3. Organicsoils.

The soil component are assigned group symbols as indicated

below: Coarse –grained soils: Gravel:G Sand:S

Finegrained soils:

Silt:M Clay's Organicsoil's

Table4.3UnifiedSoilClassification System

MajorDivisio		Group Symbols	
Gravels 50% or more of coarse e Grai n Soils mor e fraction retained on No.4 sieves Sandmo rethan 50% of cross fraction passes No.4sie ve Soils 50% or more passes No.4sie ve	Cleargrav els - 200fractio n <5% Gravel with fine- 200>5% fraction Clean sand s-200<55 fraction Sandwith fines- 200>12% fraction	GW Wett graded GP GM GC SW SP SM	Typic al name s
*		SC	
Fine- grained			

soils 50% or morepass es No.200 sieve. Table4.3givesthedetailsofUnifiedsoilClassificationsystem.Theoriginalc asagrande plasticity chart used for classifing fine graindsoilis givenin Fig 4.3

Theysymbol Mfor sily in drivedfrom the swedishword 'mo'for silt. Example 4.3. classify the soil with composition indicated in 4.2 using US Csystem.

Solution:Sincemorethan50%ofsoilpassesthrough0.074mmsievethesoil isfine grained.

Plasticityindex=(50-40)%=10%

Fromfig4.3

ForwL=40%ANDIp=10%thesoilcanbeclassifiedasMLOR OL

INDIANSTANDARDSOILCLASSIFICATIONSYSTEM

Indian standard soilclassification system (IS 1498-1970 classification and identification of soil for general engineering purpose) is esssentially based on unified soil classification system and the salient features and given in the following discussion.

Inthesystemsoilsarebroadlydividedinto3 division

- 1.coarse-grained soil–ifmorethan 50% bymassis retainon 75 micron IS sieve.
- 2. Finegrainedsoil-

ifmorethan50%bymasspassesthrough75micronIS sieve.

3. Highly organicsoils and other miscelliouns soil material.

Thesoilcontentlarger

%offibrousorganicmattersuchaspeatandparticlesofdecompose vegetation.Inadditionshortensoilcontainingshells,concretionscind ersand other non soil material insufficient quantities are also

givisited in this

CoarsegrainedsoilsaregroupedasgravelsandsandswithgroupsymbolsGand S

Gravels(G)ifmorethan50%bymassofthecoarsegrainedfractionpas sed through 4.75 mm IS sieve .

Dependingonthegradationgravels(G)andsands(S)arefurtherdescr ibedusing group symbols are indicated below.

GW-WellgradedgravelforwhichCu>4andCcliesbetween 1&3

GP- poorly graded gravel which does not meet all graduation requirement

of GW

SW-

WellgradedsandforwhichCu>6andCcliesbetween1& 3 GM-silty gravel if lp > 4 for fine- grained fraction. GC-Clayey gravel if Ip < 7 for fine-grained fraction. SM-Silty sand if Ip<4 for fine grainedfraction.

SC-ClayeysandifIp>7forfine-grainedfraction.

Inthecaseofcoarse-

grainedsoilsmixedwithfinesifIpliesbetween4 and 7 one has to use proper judgment in dealing with this border line case. Generally non-plastic classification is favored in such cases. For examplea

sandwith10%fineswithCu>6,Ccbetween1and3andIp=6 wouldbeclassifiedasSW-SMratherthanSW-SC.

Fine-

grainedsoilsaregroupedunderfollowingthreesubdivisionswith respectivegroupsymbols:

Inorganic silts and very fine sands(M) Inorganic clays(C)

Organicsilts, Organicclays and Organic matter (O)

Depending on liquid limit which is considered a good index of compressibility

finegrainedsoilsaredescribedaspossessing(i)lowcompressibili ty(L)when liquidlimitislessthan35percent.

- (ii) intermediate or medium compressibility (I) when liquid limit lies between 35 percent and 50 percent
- (iii) highcompressibility(H)whenliquidlimitisgreaterthan50 percent.

The plasticity chart originally devised by A.

Casagrande and slightly modified by IS is used to classify finegrained soils in the laboratory. The A-line having the equation:

Ip=0.73(Wl-20)

And the two vertical lines at wl=35and wl=50 divide the chart into six regions with group symbols marked as shown in Fig.4.4 if the plotted position lies below A-line, the soil has to be checked for organic odour by slight heating.

Ifnoorganicodourissmeltthanonlyitshouldbeclassifiedasinorga နေရှေမှုရှ်စုံရပbt,thesoilshouldbeoven-

driedanditsliquidlimit determined

again. In the case of organic soils there will be large reduction in liquid limit on drying (reduction generally>25%).

Soil	Soil		Particlesizerangeanddescription
	compone	Symb	
Coarse- grained	Boulde	r none	Roundtoangular,bulkyhard,rock particle, average diametermore than 300mm.
Componen	t Cobbl e	None	Roundtoangular,bulkyhard,rockpartic le averagediametersmallerthan 300
	Gravel	G	mmbut retainedon80mmsieve. Roundedtoangular,bulkyhard, rock particle,passing80mmsievebut retained on 4.75mmsieve. Coarse:80mmto20mmsieve
	Sand	S	Fine: 20 mm to 4.75 mm sieve Roundedtoangularbulkyhard, rocky particle, passing 4.75 mmsieve retained on 75 micronsieve Coarse: 4.75 mmto 2.0 mmsie ve Medium: 2.0 mmto 425 micronsi eve Fine: 425 micron to 75 micron sieve
	silt	M	Particlessmallerthan75-micron sieve indentifiedbybehavior;thatisslightly plasticornon-

			plasticregardlessofmoisture and exhibits little or no strength whe	
Fine— grained Component			dried	
S	Clay	С	Particlessmallerthan75-micron sidentifiedbybehavior,thanis,itcare to exhibit plastic properties wit certain range of moisture and exhibits considerable strengthwhenairdried	nmad

CHAPTER-5 PERMEABILITYAND SEEPAGE

Conceptof Permeability:-

- Thepropertyofsoilwhichpermitsflowofwater(orotheranyliquid) throughitiscalledthepermeabilityinotherworld,thepermeabilityinth e case with which water can flow through it.
- > Permeabilityisveryimportantengineeringpropertyof soil.
- The knowledge of permeability is essential in a number of soil engineering problemssuchas:SettlementofBuildings,Yieldofwells,Seepagethrough and below the earth surface.
- Permeabilitycontrolsthehydraulicstabilityofsoil masses.
- The permeability of soils is also required in the design of filters
- required to prevent piping in hydraulic structure.

Darcy's Law:-

The flow of free water through soil is governed by Darcy's law. In 1856, Darcy experimentally that for laminar flow in a homogeneous soil, the velocity of flow (v) is given by

v=ki <u>Equa</u>**‡**ionno -1

Where, k= coefficient of permeability, i= hydraulic gradient and v = velocity of flow in laminar flow in homogeneous soil

The above equation is known as Darcy's law, which is one of the corner stones of soil engineering. The discharge 'q' is obtained by multiplying the velocity offlow(v)bythetotalcross-sectionalarea(A)normaltothedirectionofflow

Note: - 1) The velocity of flow is also known as discharge velocity or superficial velocity.

2) Thearea Aintheabove equation includes both the solids and the voids.

Co-efficient of Permeability:-

The coefficient of permeability can be defined using the equation 1. If the hydraulic gradient is unity, the coefficient of permeability is equal to the velocity of flow

Or,

- The coefficient of permeability is defined as the velocity of flow which would occurunderunithydraulicgradient. The coefficient of permeability is equal to the velocity of flow.
- Thecoefficientpermeabilityhasthedimensionsofvelocity [L/T].
- Thecoefficientofpermeabilitymeasuredinmm/sec,cm/sec,m/sec,m/day or other velocity units.
 - The coefficient of permeability depends upon the particle size and upon
- > many factors.
 - According to USBR, the soil having co-efficient permeability

greater than 10-3mm/secareclassifiedasperviousandthosewithavaluelessthan10-5to 10-3mm/sec are designated as semi-pervious.

Factorsaffecting Permeability of soils:-

The following factors affect the permeability of soils.

- (1) ParticleSize.
- (2) Structureofsoilmass.
- (3) Shapeofparticles.
- (4) Voidratio.
- (5) Properties of water.
- (6) Degreeofsaturation.
- (7) Adsorbedwater.
- (8) Impurities inwater.
- (1) Particle Size: -

Co-efficient of permeability of soil is

proportional to the square of particle size (D). The permeability of coarse grained soils is very large as compared to that of fine-grained soils. The permeability of coarse sand may be more than one million times as much that of clay.

(2) Structure of soil mass: - The coefficient C takes into account the shape offlow passage. The size of flow passage depends upon the structural arrangement. For same void ratio, the permeability is more in the case of flocculated structure as compared to that in the disperses structure.

Stratified soil deposits have greater permeability parallel to the plane of stratification than that perpendicular to this plane. Permeability of soil deposit also depends upon shrinkage cracks, joints, fissures and shear zones. Loess deposits have greater permeability in the vertical direction than in the horizontal direction.

The permeability of natural soil deposit should be determined in undisturbed

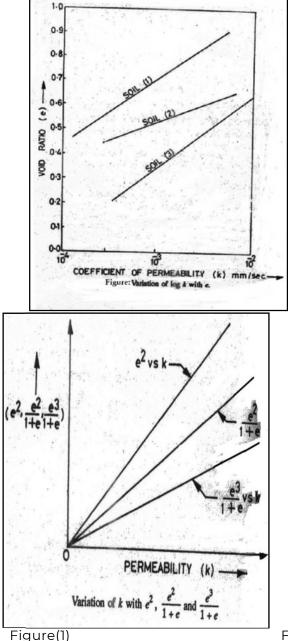
condition. The disturbance caused during sampling may destroy the original structure and affect the permeability. The effect of disturbance is more

ronounces in case of fine-grained soils than in the case of coarse- rained soils.	
(3) Shape of Particles: - The permeability of a soil depends upon	
he shape of	
articles. Angular particles have greater specific surface are as compared with	
he	

roundedparticles. For the same void ratio, the soils with an gular particles are less permeablethanthos withroundedparticles, as the permeability is inversely

 $proportional to the specific surface. However, in a natural deposit, the void ratio {\tt restaural} and {\tt restaural} an$ for asoil with angular particles may begreater than that for rounded particles, and thesoil with angular particles may be actually more permeable.

(4) Void Ratio: - For a given soil, the greater the void ratio, the higher is the value of the coefficient of permeability. Based on the other concepts, it has been established that the permeability ofsoil varies ase2ore2/ (1+e)(figure-2). Whatever may be the exact relationship; alloils have e versus log k plot as a straight line (figure-1).



Figure(2)

Ifthepermeabilityofasoilatavoidratioof0.85isknown,itsvalueat another void ratio of 'e' can be determined using the following equation given by Casagrande:

k_{=1.4k0.85e2}

Where k0.85 = permeability at void ration of 0.85, k = permeability at a void ratio of 'e'.

- _____(5) Properties of Water: The co-efficient of permeability is directly proportional to the unit weight of water (γ w) and is inversely proportional to its viscosity (μ). The coefficient of permeability increases with an increase thetemperature due to reduction in the viscosity.
- (6) Degree of Saturation:- if the soil is not fully saturated, it contains air pocket formed due to entrapped airor due to air liberated from percolating water. Whatever may be the cause of presence of air in soils, the permeability is reduced due to presence of sir which causes blockage of passage. Consequently, the permeability of partially saturated soil is considerably smaller than that of fully saturated soil. In fact Darcy's Law not strictly applicable to such soils.

(7) Adsorbed Water: - The fine grained soils have a layer of adsorbed water stronglyattachedtotheirsurface. This adsorbed water layer is not free to move undergravity. It causes an obstruction to flow of water in the pores and hence reduces the permeability of soils.

Itisdifficulttoestimatethevoidoccupiedbytheadsorbedwater.According to one estimate, the void ration occupied by adsorbed water is about 0.10. Theeffectivevoidratio availablefor flowof water is thus about (e-0.1) and not 'e'. In some cases, at very low hydraulic gradient, the coefficient of permeability of fine- grained soils becomes negligible small due to presence of adsorbed water.

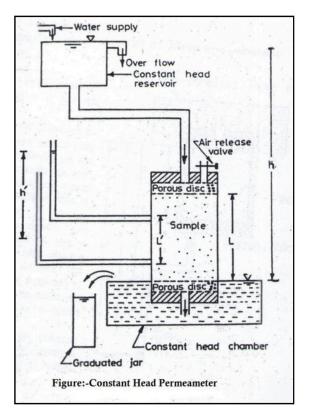
Impurites in Water: - Any foreign matter in water has a tendency to plugthe flow passage and reduce the effective voids and hence the permeability of soils.

. 1- ConstantHeadPermeability Test:-

The coefficient of permeability of a relatively more permeables oil can be determined in a laboratory by the constant – head permeability test.

- 1. Thetestisconductedinaninstrumentknownasconstant-headPermeameter.
- 2.It consists of a metallic mould, 100 mm internal diameter, 127.3 mm effective height and 1000 ml capcity according to IS: 2720 (Part XVII).
- 3.The mouldisprovided with adetachable extension collar, 100 mm diameter and 60 mm high, required during compaction of soil.
- 4. The mould is provided with drainage base plate with recess for porous stone.
- 5. The mould is fitted with a drainage cap having an inlet valve and an airrele as evalve.

 $6. \ The drainage base and cap have fittings for clamping to the mould.$



- 1. The above figures how saschematics ketch.
- 2. The soils ample is placed in side the mould between two porous discs.
- 3. The porous discs should be at least tentimes more per meable than the soil.
- 4. The porous discs should be deaired before the seare placed in the mould.
- 5. Thewatertubesshouldalsobedeaired.
- 6. The sample can also be prepared in the permeameter by pour ing the soilinto it and tamping it to obtain the required density.
- 7. Thebaseisprovidedwithadummyplate,12mmthickand108mmindiam eter, which is used whenthesampleis compacted in the mould.
 - 8. It is essential that the sample is fully saturated. This is done by one of the following three methods:
 - i. By pouring the soil in the permeamter filled with water
 - ii. and thus depositing the soil under water.

 Byallowingwatertoflowfromthebasetothetopafterthesoil has been placed in the mould. This is done by attaching theconstant-head reservoir to the drainage base. The upward flow is maintained for sufficient time till all the air has been expelled out.
 - iii. Byapplying a vacuum pressure of about 700mm of mercurythrough the drainage cap for about 1.5 minutes bifter closing drainagevalve. Then the soil is saturated by allowing deaired water to enter from drainage base. The air-release valve is keptopen during saturation process.
- 9.After the soil sample has been saturated, the constant-head reservoir is connected to the drainage cap.
- 10. Waterisallowedtoflowoutfrom the drainage base for sometime tilla steady-state is established.

- 11. The water level in the constant-head chamber in which the mould is placed iskept constant.
- 12. The chamber is filled to the brimat the start of the experiment.
- 13.Thewater

whichentersthechamberafterflowingthroughthesamplespills over the chamber and collected in a graduated jar for convenient period.

14.Theheadcausingflow(h)isequaltothedifferenceinwaterlevelsbetwee n the constant-head reservoir and the constant-head chamber.15.Ifthecross-sectionalareaofthespecimenisA,thedischargeisgivenby

or, k=(ql)/(Ah) where,L=Lengthofspecimen,h=headcausingflow.

The discharge qualtothevolume of water collected divided by time. The finer particles of soil specimen have a tendency to migrate towards the end faces when water flows through it. This results in the formation of a filter skin at the ends. The coefficient of permeability of these end portions is quite different from that of middle portion. For more accurate results, it would be preferable to measure the loss of head h overalength L in the middle to determine the hydraulic gradient (i). Thus i = h'/L'.

The temperature of permeating water should be preferably somewhat higher thanthatofthesoilsample. This will prevent release of airduring the test. It also helps in removing the entrapped air in the pores of soil. As the water cools, it has tendency to absorb air.

To reduce the chances of formation of large voids at the points where the particlesofsoiltouchthepermeameterwalls, the diameter of the permeameter is kept at least 15 to 20 times the particles size.

To increase the rate of flow for the soils of low permeability, a gas under pressure is applied to the surface of water in the constant-head reservoir. The total head causing flow in that case increase to (h + p/yw), where p is pressure applied.

The bulk density of the soil in the mould may be determined from the mass of soilinthemouldanditsvolume. The bulk density should be equal to that in the field. The undisturbed sample can also be used instead of the compacted fample.

accurateresults, the specimens hould have the same structure as innatural conditions.

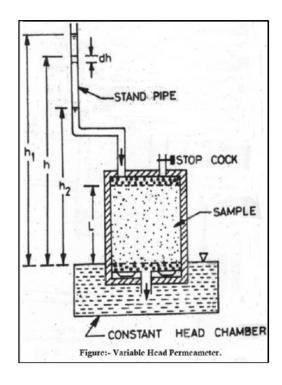
The constant head permeability test is suitable for clean sand and gravel with k > 10-2 mm/sec.

5.3.2-FallingHead / VariableHeadPermeability Test: -

For relatively less permeability soils the quantity of water collected in the graduated jar of the constant-head permeability test is very small and cannot be accurately. For such soils, the variable-head permeability test is used in the constant-head permeability test.

1)A vertical, graduated stand pipe of known diameter is fitted to the top of permeameter.

- 2) The sample is placed between two porous discs.
- 3)The whole assembly is placed in a constant head chamber filled with water to brim at the start of the test. (See the below figure shows a schematic sketch).



- 4) Teeporousdiscsandwatertubesbedeairedbeforethesampleisplaced.If in-situ, undisturbed sample is available, the same can be used; otherwise the soil is taken in the mould and compacted to required density.
- 5)The valve at the drainage base (not shown in figure) is closed and vacuum pressureis applied slowlythroughthedrainagecapto remove air from the soil.
- 6)The vacuum pressure is increased to 700 mm of mercury and maintained for about 15 minutes.
- 7)The sample is saturated by allowing deaired water to flow upward from the drainage base when under vacuum.
- 8) Whenthesoilissaturated, both the top and bottom outlets are closed.
- 9) The standpipe is filled withwater to require dheight.
- 10) The test is stated by allowing the water in the standpipe to flot through the sample to constant head chamber from which it over flows and spills out.
- 11) Asthewaterflowsthroughthesoil, the waterlevel in the standpipe falls.
- 12) The time required for the water level to fall from a known initial head (h1) toknown as final head (h2) is determined.
- 13) The head is measured with reference to the level of water in the constanthead chamber.

Letusconsidertheinstantwhentheheadish.Fortheinfinitesimal small time dt, the head falls by dh. Letthedischargethroughthesamplebeq.

Fromcontinuityofflow, adh = -a dt

Where 'a' is cross-sectional area of standpipe.

Integrating,
$$\frac{AKt2}{-f} dt = -f + \frac{h2}{h} + \frac{dh}{h}$$

Where,t=(t2-

t1),thetimeintervalduringwhichtheheadreduces from h1 to h2).

Sometime
$$k_{2.30aL}$$
 log10(h1/h2)

The rate of fall of water level in the stand pipe and te arte of flow can be adjusted by changing the area of cross-section of the standpipe. The smaller diameter pipes are required for less pervious soils.

The coefficient of permeability is is reported at 27° C as per IS: 2720 (PartXVII). The void ratio soil is also generally determined. The variable head permeameter is suitable for very fine sand and silt with k= 10-2to 10-5mm/sec. Sometime, the permeability test is conducted

using the consolidometer

instead of the permeameter mould. The fixed-ring consolidometer is used a variable –head permeameter by attaching a stand.

.1-Seepage Pressure: -

As water flows through the soil, it extends a force on the soil. The force ${\sf acts} \qquad \qquad {\sf in}$

the direction of flows. This force is known as drag force or see page force. The pressure induced in the soil is known as see page pressure.

Or

By virtue of the viscous friction exerted on water flowing through soil energy

transferiseffectedbetweenthewaterandsoil. The force corresponding to this energy transfer is called the seepage force or seepage pressure. Thus, seepage pressure is the pressure exerted by water on the soil through which percolates.

5.4.2- ThephenomenonofQuick Sand: -

When flow takes place in an upward direction, the seepage pressure also acts in the upward direction and the effective pressure is reduced. If the seepage pressure becomes equal to the pressure due to

submerged weight of the soil, the effective pressureisreducedtozero,insuchcase, acohesionlesssoillosesallitsshear strength, and the soil particles have a tendency to move up in the direction of flow.Thisphenomenonofliftingofsoilparticlesiscalledquickcondition,boiling condition or quick sand. Thus, during the quick condition,

$$\sigma'=zy'-p_{s=0}$$

or, $ps=z$ γ'
or iz $yw=zy'$
Fromwhich,
 $I=i='_c$ γ γ'_c $w=\frac{G-1}{1+e}$

- The hydraulic gradient at such a critical state is called hydraulic gradient. For loose deposits of sand or sand or silt, if voids ratioe is taken as 0.67 and G as 2.67, the
- critical hydraulic gradient works out to be unity. Itshouldbenotedthatquicksandisnotatypeofsandbuta flow condition occurring within a cohesionless soil when its effective pressure is reduced to zero due to upward flow of water.

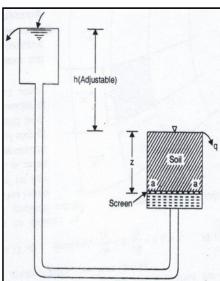


Figure:-QUICK SAND CONDITION

- 1. The figure shows a set-up to demonstrate the phenomenon of quicks and.
- 2. Water flows in an upward direction through a saturated soil sample of thickness 'z' under a hydraulic head 'h'.
- 3. This head can be increased or decreased by moving the supply tank in the upward or downward direction.
- 4.Whenthesoilparticlesareinthestateofcriticalequilibrium,thetotal upward force at the bottom of soil becomes equal to the total weight of all the materials above the surface considered.

Equating the upward and downward forces at the level *a-a*, we have,

$$(h+z)$$
 γ WA=Z γ t A

$$hyw = Z_{VSQt-V} \bar{\nabla} Z^{\gamma'}$$

$$\frac{h}{z} = i'_{c=V} / yw = G-1$$

$$\frac{1+e}{1+e}$$

$$\frac{h}{z} = i'_{c} = \gamma / \gamma W = G - \frac{1}{1 + e}$$

5.5.1- Conceptof Flow -

Net:-

- 1. The graphical method of flown et construction, first given by Forchheim er (1930), is based on trail sketching.
- 2. The hydraulic boundary conditions have a great effect on the general shape of the flow net, and hence must be examined before sketching is started.
- 3. The flow net can be plotted by trial and error by observing the properties of f flownetandbyfollowingpracticalsuggestiongivenbyA.Casagrande.

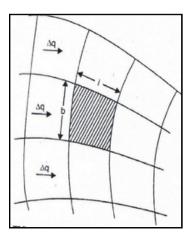


Figure:-PORTIONOFAFLOW NET

5.5.2-PropertiesofFlow - Net: -

- 1. The flow lines and equipotential line meet a tright anglest oone another.
- 2. Thefieldsareapproximatelysquares, so that a circle can be drawn to uchi ng all the four sides of the square.
- 3. The quantity of waterflowing through each flow channel is same, similarly y, the same potential drop occurs between two successive equipotential lines
- 4.Smaller the dimensions of the field, greater will be the hydraulic gradient and velocity through it.
- 5.Ina homogeneous soil, every transition in the shape of the curves issmooth, being either elliptical in shape.

5.5.3- Application of Flow - Net: -

Aflownetcanbeutilizedforthefollowing purposes:-

a) Determinationofseepage.

- b) Determinationofhydrostaticpressure.c) Determinationofseepagepressure.

d) Determinationofexistgradient.

(a) Determinationofseepage:- Figureshowsaportionofflownet. The portion between any two successive flow lines is known as flow channel. The portion enclosed between two successive equipotential lines and successive flow lines is known as field as that shown hatched in the figure

Letb&lbethewidthandlengthofthefield
Δh=headdropthroughthefield
Δq=Dischargepassingthroughtheflowchannel
H=totalhydraulicheadcausingflow=differencebetweenupstr
eam and downstream heads.

b= k H(Nf/

Nd), Where, Nf = Total number of flow

channel in the net

Nd=Totalnumberofpotentialdropsinthecomplete net This is required expression for the discharge passing through flow-net and valid for isotropic soils in which kx = kyk.

(b) Determination of hydrostatic pressure:- The hydrostatic pressure at any point within the soil mass is given by $= u = \gamma w h w$ Where u = hydrostatic pressure, hw = Pizometrichead

The hydrostatic pressure in terms of Pizometrichead hwis calculated the relation -

hw=h-7

Whereh=Hydraulic potential at the point under consideration.
Z=position head of the point above datum, considered positive upwards.

(c) Determination of see page pressure:-

The hydraulic potential h at any point located after n potential drops, each value Δ h is given by

 $h=H-n \Delta h$

theseepagepressureatanypointequalsthehydraulicpotentialorba lanced hydraulicheadmultiplied byunitweightofwater andhenceisgiven by p = h ($H-n\Delta h$),

The pressure acts in the direction of flow.

(d) Determination of exist gradient:-The exit gradient is hydraulic at the downstreamendoftheflow linewherethepercolatingwaterleavesthesoil mass and emerges into the free water at the downstream. The exit gradient

can be calculated from the following expression, in which Δ hrepresents the

potential dropand/the average length of last field in the flown etatexit end:

 $i \in (\Delta h/l)$.

CHAPTER-6 COMPACTIONAND CONSOLIDATION

COMPACTION

Compactionistheapplicationofmechanicalenergytoasoilsoastorearrangeit s particles and reduce the void ratio.

It is applied to improve the properties of an existing soil or in the process of placingfill such as in the construction of embankments, road bases, runways, earth dams, and reinforced earth walls. Compaction is also used to prepare a levelsurface during

construction of buildings. There is usually no change in the water content and in the size of the individual soil particles.

Theobjectivesofcompactionare:

Toincreasesoilshearstrengthandthereforeitsbearingcapacity.
Toreducesubsequentsettlementunderworkingloads.
Toreducesoilpermeabilitymakingitmoredifficultforwatertoflowthrough.

LIGHTANDHEAVYCOMPACTIONTEST

LaboratoryCompaction

The variation in compaction with water content and compactive effort is first determined in the laboratory. There are several tests with standard procedures such as:

 $\hbox{$\blacksquare$ IndianStandardLightCompactionTest(similar to Standard ProctorTest)}\\$

■ IndianStandardHeavyCompactionTest(similartoModifiedProctorTest)

IndianStandardLightCompaction Test

Soiliscompactedintoa1000cm3mouldin3equallayers,eachlayerreceiving25blow s of a 2.6kgrammerdropped from a heightof 310mm above thesoil.Thecompactionis repeated at various moisture contents.

IndianStandardHeavyCompaction Test

It was found that the Light Compaction Test (Standard Test) could not reproduce the densities measured in the field under heavier loading conditions, and this led to the development of the Heavy Compaction Test (Modified Test). The equipment and procedure are essentially the same as that used for the StandardTest except that the soiliscompactedin5layers,eachlayeralsoreceiving25blows.Thesamemouldisals o used. To provide the increased compactive effort, a heavier rammer of 4.9 kg and a greater drop height of 450 mm are used.

OPTIMUM MOISTURE CONTENT OF SOIL, MAXIMUM DRY DENSITY, ZEROAIR VOID LINE

To assess the degree of compaction, it is necessary to use the dry unit weight, which is an indicator of compactness of solid soil particles in a given volume. The laboratory testing is meant to establish the maximum dry density that can be attained for a given soil with a standard amount of compactive effort.

Inthetest, the dryden sity cannot be determined directly, and assuch the bulk density

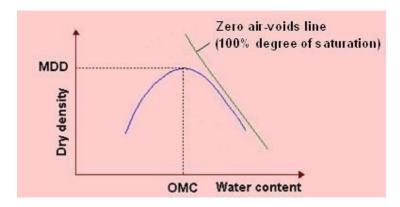
$$\gamma_d = \frac{\gamma_t}{1 + w}$$

and the moisturecontentareobtainedfirsttocalculatethedry density as

$$\gamma_t$$
 , where

= bulk density, and w = water content.

A series of samples of the soil are compacted at different water contents, and a curveis drawn with axesof dry densityandwater content. The resulting plot usually has a distinct peak as shownch inverted "V" curves are obtained for**cohesivesoils** (or soils with fines), and are known as compaction curves.



Drydensitycanberelatedtowatercontentanddegreeofsaturation(S) as

$$\gamma_d = \frac{G_{S} \cdot \gamma_W}{1 + e} = \frac{G_{S} \cdot \gamma_W}{1 + \frac{w \cdot G_{S}}{S}}$$

Thus, it can be visualized that an increase of dryden sity means a decrease of voids ration and a more compact soil.

Similarly, drydensity can be related to percentage air voids (n a) as

$$\gamma_d = \frac{(1 - n_a)G_s.\gamma_w}{1 + wG_s}$$

Therelationbetweenmoisturecontentanddryunitweightforasaturatedsoilisthe **z ero air-voids line.** It is not feasible to expel air completelybycompaction, no matter how much compactive effort is used and in whatever manner.

EffectofIncreasingWaterContent

Aswaterisaddedtoasoilatlowmoisturecontents, it becomes easier for the particlest o move past one another during the application of compacting force. The particles come closer, the voids are reduced and this causes the dry density to increase. As the water content increases, the soil particles develop larger water films around them.

This increase in drydensitycontinues till a stage is reached where water starts

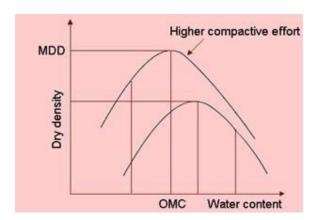
occupyingthespacethatcouldhavebeenoccupiedbythesoilgrains. Thusthewater at this stage hinders the closer packing of grains and reduces the dryunit

weight.
The**maximumdrydensity(MDD)**occursatan optimumwatercontent(OMC),and their values can be obtained from the plot.

EffectofIncreasingCompactiveEffort

The effect of increasing compactive effort is shown. Different curves are obtained for

differentcompactiveefforts. Agreater compactive effort reduces the optimum mois ture content and increases the maximum dry density.



An increase in compactive effort produces a verylarge increase in drydensity for soil

whenitiscompacted atwater contents drier than the optimum moisture content. Its hould be noted that for moisture contents greater than the optimum, the use of heavier compaction effort will have only a small effect on increasing dryunit weights.

It can be seen that the compaction curve is not a unique so il characteristic. It depends on

the compaction effort. For this reason, it is important to specify the compaction procedure (light or heavy) when giving values of MDD and OMC.

FactorsAffecting Compaction

The factors that influence the achieved degree of compaction in the laboratory are:

Plasticityofthesoil

Watercontent

Compactiveeffort

FIELDCOMPACTIONMETHODSANDTHEIR SUITABILITY

CompactionEquipment

Most of the compaction in the field is done with rollers. The four most common types of rollers are

- 1. Smooth-wheelrollers(orsmooth-drumrollers)
- 2. Pneumaticrubber-tiredrollers
- 3. Sheepsfootrollers
- 4. Vibratoryrollers

Smooth-wheelrollersaresuitableforproofrollingsubgradesand for

finishingoperationoffillswithsandyandclayeysoils. Theserollersprovide 100% covera ge under the wheels, with ground contact pressures as high as 310 to 380 kN/m2 (45 to 55 lb/in2). They are not suitable for producing high unit weights of compaction when used on thicker layers.

Pneumaticrubber-tiredrollersarebetterinmanyrespectsthan the smooth-wheel rollers. The former are heavily loaded with several rows of tires.

These tires arecloselyspaced—fourtosixinarow.Thecontactpressureunderthetirescanrangefrom 600to700kN/m2(85to100lb/in2),andtheyproduce about 70 to 80%coverage. Pneumatic rollerscanbeusedforsandyandclayeysoilcompaction.Compactionisachievedbya combination of pressure and kneading action.

Sheepsfootrollersaredrumswithalargenumberofprojections. The area of each projection may range from 25 to 85 cm2(_ 4 to 13 in2). These rollers are most effective

 $in compacting clayeyso ils. The contact pressure under the projections can range from {\bf 1400}$

to7000kN/m2(200to1000lb/in2).Duringcompactioninthefield,theinitialpassescom pact the lower portion of a lift. Compaction at the top and middle of a lift is done at a later stage.

Vibratoryrollersareextremelyefficientincompactinggranularsoils. Vibrators can beattachedtosmooth-wheel, pneumaticrubber-

tired, or sheeps footrollers to provide vibratory effects to the soil.

 $Hand held vibrating plates can be used for effective compaction of granular so ils\ over a limited area. Vibrating plates are also gang-$

mountedonmachines. These plates can be used in less restricted areas..

CONSOLIDATION:

AccordingtoTerzaghi(1943), "adecreaseofwatercontentofasaturatedsoil without replacement of the water by air is called a process of consolidation." When saturated clayey soils-which have a low coefficient of permeability-are subjected to a compressivestressdue to afoundation loading, theorewaterpressurewill immediately increase; however, due to the low permeability of the soil, there will be a time lag between the application of load and the extrusion of the pore water and, thus, the settlement.

DIFFERENCEBETWEENCOMPACTIONAND CONSOLIDATION:

Consolidation and compaction are totally different process. Though both process results a reduction in volume, it is important to know the difference between them. These are:



a.Compaction reduces volume of soil by rapid mechanical methods like tamping, rolling and vibration; whereas consolidation process reduces volume gradually by static, sustained loading.

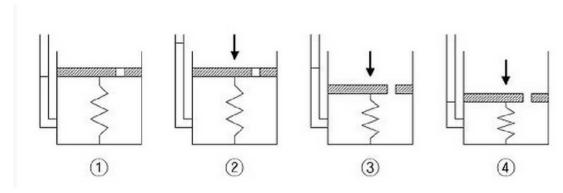
b.Compaction decreases volume by expelling air from partially saturated or dry soil; whereas consolidation process reduces volume by squeezing out water from saturated soil. In compaction process water content is not altered.



c.Compactionisahumangeneratedpressingmethodtoproducehighunitweight of soil. Thus increasing other properties to have better founding soil. In contrast, consolidation is natural process where volume of saturated soil mass reduced by static loads from the weight of building or other structures that is transferred to soil through a foundation system.

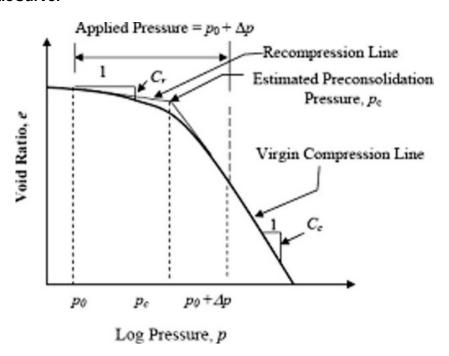
SPRINGANALOGYMETHOD

Theprocessofconsolidationisoftenexplainedwithanidealizedsystemcomposed of a spring, a container with a hole in its cover, and water. In this system, the spring represents the compressibility or the structure of the soil itself, and the water which fills the container represents the pore water in the soil.



- 1.The container is completely filled with water, and the hole is closed. (Fully saturated soil)
- 2.A load is applied onto the cover, while the hole is still unopened. At this stage, only the water resists the applied load. (Development of excess pore water pressure)
- 3. Assoonastheholeisopened, waterstartstodrain outthrough the hole and the spring shortens. (Drainage of excess pore water pressure)
- 4.Aftersometime,thedrainageofwaternolongeroccurs.Now,thespring alone resists the applied load. (Full dissipation of excess pore water pressure. End of consolidation)

Pressure-VoidRatioCurve:-



soil,

Normallyconsolidated,UnderconsolidatedandOverconsolidated

Consolidation is a process by which soils decrease in volume. According to Karl

von

Terzaghi "consolidation is any process which involves a decrease in water saturatedsoilwithoutreplacementofwaterbyair." Ingeneralitistheprocessin which

reduction

in volume takes place by expulsion of water under long term static loads. It occurs stress is applied to a soil that causes the soil particles to pack togethermoretightly,thereforereducingitsbulkvolume.Whenthisoccursina soil

that is saturated with water, water will be squeezed out of the soil. The magnitude of consolidation can be predicted by many different methods. In the Classical Method, developed by Terzaghi, soils are tested with an <u>oedometer</u> test to determine their compression index. This can be used to predict the amount of consolidation.

Whenstressisremovedfromaconsolidatedsoil,thesoilwillrebound,regaining someofthevolumeit hadlostintheconsolidationprocess.Ifthestressis reapplied, the soil will consolidate again along a recompression curve, defined by the becompressionindex. Thesoilwhichhaditsloadremovedisconsidered to overconsolidated. This is the case for soils which have previously had glaciers on them. The highest stress that it has been subjected to is termed the preconsolidation stress. The overconsolidation ratio or OCR is defined as the highest stress experienced divided by the current stress. A soil which is currently experiencing its highest stress is said to be normally consolidated and to have an OCR of one. A soil could be considered underconsolidated immediately after a new load is applied but before the excess pore water pressure has had time to dissipate.

AssumptionofTerzaghi'stheoryofone-dimensional consolidation

- 1. Thesoilishomogenous(uniformincompositionthroughout).
- 2. Thesoilisfullysaturated(zeroairvoidsduetowatercontentbeingsohigh).
- 3. The solid particles and water are incompressible.
- Compressionandflowareone-dimensional(verticalaxisbeingtheoneof interest).
- 5. Strainsinthesoilarerelativelysmall.
- 6. Darcy'sLawisvalidforallhydraulicgradients.
- of premeability frament the coefficient of volume compressibility remain constant throughout the process.
- 8. There is a unique relationship, independent of time, between the void ratio and effective stress

CoefficientofConsolidation:

The Coefficient of consolidation at each pressures increment is calculated by using the following equations:

i. Cv=0.197d2/t50(Logfittingmethod)

In the log fitting method, a plot is made between dial readings and logarithmic of time, the time corresponding to 50% consolidation is determined

ii. Cv=0.848d2/t90(Squarefittingmethod)

In the square root fitting method, a plot is made between dial readings and square root of time and the time corresponding to 90% consolidation is determined.

TimeFactor:-

The magnitude of consolidation settlement is often calculated using Terzaghi's expression for average degree of consolidation (U) with respect to time. Developed during a time of limited computing capabilities. Terzaghi's series solution to the onedimensional consolidation equation was generalized using a dimensionless time factor (T), where a single U-T curve is used to describe the consolidation behavior of both singly and doubly drained strata. As a result, any comparisons between one- and twoway drainage are indirect and confined to discrete values of time. By introducing a modifiedtimefactor T * intermsoflayerthickness(D)insteadofthemaximum drainage path length (Hdr), it is now possible to observe the effect of drainageconditions over a continuous range of time for a variety of asymmetric initial excesspore pressure distributions. Although two separate U-T plots are required (for singlyand doubly drained cases), the time factor at specific times remains the same for both cases, enabling a direct visual comparison. The importance of a revised time factor is evident when observing the endpoint of consolidation, which occurs as U approaches 100%. This occurs at $T \star \cong 0.5$ for two-way drainage and at $T \star \cong 2$ for one-way drainage, an observation notpossibleusingthe traditionalexpression for time factor.

Estimationofconsolidationsettlements

Prediction of groundsettlements havealways beena big challengefor theengineers that are responsible for the design of subway tunnel projects. Since groundsettlement is a crucial concept directly affecting the successfulness of a project, it must be taken seriously and should be accurately estimated.

Categories:

- 1. <u>Immediate settlement</u> elastic deformation of dry soil and moist and saturated soils without change to moisture content
 - a due to high permeability, pore pressure in clays support the entire added load and no immediate settlement occurs
 - generally, due to the construction process, immediate settlement is not important
- 2. <u>Primary consolidation settlement</u> volume change in saturated cohesive soils because of the expulsion of water from void spaces
 - high permeability of sandy, cohesionless soils result in near immediate drainage due to the increase in pore water pressure and no primary consolidation settlement occur

DIFFERENCEBETWEENPRIMARYANDSECONDARY COSOLIDATION

Primaryconsolidation

Thismethodassumesconsolidationoccursinonlyone-dimension.Labratorydaotais usedtoconstructaplotofstrainorvoidratioversuseffectivestrsswherethe effectivestressaxisis ona logarithmicscale.Theplot'sslopeisthecompression indexorrecompressionindex.Theequationforconsolidationsettlementof a normallyconsolidatedsoilcanthenbedeterminedto be:

$$\mathbf{E} = \frac{\mathbf{C}_{\mathbf{c}}}{\mathbf{I} + \mathbf{E}_{\mathbf{c}}} \mathbf{H} \mathbf{E}_{\mathbf{c}}$$
where

δcisthesettlemetdunetoconsolidation.

Ccisthecompressionindex. e0

is the initial void ratio.

Histheheightofthesoil.

σzfisthefinalverticalstress.

σz0istheinitialverticalstress.

CccanbereplacedbyC(therercompressionindex)foruseinoverconsolidatedsoils wherethefinaleffectivestressislessthanthepreconsolidationstress. Whenthefinal effectivestressisgreaterthanthepreconsolidationstress,thetwoequationsmust be usedincombinationt omodelboththerecompressionportionadthevirgin compression portion of te consolidatiohn processes, as follows,

$$\mathbf{E}_{\mathbf{z}} = \frac{\mathbf{C}_{\mathbf{z}}}{\mathbf{1} + \mathbf{E}_{\mathbf{z}}} \mathbf{H} \log \left[\frac{\sigma_{\mathbf{z}}}{\sigma_{\mathbf{z}}} \right] + \frac{\mathbf{C}_{\mathbf{z}}}{\mathbf{1} + \mathbf{E}_{\mathbf{z}}} \mathbf{H} \log \left[\frac{\sigma_{\mathbf{z}}}{\sigma_{\mathbf{z}}} \right]$$

whereozcisthepreconsolidationstressofthe soil.

Secondaryconsolidation

Secondaryconsolidationistheconsolidationofsoilthattakesplaceafter primary consolidation. Even after the reduction of hydrostatic pressures ome cmpression of soiltakesplaceats low rate. This is known as secondary consolidation. Secondary o

consolidationiscause d bycreep,viscousbehavioroftheclay- watersystem, consolidationoforganicmatter,andotherprocesses.Insand,settlemntcaused by secondarycompressionisnegligible,butinpeat,itisverysignificant.Due to secondaryconsolidationsomeofthehighlyviscouswaterbetweenthepointsof contact is forced out.

Secondaryconsolidationisgivenbythe formula

$$\mathbf{G}_{1} = \frac{\mathbf{H}_{2}}{\mathbf{I} + \mathbf{G}} \mathbf{G}_{1} \mathbf{G}_{2} \mathbf{G}_{3}$$

Where

H0istheeighhtoftheconsolidatingmedium
e0istheinitialvoidratio
Caisthesecondarycompression index
t isthelengthoftimeafterconsolidationconsiderais the
length of time for achieving 90% consolidation

CHAPTER-7 SHEAR STRENGTH

Introduction

Soil mass when loaded may fail due to shear stress induced in it. Examples of such failuresaresinkingofsoilmassunderheavilyloadedfoundation, spallingofsoil along the edge of vertical cut, slide in an earth embankment with a steep slope movement of backfill behind a weak retaining wall etc. In all the above cases, the soil fails essentially due to shear. When the shear stress induced in a mass of soil reaches limiting value, shear deformation occurs, which leads to the failure of soil mass. The resistance offered by the soil to shear is known as shear resistance.

The maximum shearing resistance of soil against continuous shear deformation along potential failure plane is known as **shear strength** of soil. The plane along which failure of soiltakes place due to sliding is known as failure plane. Failure will takeplace on the plane on which the shear stress exceeds the shear resistance. However, if the soil has weak Failure may planes, the failure will be located in the weak est zone. not take place along the plane of maximum shear stress, i.e., the plane which makes 450 with the principal planes.

The shearing resistance of soil is composed of two components: Normal stressdependent and normal stress independent. Examples of the above two cases are:

- 1. Frictionalresistancebetweentheparticlesatthepointofcontact
- 2. Cohesion or force of attraction between soil particles. It is characteristic of soil state and is independent of normal stress across the plane.

Theabovetwocomponentscanbebetterunderstoodbycomparingtwomaterials, sand and clay. Considerable force is required to shear a block of clay as shown in the Figure 1(a) evenwhen there is no external force acting on the block. This force ishigher when the block is dry and lower with increase in water content of the soilsample. This component is called cohesion. On the other hand, if we take a sample of sand in asplit mould and try to shear it, theforcerequired is practically nil when thereisnoexternalnormalforce. Now, if we apply external normal pressure, the force

required to shear the sample increases and is proportional to the normal pressureapplied. This component is called friction.

Shear strength of the cohesionless soil results from inter granular friction as above.

Plastic undrained clay does not have external friction. Hence, strength of soil results

from cohesional one. In other intermediates oils, shear strength of such soil results from

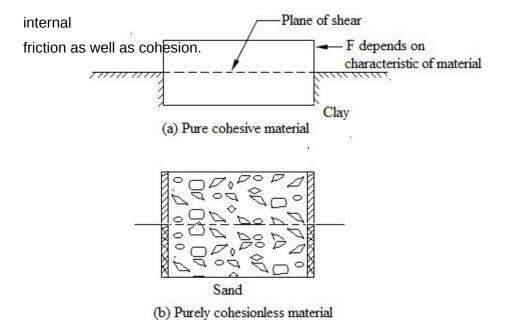


Figure1

Theoryoftwodimensionalstresssystem: Mohr's Stress Circle Innumerable

planes pass through each point in a soil mass. The stress components on each plane through the point depend upon the direction of the plane. It is known from

strength ofmaterialthat there exists threemutually perpendicularplanesthrougha

point on

which there is no shear stress and only normal stress acts. Such planes magnitude, these stresses are known as major principal stress $\square \square \square \square$, in are called principal planes and the normal stresses, the principal stresses. In order of their principal stress $\square \square \square \square$. However, in most soil we deal with,

failure of soil mass is independent of intermediate stress. In such problems two dimensional stress analyses gives acceptable results for the solution of such failure problems.

Consider the case of a soil element as in Figure 2 whose sides are principal planes i.e., only normal stresses are acting on the faces of the element. The stress components at a point on a give plane are given by

where \Box and \Box are normal stress and shear stress component on a plane inclined at anangle of \Box with the major principal plane.

The above results can be represently drawing a circle with radius
$$\frac{1}{2}$$
. The

circlesodrawnisknownasMohr'scircle.Eachpointonthecircumferenceofthe circle gives two stress coordinates at that point on an inclined plane.

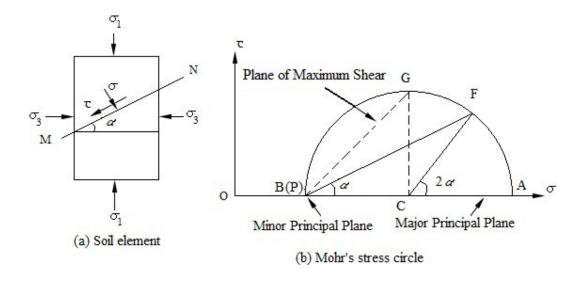


Figure2Mohr'sstresscircle

In Figure 2(a), the major principal plane is horizontal and minor principal plane is vertical. Point Ainthe Mohr's circle represents the major principal stress $\square 1,0 \square$ Brepresents the minor principal stress $\square 3,0 \square$. To determine the stress compone a plane through the point, a point called pole is to be located on the circle. The pole is drawn by drawing a straight line parallel to the plane on which the stress conditions

are known. Hence, the pole *P* islocated by drawing a horizontal line through the pointArepresenting the major principal stress \(\Boxed{1} \Boxed{1}. \text{The pole can also be drawingaverticallinethrough Brepresentingminorprincipalplane \(\Boxed{3} \Boxed{3}. \text{Toknown the stress on the inclined plane, astraightline PF parallel to the plane is drawn through the pole *P*. The point F on the circle gives the coordinates of the stress on the plane inclined at an angle \(\Boxed{3} \) with the direction of major principal plane. The shear stress is considered to be positive if its direction gives a clockwise moment about apoint outside the wedge such as point *E*.

Consider another soil element as shown in Figure 3(a) in which major principal planes are not horizontal and vertical, but are inclined to yandx-directions. The corresponding Mohr's stress circle is drawn as shown in Figure 3(b). Point A

representsprincipalmajorprincipalstress $\square 1,0 \square$ and minorprincipal stress \square locate the pole, a line parallel to the major principal plane is drawn through A to intersect the circle at P. PB gives the direction of the minor principal plane. To determine the stress components on any plane MN inclined at an angle \square with the major principal plane, a line making an angle of \square with PA is drawn through P, to intersect the circle at F. The coordinates of point F give the stress components on the plane MN.

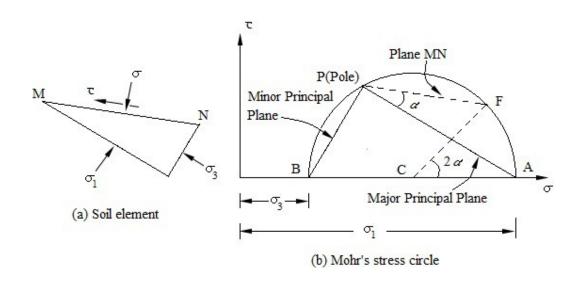


Figure3Mohr'sstresscircle

Mohr-CoulombTheoryofFailure

Varioustheoriesoffailureofsoilhavebeenproposedbymanysoilscientists.Of these,theoneproposedbyCoulombandgeneralisedbyMohrhasbeenthemost useful for failure problems dealing with soil and hence has got wide acceptanceamongst the soil scientists. This failure theory is known as Mohr-Coulomb failure theory.

According to Mohr,thefailureofsoli along aplanetakesplacewhen theshear stress the

onthatplaneexceedstheshearresistanceofthesoil. The shearresistance is tance of the soil. The shearresistance of the soil and the shearresistance of the soil. The shearresistance of the soil and the shearresistance of the soil. The shearresistance of the soil and the shearresistance of the shear expectation of the shear expec

Where $\Box f \Box S \Box$ Shearstressatfailure \Box Shearresistance

If the normal stress and shear stress are plotted, a curve is obtained. This curve is called the shear envelope. Coulomb as sumed the relationship between \Box f and \Box as linear and gave the following strength equation.

$$S\square C\square \square tan\square$$

For most of the cases of stability of soil, Mohr's failure can be approximated as astraight line for practical purposes and thus agrees with the above strength equation given by Coulomb.

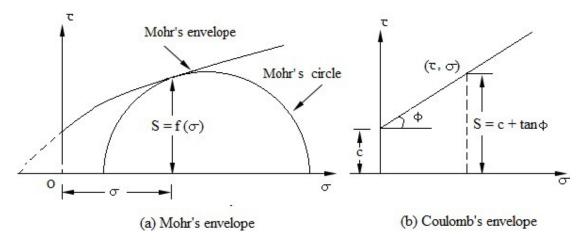


Figure4

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C and \Box in the expression $S\Box C$ \Box \Box tan \Box are empirical constants and are as cohesion

and angle of friction or shearing resistance. In general the above constants are known as shear strength parameters.

Depending upon the nature of soil and the shear strength parameters, soils

can be

described as (i) cohesive soil, (ii) cohesion-less soil, and (iii) purely cohesive soil. The strength envelopes for the three cases are shown in the Figure 5. $\tau = c$

Case II: c = 0

Figure5Strengthenvelopesforthreetypesof soils

Case III: Ø = 0

Effectivestress principle

Case I: c - Ø soil

Extensiveexperimentalstudiesonremouldedclayshaveshowntheshearing strength of soilmassis controlled by the effective stress and not by the total normal stresson the plane of shear. The values of shear parameters, i.e., cohe sion and angle of shearing resistance do depend upon the pore water pressure of the soil. Therefore, the Mohr-Coulomb strength equation may be expressed in terms of effective stress.

_f[C]____tan___

Where $c \square$ and $c \square$ are termed as effective shear parameters.

In terms of total stresses, the equation takes the form

 $\Box f\Box Cu\Box\Box tan\Box u$

Where Cuistheapparent cohesion a wist the apparent angle of shearing resistance

Determinationoffailure

plane

Failureofsoilmaynottakeplacealongtheplaneofmaximumshearstress. The failure will take

place along the most dangerous plane called failure plane. The failure

plane, letus express the normal stress and she arstress on any plane inclined at an angle of to the major principal plane.

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Theequationofshearstrengthisgiven by

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$$\frac{1}{2}$$
 $\frac{1}{2}$ orminimum value of $\frac{1}{2}$ $\frac{1}{2}$

where distheangleoffailure plane with respect to major principal plane.

The above expression for location of failure plane can be directly derived from Mohr's circleshowninFigure6. *EF* represents the failure envelope given by the straight line

 $\Box f \Box C \Box \Box \Box \Box \tan \Box \Box$. *P*isthepolewithstresscoordinates

□□3□,0□.TheMohr'scircle is

tangential to the Mohr envelope at the point *F. PF* represents the direction of failure

plane, inclined at an angle □ with the direction of major principal plane.

From the $\Box 450\Box^{\Box}$ geometry of Figure 6, when get from triangle *EFK*.

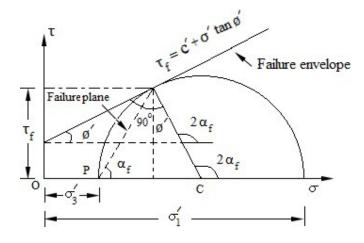


Figure6

Itmaybenotedthatanypointonthefailureenveloperepresentstwostress components \Box and \Box fat failure. And for each \Box and \Box f, there exists two values of principaleffectivestressontwoprincipalplanesforwhichfailuretakesplace. It is evidentfrom Figure 5 that \Box fatfailure is less than the maximum shear stress, corresponding to the point G, and acting on the plane PG. Thus the failure plane does not carry maximum shear stress, and the plane which has the maximum shear stress is not the failure plane.

Determinationofshearstrengthparameters

Sheartestsareconductedonundisturbedsoilsamplesobtainedfromthefield. The testresultsareusedtoplotfailureenvelopetodeterminetheshear strength

parameters. It is to be noted that the shear strength parameters are fundamental properties of soil and are considered as coefficients obtained from the geometry of the strength envelope drawn by using shear test results. So, during test on saturatedsamples, care should be taken to simulate the field drainage condition.

Followingfourmethodsofsheartestsarecommonlyusedinthe laboratory.

- 1. Directsheartest
- 2. Triaxialcompressiontest
- 3. Unconfinedcompressiontest
- 4. Vanesheartest

Basedonthedrainageconditions, the sheartests are classified as

- Consolidateddrainedtest(Drainedtest/Quicktest)
- 2. Consolidatedundrainedtest
- 3. Unconsolidatedundrainedtest

1. Consolidateddrainedtest

This is also known as drained test. In this test drainage of water is allowed

during the

test. The soil sample is first consolidated fully under the normal load (in direct sheartest)

or the all round pressure (in triaxial test) and the shear stress is applied slowly

enough

for the water in the sample to drain away. This simulates the long term conditions in the

life of a structure, i.e., the long term stability of earth dam. The effective

stress

parameters are used.

2. Consolidatedundrainedtest

In this test, the soil is consolidated under the normal load or the all-round pressure

shearingisdonerapidlysothatdrainagedoesnottakeplace. This simulates the sudden effects during the life of a structure, e.g., sudden drawdown of upstream water

levelinanearthdam. The parameter sused are Cu and $\Box u$. If pore pressure

measurements are

made then effective stress parameters can be used.

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3. Unconsolidatedundrainedtest

Inthiscase the normalload or the all-round pressure as well as she arstress are

not get mobilised. This simulates short term failure conditions in a structure, e.g., stabilityofanearthdamimmediatelyafterconstruction. The total stress parameters are used for these cases.

Directsheartest

The direct shear test apparatus consists of (i) shear box of square or circular section,

- (ii)loadingyokeforapplyingnormalforce, (iii)gearedjackforapplyingshear force,
- (iv) proving ring to measure shear force, and (v) strain gauges to measure horizontal displacement and vertical displacement for volume change.

The shear box consists of two halves which can slide relative to each other. The lower half is rigidly held in position with the bottom of the shear box container, which slides shearforce. The geared jackmay

partitions it her by slectric motal act by hande the upper half of the box is buttagainst a proving ring. The soil sample is placed and compacted in the shear box. The sample held in position between a pair of metal grids and porous stones or plates as shown in the Figure 7. The grid plates, provided with linear slots, are placed above the top and below the bottom of the specimen. To have proper grip with the soil specimen, the linear slots in the grid plate are aligned perpendicular to the direction of the shearing helpoftwo

areremoved force. The soils pecimenis compacted in shear box by clamping together with the before shearing force is applied. Direct shear test may be of two types. Strain controlled shear screws provided for the purpose. However, the sescrews box and stress controlled shear box. The working principles of two types of shear box are explained in the following paragraphs.

In case of strain controlled shear test a normal load N is applied on the specimen by means of loading yoke and is kept constant throughout the test. The shearing strain is increased at a constant rate by pushing the lower box through the geared jack. The movementof lower partofthebox istransmitted throughthespecimento theupper part of the box. The proving ring attached to the upper part reads the shear force F at failure. A number of tests are conducted on identical specimens with increased normal loadsandthecorrespondingshearforcerecorded. Agraphisplotted between the shearforce F as ordinate and the normal load N as the abscissa. The plots on btained is known as the failure envelope. Figure 8(b) shows the failure envelope polotted as a

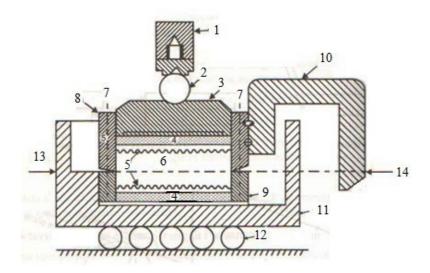


Figure7Shearboxwithaccessories

1	Loadingyoke	8.	Upperpartofshearbox
	Steelball	9.	Lowerpartofshearbox
2	Loadingpad	10.	U-arm
	Porousstones	11.	Containerforshearbox
3	Metalgrids	12.	Rollers
	Soilspecimen	13. 14.	Shearforceappliedbyjack
4	Pinstofixtwohalvesofshear box	1 -7.	Shear resistance measured by
•			proving ringdial gauge

.

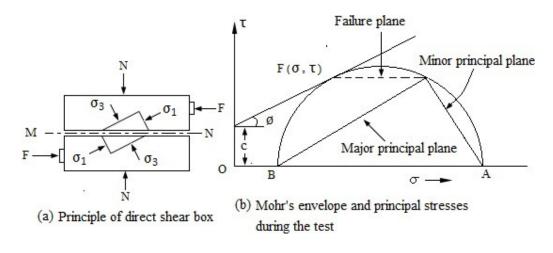


Figure8Shearboxtest

Advantagesofdirectsheartest

- 1. Directsheartestisasimpletestcomparedtothemorecomplextriaxialtest.
- 2. As the thickness of sample is small, it allows quick drainage and rapid dissipation of pore pressure during the test.

Disadvantagesofdirectshear test

- The distribution of normal stresses and shear stresses over the potential failure plane is not uniform. The stress is more at the edges and less at the centre. Hence, progressive shear failure takes place as the shear strength is notmobilised simultaneously at all points on the failure plane.
- $2. \ The failure plane is predetermined, which may not be the weak est plane.$
- 3. Theareaundersheargraduallydecreasesasthetestprogresses. The corrected area at failure, Af should be used for computing the values of normal stress \square and shear stress \square .
- 4. Thereis littlecontrol on thedrainage ofporewater ofsoil as compared to the triaxial test.
- 5. Thestressonaccountoflateralrestraintduetosidewallsofshearboxisnot accounted for in the test.
- 6. Thereisnoprovisionformeasurementofporewaterpressure.

Problem1.

Expanaetirectsheartestonundisturbedsoilsample, following data have been

Evaluate the undrained shear strength parameters. Determine shear strength, major and minor principal stresses and their planes in the case of specimen of sample subjected to a normal stress of 100 kN/m2.

Normalstress(kN/m2)

11011110110110	00(111 1/1112)		70	96	114
Shear	stress	at	138	156	170
failure(kN/r	m2)				170

Solution.

$Plot the shear stress versus normal stress to obtain the failure envelope keeping the \ scale \ same and \ scale \ scale \ same and \ scale \ sc$
for both the stresses. From the plot in Figure 9,

Theangleofshearingresistance, $\Box\Box\Box\Box\Box$; cohesion, $c\Box\Box\Box$ kN/m2

The shear strength corresponding to the normal stress of 100 kN/m2 is 160 kN/m2.

The

coordinate corresponding to (100, 160) is the failure point F. Draw the Mohr'scircle so that the failure envelope is tangent to the circle at F. To do so, draw FC perpendicular to the failure envelope. With C as centre and CF as radius, draw a circleso as to intersect the normal load axis at A and B. Point A corresponds to the major

principalstress $\sqcup 1 \sqcup 410$ kN/m 2 andpoint B correspondstotheminorprincipal stre	ess
□3□20kN/m2.	

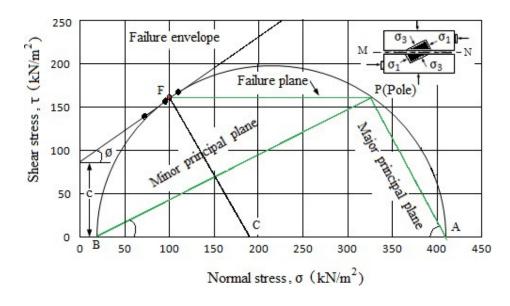


Figure9

To locate the position of the pole, draw a line *FP* parallel to the failure plane in theshearbox(horizontal). *P*isthepole. *PA*isthedirectionofmajorprincipal plane which makes

an angle 57 in the clockwise direction with the plane of shear. PB is the minor

principal

plane, making an angle of 58 in the anticlockwise direction with the plane of shearing.

Problem2. A sample of cohesionless sand in a direct shear test fails under a

shear stress of 160

kN/m2 when the normal stress is 140 kN/m2. Find the angle of shearing resistance and

the principal stress at failure. Solution.

Plotthefailureenvelopepassingthroughtheoriginandthepointwithcoordinate (140, 160) as

normal stress and shear stress coordinates. The scale for both the stress axes are perpetuetinthe Figure 10,

Same Theangleofshearingresistance, $\Box\Box\Box\Box\Box\Box\Box\Box$; cohesion, $c\Box 0$

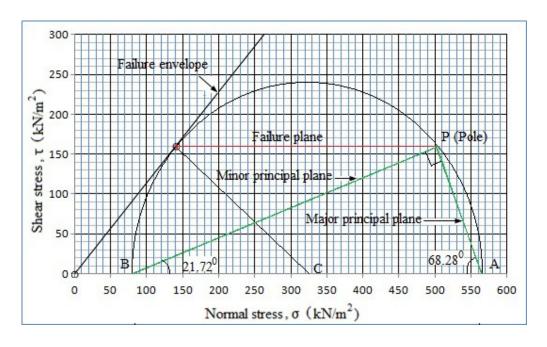


Figure 10

Draw the Mohr's circle so that the failure envelope is tangent to the circle at F. To doso, draw FC perpendicular to the failure envelope. With C as centre and CF as radius, drawacirclesoastointersectthenormalloadaxisat AandB.PointAcorrespondsto themajorprincipalstress $\square \square 565..81$ kN/m2 and pointBcorrespondstotheminor principalstress $\square \square 80.35$ kN/m2.

To locate the position of the pole, draw a line *FP* parallel to the failure plane in theshearbox(horizontal). *P*isthepole. *PA*isthedirectionofmajorprincipal plane which makes

an angle 68.280 in the clockwise direction with the plane of shear. *PB* istheminorprincipalplane,makinganangleof21.720intheanticlockwisedirection with the

plane of shearing. Problem3. A cylinder of soil fails under an axial stress of 80

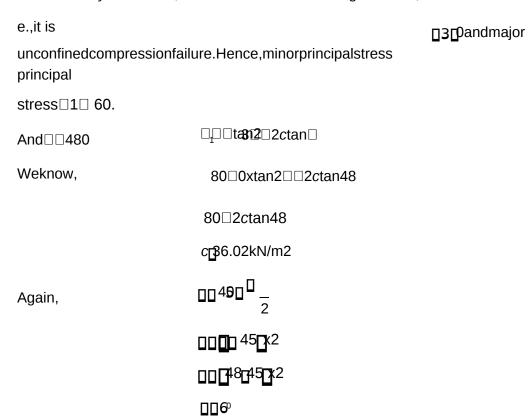
kN/m2. The failure plane makes an

angle of 480 with the horizontal. Calculate the value of cohesion and the angle ofinternal

friction of the soil. Verify by graphical method.

Solution.

As the reisonly axial stress, the reison lateral stress acting on the soil, i.



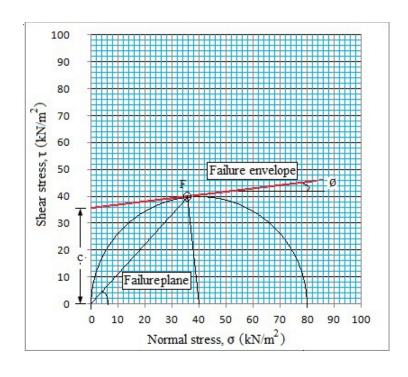


Figure11

The Mohr's stress circle is drawn with rad $\frac{1}{2}$ $\frac{800}{2}$ $\frac{1}{2}$ 40. The circle passes

throughtheoriginrepresentingtheminorprincipalstresswhichisalsothepole. FailureplaneisdrawnthroughthepoleOsoastointersecttheMohr'scircleatF. JoinFwiththecentreCoftheMohr'scircle.Drawthefailureenvelopebydrawinga tangentatFonthecirclesoastointersectthey-axis.Theslope $\Box\Box$ 60ofthefailure plane is the angle of shearing resistance. The y-intercept c = 36.02 kN/m2 is thecohesion.

Triaxialcompressiontest

Triaxial shear test is the most extensively used for computation of shear strength parameters. In this test, the pecimen is compressed by applying all the three principal stresses, $\Box 1$, $\Box 2$ and $\Box 3$.

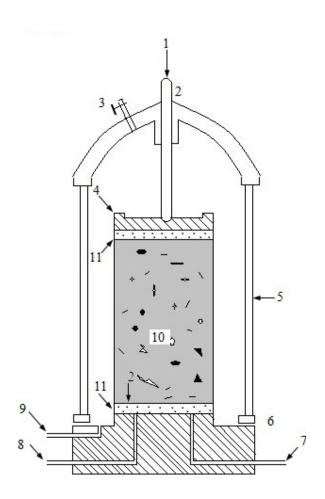


Figure12Triaxialcell

- 1. Axialloadmeasuredbyproving ring dial gauge
- 2 LoadingarmAirreleasevalve
- Top cap
- 4 PerspexcylinderSealingring

- 7. Porewateroutlet
- 8. Additionalporewater outlet
- 9. Cellfluidinlet
- 10 Soilspecimenenclosedinrubber membrane
- · Porousdisc

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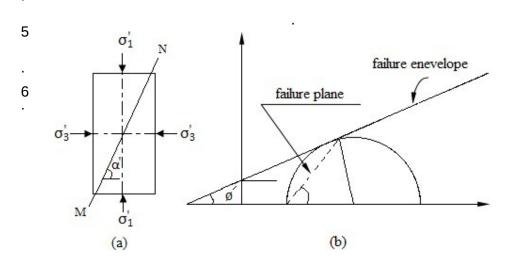
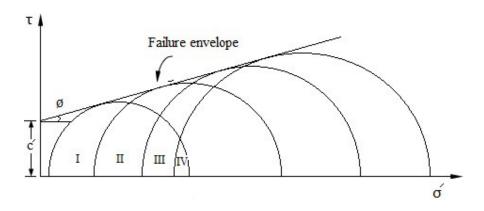


Figure 13 Stress condition and failure envelope intriaxial compression test



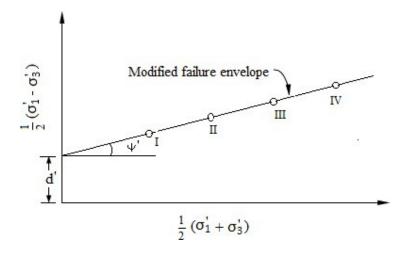


Figure14Failureenvelopes

Advantagesoftriaxialcompression test

Followingsaretheadvantagesoftriaxialcompressiontestoverthedirectshear test.

- Unlike the direct shear test in which the soil sample is forced to fail along a
 predetermined plane, the specimen in triaxial compression is free to fail alongthe
 weakest plane.
- 2. Distribution of stress is uniform along the failure plane is uniform. The shear strength is mobilized uniformly at all points on the failure plane.
- The test procedure has complete control of the drainage conditions. The field drainage conditions are better simulated in triaxial compression test ascompared to direct shear test.
- 4. Precise measurements of pore pressure and volume change are possible during the test.
- 5. The effect of end restraint does not have considerable effect on the result as failure usually occurs near the middle of the sample.

Unconfinedcompression test

Unconfinedcompressiontestisaspecialcaseoftriaxialcompressiontestinwhich no lateralorconfiningstress

1213194plied.Acylindricalsoilsample of length2to2.5timesthediameterisusedastestsample.Thesoilspecimenisonly to

the major principal stress \square 1 till the specimenta il sdue to she aring along a critical failure plane.

Figure 15 shows the simplest form of compression testing machine. It consists of asmallload frame fitted with a proving ring to measure the vertical stress 1applied to the soil specimen. A separate dial gauge is used to measure the deformation of the sample.

The sample is conically hollowed at its ends and placed between two conical seatings attached to two metal plates. The conical seatings reduces end restraints and prevents the tendency of the specimen to become barrel shaped. The load is applied through a calibrated spring by manually operated screw jack at the top of the machine. The test sample is compressed at uniform rate of strain by the compression testing equipment. the

Shearialdaformationarial metalliase or dilugariate tumor essive to contract the dature of a definite maximum load is indicated by the proving ring which decreases rapidly with further increase of strain. However, no definite maximum load is indicated by the proving ring dial in case of a plastic failure. In such a case, the load corresponding to 20% strain is arbitrarily taken as the failure load. The maximum axial compressive stress resisted by the specimen before failure is called the unconfined compressive strength.

Theunconfinedcompressiontestisaquicktestinwhichnodrainageisallowed.

Since □3 □

0,theMohr'scirclepassesthroughtheorigin,whichisthepole.Figure 16 shows the stress conditions in a typical unconfined compression test. The equation plastic equilibrium may be expressed as

$$\Box 1 \Box 2cu$$
 tan $\Box \Box 2c$ tan $\Box \Box 45 \ 0 \ \Box u$

Intheabove equation, there are two unknowns cu and $\Box u$, and cannot be determined by the unconfined tests ince an umber of test on the identical specimens give the same value of $\Box 1$. Hence, the unconfined compression test is generally conducted on saturated clay for which the apparent angle of shearing resistance $\Box u \Box 0$. Hence

TheradiusoftheMohr'scircleis

Thefailureenvelopeishorizontal.
$$PF$$
is

thefailureplane, and the stresses on the failure plane are

$$\begin{array}{cccc}
q \\
u \\
2 & 2
\end{array}$$

where qu is the unconfined compressive strength at failure. The compressive stress $q = \frac{F}{ac}$ is calculated on the basis of changed cross-sectional area Acat failure, which

isgivenby

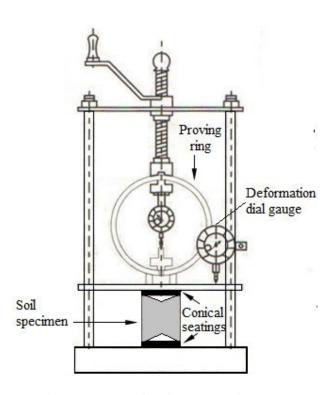


Figure15UnconfinedCompressiontestset up

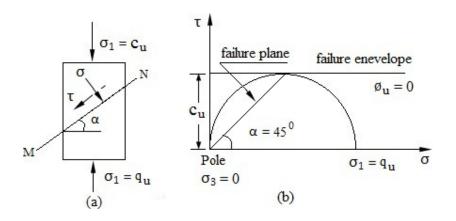


Figure16Unconfinedcompression test

Where

Ac= corrected area of cross section specimen

A0= initial area of cross section of

specimenL0= initial length of the specimen

V=initialvolumeofthespecimen

 \Box *L*=changeinlengthatfailure

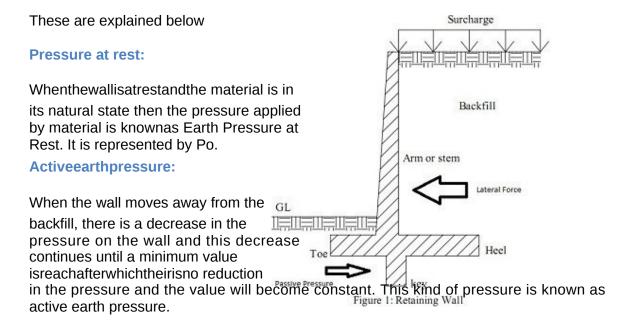
 $\Box \Box \frac{\Box L}{\Box a}$ xialstrainatfailure L0

CHAPTER-8 EARTHPRESSUREONRETAINING STRUCTURES

In 1929 Terzaghi (The Father of Soil Mechanics) conducted experiments on the retaining wall and showed the relation of pressure on the wall if wall changes itspositioni.etomoveinwardstothebackfill,outwardsofitorremainatitsplace.

Therearethreetypesofearthpressuresonthebasisofthemovementofthe wall.

- EarthPressureatrest
- 2. ActiveEarthPressure Passive Earth Pressure



Passiveearthpressure:

When the wall moves towards the backfill, there is an increase in the pressure on the wall and this increase continues until a maximum value is reach after which their is no increase in the pressure and the value will become constant. This kind of pressure is known as passive earth pressure. This means that when the wall is about to slip due to lateral thrustfrom thebackfill, are sistive force is applied by the soil in front of the wall.

Alternatively:-

Earth pressure is the force per unit area exerted by soil. The ratio of horizontalto vertical stress is called coefficient of lateral earth pressure (K).

$$K = \frac{\sigma'_h}{\sigma'_v}$$

Earthpressureforcescanbeat-rest(Figa), active(b) or passive (c).

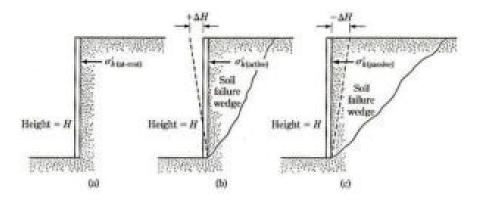


FIG-2

Typicalrangeoflateralearthpressure coefficients

Condition	Granular Soil	Cohesive Soil
Active	0.20-0.33	0.25-0.5
Passive	3–5	2–4
At-Rest	0.4-0.6	0.4–0.8

At-RestEarthPressure

Underconditionsofzerohorizontaldisplacement, the soil is said to beat-rest:

When the retaining wall is at rest then the ratio between the lateral earth pressure and the vertical pressure is called the co-efficient of the earth pressure at rest,

Ko=lateralpressure/vertical pressure

Ko≈1-sinΦ'(granularsoils)

ActiveEarthPressure

For a level backfill (β =0), the following equation is used to determine the active earth pressure (pa) for all types of soils.

When the retaining wall is moving away from the backfill the the ratio between lateral earthpressureandverticalearthpressureiscalledco-efficientofactiveearth pressure.

Ka=lateralpressure/vertical pressure

$$p_a = K_a \gamma H - 2c \sqrt{K_a}$$

For saturated clay soils, $\Phi = 0$; Ka=1: pa=yH-2c

For granular soils, c=0: pa = Ka y H

The critical depth, Zcr, which is the depth at which the horizontal pressure is zero, can estimated by:

$$z_{cr} = \frac{2c}{\gamma \sqrt{K_a}}$$

Thetotalactiveresultantforce(withoutsurchargeorcohesion)issolvedfor by:

$$R_a = \frac{1}{2} p_a H = \frac{1}{2} K_a \gamma H^2$$

PassiveEarthPressure

Foralevelbackfill(β =0),thefollowingequationisused to determine the passive earth pressure for all types of soils.

When the retaining wall is moving towards the backfill, then the ratio between the lateral earth pressure and the vertical earth pressure is called the Co-efficient of passive earth pressure.

Kp=lateralpressure/vertical pressure

$$p_p = K_p \gamma H + 2c \sqrt{K_p}$$

For saturated clay soils, $\phi = 0$, $K_p = 1$: $p_p = \gamma H + 2c$

For granular soils, c = 0: $p_p = K_p \gamma H$

Thetotalpassiveresultantforce(withoutsurchargeorcohesion)issolvedfor by:

$$R_p = \frac{1}{2} p_p H = \frac{1}{2} K_p \gamma H^2$$

Surcharge:

Thematerialwhichlieabovethehorizontalleveloftheretainingstructureisknown as surcharge. The angle which this material makes with the retaining is surcharge angle.

8.2-UseofRankine'sformulaforthefollowingcases(cohesion-less) soil only)

 $Assumptions made by Rankine for the derivation of earthpressure \ . \\$

- > Thesoilmassishomogeneousandsemi-infinite.
- > Thesoilisdryandcohesionless.
- > Thegroundsurfaceisplane, which may be horizontal or inclined.
- > Thebackoftheretainingwallissmoothandvertical.
- > Thesoilelementisinastateofplasticequilibrium,i.e.,atthevergeoffailure

ACTIVEEARTH PRESSURE:

1. Backfillwithno surcharge

LetusconsideranelementofdrysoilatadepthZbelowalevelsoilsurface. Initially ,theelementisatrestconditions,andthehorizontalpressureisgiven by σh =k0 σv

Where σ visthevertical stress at C, and σ his the horizontal stress at C. Of course, σ v = yZ.

The stresses σ h and σ v are respectively minor

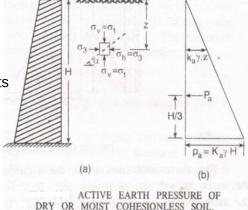
and major principal stresses, and are indicated by points A and B in the Mohr circle in fig 2.b.

Let us now consider the case when the vertical stress remains constant while the

horizontal stress is decreased. The pointA shifts to position A' and the diameter of the Mohr circle increases. In the limiting condition, the point A shifts to the position A' when the Mohr circle [marked (3)] touches the failure envelope. The soil is at the verge of shear failure. It has attained the

Rankine's active state of plastic equilibrium. Thehorizontalstress atthatstate is the active pressure(Pa).

Fig.2.c shows the Mohr circle when active conditions are developed. Point E represents the active condition. From the figure,



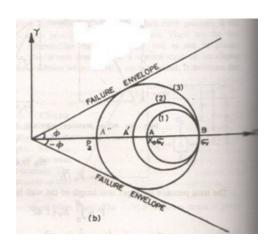


FIG2.(b) FIG 2.(c)

Pa= OE=OC-CE

CE=CD=OC sin∅',

 $Pa=OC-OCsin \varnothing'=OC(1-sin \varnothing') \qquad ...(a)$

 σv =OB=OC+CB=OC+OCsin \emptyset '

 $\sigma v = OC(1 + \sin \varnothing')$...(b)

FromEqs.(a)and(b),

Pa 1−sin⊘'

 $\sigma v = \frac{1 + \sin \emptyset}{1 + \sin \emptyset}$

Par 1-sin⊘'

Pa=Kayz ..(c)

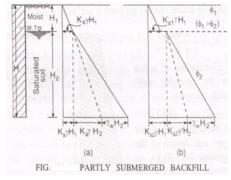


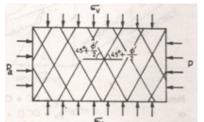
FIG2.(e)

Where Kais a co-efficient of active earth pressure . It is a function of the angle of

shearing

resistance(∅'),andis

Fig.2.eshowsthe inclined at $(45^{\circ} + \emptyset/2)$



givenby
$$K_{\overline{a}} = (\frac{1-\sin\emptyset'}{1+\sin\emptyset'})=$$

failureplanes. These are to the major principal

plane which is horizontal. The total active earth pressure *Pa* or the resultant pressure per unit length of the wall is found by integrating or from the triangular pressure distribution diagram.

 $P_{a=0}^{-1}$ KayH2actingatH/3fromthebaseofthewall.

If the soil is dry ,y is the dry unit weight of the soil, and if wet,yis the moist weight.

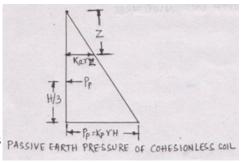
2. Backfillwithuniform surcharge

If the backfill is horizontal and carries a surcharge of uniform intensity q per unit area, the vertical pressure increment, at any depth Z, will increase by q. The increase in the lateral pressuredueto this will beKaq.Hencelateral pressure at any depth Z isgiven by

Pa=Kayz+Kaq

Atthebaseofthewall, the pressure intensity is Pa

FIG. 3(a) and(b) shows thetwo alternativemethods of plotting the lateral pressure diagram for



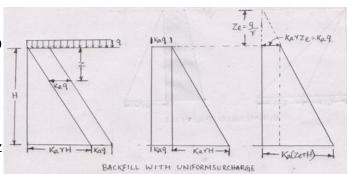
thiscase. The lateral pressure increment due to the surcharge is the same at every point of the back of the wall, and does not vary with depth Z. The height of the fill Ze, equivalent to the uniform surcharge intensity is given by the relation,

$$Ka_{\gamma ze=Kaq,ze=}$$

This means that the effect of the surcharge of intensity q is the same as that of a fill of height Ze above the ground surface.

3. Submerged Backfill

In this case, the sand fill behind the retaining wall is saturated with water. The lateral pressure is made up of two components: (i)lateral pressure due to submerged weighty'of the soil, and (ii)lateral pressure due to water. Thus at any depth z below the surface.



Pa=Kay'z+ywz

The pressure at the base of the retaining wall (z=H) is given by

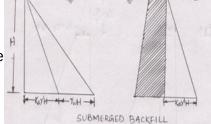
Pa=Kay'H+ywH

If the free water stands to both sides of the wall, the water pressure need not be considered, nd the net lateral pressure is given by

Pa=Kay'H

Ifthebackfillispartlysubmerged,i.e.,thebackfillis moist to a depth H1below the ground level, and then it is

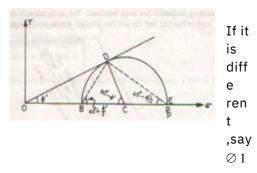
submerged,thelateralpressureintensityatthebaseof the wall is given by

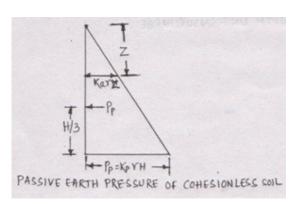


$$P_{a}=K_{a}\gamma'H1+Ka\gamma'H2+\gamma wH2$$

The above expression is on the assumption that the value

of of $\ensuremath{\mathcal{O}}$ is the same for the moist as well as submergeds oil.





and Ø2 respectively, the earth pressure co- efficient, KandK torboththeportions will be different. As Ø decreases K

increases. The lateral pressure intensity at the base of wallis given by

Pa=Ka1y'H1+Ka2y'H2+ywH2

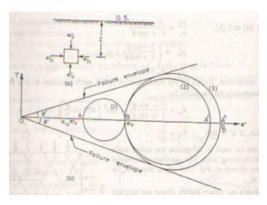
PASSIVEEARTHPRESSURE

Let us consider an element of dry soil at a depth Z below a level soil surface. As the soil is compressed laterally , the horizontal stress is (σ h) increased, where asthe vertical stress (σ v) remains constant.

The stresses σ h and σ vare respectively minor and major principal stresses, and are indicated by

pointsAandBintheMohrcircle.

The pointA shifts to position A' and the diameter of the Mohr circle increases. In the limiting condition, the point A shifts to the position A" when the Mohr circle [marked (3)] touches the failure envelope. The soil is at the verge of shear failure. It has attained the Rankine avtive state of plastic equilibrium. The horizontal stress at that state is the active pressure(Pp).



 $\sigma v = OC(1-\sin \emptyset')$..(e) From Eqs.(a) and (b),

..(d)

$$\frac{Pp}{\sigma v} = \frac{1 + \sin \varnothing'}{1 - \sin \varnothing'}$$

$$Pp = (\frac{1 + \sin \varnothing'}{1 - \sin \varnothing'}) \sigma v$$

Where Kpis a co-efficient of passive earth pressurelt is a function of the angle of shearing resistance (\emptyset '), and is given by

$$K_{p}^{=}(\frac{1+\sin\emptyset'}{1-\sin\emptyset'}=\tan 245^{\circ}-(\frac{\emptyset'}{})]$$

Figure shows the failure planes. These are inclined at (45°+ Ø/2) to the major principal plane which is horizontal.

The distribution of passive earth pressure, given in Eq.(f) is triangular, with maximum value of

KpyH at the base of the retaining wallof height H. The total pressurePp for a depth H is given by

= 1 Kp = 2 M

If a uniform surcharge intensity per unit area acts over the surface of the backfill, the increase in the passive pressure will be equal to Kpq. The passive pressure $Pp = Kp (\gamma Z + q)$ intensity at a depth z is then given by

EX- 1:

Compute the intensities of active and passive earth pressure at depth of 8 metres indry cohesionless sand with an angle of internal friction of 300 and unit weight of 18 kN/m3. What will be the intensities of active and passive earth pressure if the water level rises to the ground level ?Take saturated unit weight of sandas 22kN/m3.

Solution: (a)Drysoil:

$$\mathsf{Ka} = \frac{1 - \sin \varnothing'}{1 + \sin \varnothing'} = (\frac{1 - \sin 30^{\circ}}{1 + \sin 30^{\circ}}) = \frac{1}{3} \qquad \mathsf{Kp} = (\frac{1 + \sin \varnothing'}{1 - \sin \varnothing'}) = (\frac{1 + \sin 30^{\circ}}{1 - \sin 30^{\circ}}) = (\frac{1 + \sin 30^{\circ}}{1 - \sin 30^{\circ}})$$

Pa=Ka
$$_{yH=}^{1}$$
 $_{x8x8=48}^{1}$ kN/m2

Pp=KpyH=3x8x8= 432kN/m2

(b)SubmergedBackfill:

$$y' = Sat = 32-9.81=12.19kN/m$$
 $P = K H + \gamma H = x^{1} 12.19x8 + (9.81x8) = 111kN/m2$
 $y' = \gamma Sat = 32-9.81=12.19kN/m$
 $y' = \gamma Sat = 32-9.81=12.19kN/m$
 $y' = \gamma Sat = 32-9.81=12.19kN/m$

EX- 2:

A retaining wall 4 mhigh, has a smooth vertical back. The backfill has a horizontal surface in level with the top of the wall . There is uniformly distributed surcharge loadof36kN/m2intensityoverthebackfill.Theunitweightofthebackfillis18kN/m3; its angle of shearing resistance is 30oand cohesion is zero. Determine the magnitudeand point of application ofactivepressure per metre length of the wall.

Solution: K=
$$a(\begin{array}{cc} \frac{1-\sin\varnothing'}{1+\sin\varnothing'} \end{array}) = (\begin{array}{cc} \frac{1-\sin30^\circ}{1+\sin30^\circ} \end{array}) = -\frac{1}{3}$$

Thelateralpressureintensityduetothesurchargeisgiven by

$$p1=Kaq={1 \atop 3} \%6=12kN/m^2$$

Thepressureintensityduetobackfill,atdepthH=4misgiven by,

$$p_{z}=K_a$$
 yH= 1 x18x4=24kN/m2

Thetotalpressureintensityatthebaseofthewallisgiven by

$$p = p + p = 12 + 2 = 4 = 36 \text{kN/m}^2$$

The resultant total pressureP1 due to intensity p1given by : P1=

$$p1x H = 12 x 4 = 48 kN/m$$

Actingat4/2=2mfromthe base.

TheresultanttotalpressureP2duetointensityp2givenby:

P2 =
$$\frac{1}{2}$$
x p2x H = $\frac{1}{2}$ x24x4=48kN/m,actingat $\frac{1}{3}$ x4=1.33mfromthebase.

P=P1+P2=48+48=96kNpermetrelengthofthe wall.

The resultant P acts at a distance zabove the base , given by taking the moments about the base :

$$z = \frac{(48x2)+(48x1.33)}{96} = 1.67m$$

CHAPTER-9 FOUNDATION ENGINEERING

FOUNDATION: It is the bottom most part of the structure that remains in direct contact with soil and transmits the load of the structure underneath.

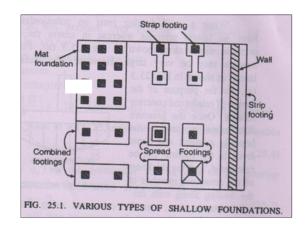
Functions of the foundation- In addition to transmitting the load of the superstructure to the soil it provides stability to the structure against overturning and erosion.

SHALLOWFOUNDATIONS

Types of Foundations may be broadly classified under two heads: shallow foundations and deep foundation is shallow if its Terzaghi, a foundation.

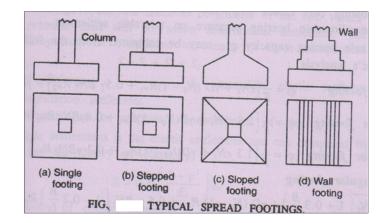
According to Terzaghi, a foundation is shallow if its depth is equal to or less than its width.

In the case of deep foundation, the depth is equal to or greater than the width. Apart from deep strip, rectangular or square foundations, other common forms of deepfoundationsare:pierfoundation, pier foundation are and well foundation. The shallow foundations are of the following types: spread



footing (or simply, footing), strap footing, combined footing, and mat or raft footing.

Fig.showsthecommontypesofshallow foundations.



Aspreadfootingorsimply footingisatypeofshallowfoundationused totransmittheloadofanisolatedcolumn,orthatofawalltothesubsoil. This ismostcommontypeoffoundation. The base of the columnor wall is enlarged or spread to provide individual support for the load. Fig. shows some typical spread footings.

BearingCapacity:

Definitions:

- 1. Footing: A footing is a portion of the foundation of a structure that transmits loads directly to the soil.
- **2. Foundation:**Afoundationisthatpartofthestructurewhichisindirect contactwithandtransmitloadstothe ground.
- **3. Foundationsoil:**Itistheupperpartoftheearthmasscarryingthe load of the structure.
- 4. **Bearingcapacity:** The supporting power of a soil or rock is referred to as its bearing capacity. The term bearing capacity is defined after attaching certain qualifying prefixes.
- Gross pressure intensity (q): The gross pressure intensity q is thetotal pressure at the base of the footing due to the weight of the superstructure, self-weight of the footing and the weight of the superstructure.

6. **Netpressureintensity(qn).**Itisdefinedastheexcesspressure,or the difference in intensities of the grosspressure after the construction of the structure and the original overburden pressure. Thus, if D is the depth of footing.

$$q$$
n=q- σ =q-yD

Where yistheaverage unitweight of soil above the foundation base.

- 7. Ultimate bearing capacity (qf). The ultimate bearing capacity isdefined as the minimum gross pressure intensity at the base of the foundation at which the soil fails in shear. (When the term bearing capacity is used in this book without any prefix, it may be understood to be ultimate bearing capacity).
- 8. Net ultimate bearing capacity (q nf). It is the minimum net pressure intensity causing shear failure of soil. The ultimate bearing capacity qf and the net ultimate capacity are evidently connected by the following relation: $qf = qnf + \sigma \qquad ...(9.1) \qquad or \qquad qnf = qf \sigma \qquad$ 9.1(a)

Where σ is the effective surcharge at the baselevel of the foundation.

- **9. Effective surcharge at the base level of foundation** (σ) . It is the intensity of vertical pressure at the vase level of foundation, computed assuming total unitweight for the portion of the soil above the watertable and submerged unit weight for the portion below the water table.
- **10. Netsafebearingcapacity**(qns). Thenetsafebearingcapacity is the net ultimate bearing capacity divided by a factor of safety F

qns=___

11. Safebearingcapacity(qs). The maximum pressure which the soil can carry safely without risk of shear failure is called the safe bearing capacity. It is equal to the net safe bearing capacity plus original overburden pressure:

$$qs=qns+\gamma D=\frac{qnf}{F}+\gamma D$$

Sometimes, the safe bearing capacity is also referred to as the ultimate bearing capacity gfdivided by a factor of safety F.

12. Safe bearing pressure or Net soil pressure for specified settlement.

It is the intensity of loading that will cause a permissible settlement or specified settlement for the structure.

13. Allowable bearing capacity or pressure (qa). It is the net loading intensity at which neither the soil fails in shear nor there is excessive settlement detrimental to the structure.

TYPESOFBEARINGCAPACITY FAILURES:

Experimental investigations have indicated that when a footing fails due to insufficient bearing capacity, distinct failure patterns are developed, depending upon type of failure mechanism. Failure is accompanied by appearance of failure surfaces and by building of sheared mass of soil. Vesic (1963) observed three types of bearing capacity failures (fig. 9.2).

- 1.Generalshearfailure,2.Localshearfailureand3.Punchingshear failur e.
- 1. Generalshearfailure:Inthecaseofgeneralshearfailure,continuo
 us failure surfaces develop between the edges of the footing and
 the ground
 surface,asshowninFig.9.2(a).Whenthepressureapproachesthevalue

 of gf the state of plastic equilibrium is reached initially in the soil.
- of qf, the state of plastic equilibrium is reached initially in the soil

around the

edges of the footing, and it then gradually spreads downwards and out wards,

abovethefailuresurfaces. The failure is accompanied by appearance of failure surface and by considerable building of sheared mass of soil. However,

thefinalslipmovementwouldoccuronlyononeside,accompaniedbytitling of the footing. Such a failure occurs in soil of low compressibility, i.e. dense or stiff soil, and the pressure-settlement curve is of the general form as shown curveaofFig.9.2(d).followingarethetypicalcharacteristicsofgeneral shear failure.

(i) Ithaswelldefinedfailuresurfaces, reachinguptogroundsurface.

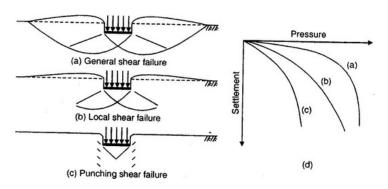


Fig9.2ModelsofBearingCapacityFailures

- (ii) There is considerable bulging of sheared mass of soil adjacent to the footing.
- (iii) Failureisaccompaniedbytitlingofthefooting.
- (iv) Failureissudden, with pronounced peak resistance.
- (v) Theultimatebearingcapacityiswelldefined.
- 2. Local shear failure: In local shear failure, there is significantcompression of the soil under the footing and only partial develop ment of state of plastic equilibrium. Due to this reason, the failure surfaces do not reach the ground surface and only slight heaving occurs. The pressure settlement curve is represented by curve b of Fig. 24.2(d), where the peak of the base resistance may never be reached. In such a failure, titling of foundation is not expected. Local shear failure is associated with soils of high compressibility and in sands having relative density

lying between 35 and 70 percent. The failure is not sudden, and itis

characterized by occurrence of relativelylargesettlementswhichwouldnotbeacceptableinpractice. Also,

ultimatebearingcapacityinsuchafailureisnotwelldefined.Followingare typical characteristics of local shear failure.

- 1. Failurepatternisclearlydefinedonlyimmediatelybelowthefooting.
- 2. Thefailuresurfacesdonotreachgroundsurface.
- 3. Thereisonlyslightbulgingofsoilaroundthefooting.
- 4. Failureisnotsuddenandthereisnotitlingoffooting.
- 5. Failureisdefinedbylargesettlements.
- 6. Ultimatebearingcapacityisnotwelldefined.
- 3.Punching shear failure: Punching shear failure occurs where there relativelyhighcompressionofsoilunderthefooting, accompanied by shearing in the vertical direction around the edges of the footing. Punchingshear may occur in relatively loose sand with relative density less than 35%. Punching shear failure may also occur in a soil of low compressibility if the foundation is located at considerable depth. The failure surface.

isverticalorslightlyinclinedandfollowstheperimeterofthebase,never reaches the ground surface. There is no heaving of the ground surface away

fromtheedgesandnotitlingofthefooting.Relativelylargesettlementsoccur in this mode. The ultimate bearing capacity is not well defined. Following the characteristics of punching shear failure.

- i) Nofailurepatternisobserved.
- ii)Thefailuresurface, which is vertical or slightly inclined, follows the perimeter of the base.
- iii) Thereisnobulgingofsoilaroundthefooting.
- iv) Thereisnotitlingoffooting.
- v) Failureischaracterizedintermsofverylargesettlements.
- vi) Theultimatebearingcapacityisnotwelldefined.

Conditionsfortypicalmodeoffailure:

Table 9.1 gives the conditions under which a typical mode of failure may occur.

Modesoffailureoffootingsinsand:

Fig. 9.3 shows the modes of failure of footings in sand. As the relative depth/widthratioincreases, the limiting relative densities at which failure type change increases.

TABLE9.1.CONDITIONSOFTYPICALMODEOF FAILURE

Condition.	Modeof failure
1.Footingsongroundsurfaceoratshallowdepth,inverydense sand	Generalshearfailure
2.Footingonsaturated,normallyconsolidatedclay,under underained	Generalshearfailure
loading	
3.Verydeepfootingindense sand	Punchingshear failure
4.Footingonsurfaceorshallowdepthinloosesand	Punchingshear failure
5.Footinginverydensesand,loadedbytransientdynamic loads	Punchingshear failure
6.Footingonverydensesandunderlainbyloosesandorsoft clay	Punchingshear failure
7.Footingonsaturated,normallyconsolidatedclayunderdrained loadi	Punching / local shear
ng 8.Footingongroundsurfaceoratshallowdepth,insoilsof high	failure
compressibility	Localshearfailure
9. (a) Footing at groundsurface or at shallow depth, in sands of	
relativedensity between 0.3 to 0.7	Localshearfailure
(b)Footingatgreatdepth,insandsofrelativedensitybetween0.7to 0.9	
	Localshearfailure

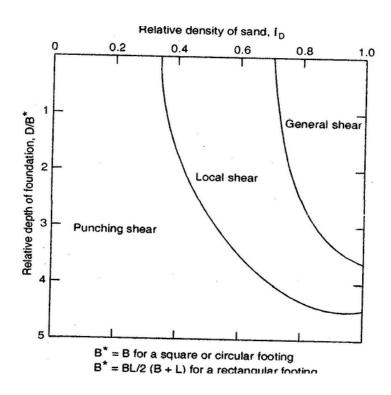


FIG. 9.3 EXPECTED MODES OF FAILURE OF FOOTINGS IN SAND (DE BEER, 1976)

TERZAGHI'SANALYSIS

Ananalysisoftheconditionofcompletebearingcapacityfailure,
usually termed general shear failure, can be made by assuming that
the soil behaves like an ideally plastic material. The concept was first
developed by
Prandtl,andlaterextendedbyTerzaghi,Meyerhofandothers.Terzaghi derived a

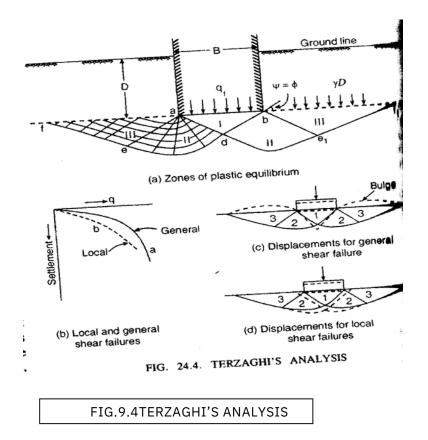
general bearing capacity equation from a modification of equations proposed by Prandtl. Fig. 9.4 shows a footing of width B, afto cause failure. The footing is and subjected to loading intensity shallow, i.e., the depth D of the footing is equal to or less than width B of the footing. Also, the footing is continuous i.e., it is a strip footing (L>5B).

The loaded soil fails along the composite surface fede1 f1. This regioncan be divided into five zones: zone I, twopairsofzone II and two pairs of zone III. When the base of the footing ab sinks into the ground,

zone

I (soil

wedgeabd)immediatelydeneaththefootingispreventedfromundergoing any lateralyield by the friction and adhesion between the soiland the base of



the footing. Thus, zone I remains in a state of elastic equilibrium, and it acts as if it were part of the footing. Its boundaries ab and da are assumed as plane surfaces, rising at an angle is the horizontal. Zone II

calledthezoneofradialshear,asthelinesthatconstituteonesetintheshear pattern radiate from the outer edge of the base of the footing. These radicallinesarestraightwhilethelinesoftheothersetarethelogarithmicspir als

with their centres located at the outeredges of the base of the footing. Zone III is called the zone of linear shear, and is identical with the for passive $\frac{450-0/2}{1000}$ with the Rankine state. The boundaries of zone III rise at horizontal. The failure zones are assumed not to extend above the horizontal

planethroughthebaseabofthefooting. This implies that the shear resistanc eof the soil above the horizontal plane through the base of the footing in the neglected, and the soil above this plane is replaced with the surcharge $q=\sigma=yD$

The application of the load intensity qfon the footing tends to

push the wedge of the soil abd into

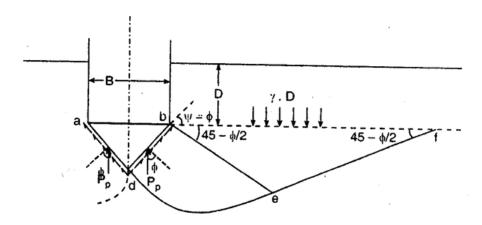


FIG. 24.5. FORCES ACTING TO RESTRAIN FAILURE.

the ground with lateral displacement of zones II and III, but this lateral

displace mention resisted by forces on the plane bd and da. These forces are:

(i) the resultant of the passive pressure PPand (ii) the cohesion c acting along the surface da and db. If it is assumed that surfaces db and da intersect the horizontal line atanangle ∅,the passive pressure acts vertically. At the instant of failure, the downward and upward forces on the edge adb of unit length must balance. The downward forces are (i) qfB and (ii) the weight

 $\begin{tabular}{l} 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & 4 & $$

Or

The resultant of passive earth pressure PPcan be divided

into three components:(i) $_{P}P_{\gamma}$ produced by weight of the shear zone $_{dbfe,}$ (ii) $_{PPc}$

producedbysoilcohesion, separately and then added to obtain the value of PP. Substituting these components in Eq. 24.9, we get.

$$qfB = 2(P_{P\gamma} \quad _{+P_{Pc} \quad +P_{Pq}} \) + B.ctan \varnothing - \stackrel{1}{\gamma} B2tan \varnothing$$

4

Or Let

and

 $2Ppc=B\times\sigma^{-}Nq$

Where $\sigma_{=}$ effectiveoverburdenpressureabovethebaseoffooting.

SubstitutinginEq.9.2 qf=cNc+
$$\sigma$$
-.Nq+0.5 γ BN γ (9.3)

If the water table is below the base of footing, $\sigma^- = \gamma D$ and hence

qf=cNc+
$$\gamma$$
DNq+0.5 γ BN γ

Hence

$$qnf = cNc + \sigma^-(Nq - 1) + 0.5\gamma BN\gamma$$

and

$$qs = [c.Nc + \sigma^{-}(Nq - 1) + 0.5\gamma BN\gamma] + \sigma^{-}$$

If the water table is below the base of footing, the above equations reduce to the forms :

$$qnf=cNc+\gamma D(Nq-1)+0.5\gamma BN\gamma$$

and

$$qs = \int_{F} [cNc + \gamma D(N_{q}1) + 0.5\gamma BN] \gamma + \gamma D$$

Forpurelycohesivesoil, the bearing capacity is given by

$$qs=cNc+\sigma^-Nq=5.7c+\sigma^-$$

Where $\sigma^{\text{-}} = \gamma D^{\text{i}}$ if the water table is below the base of the footing.

Eq. 9.3 is known as Terzaghi's general bearing capacity
Nyare the
equation for continuous footing. The parameters Nc, Ng and
dimensionless numbers, known are bearing capacity factors

of

depending only on the angle shearing resistance of the soil Terzaghiga vethe following expressions for the

bearingcapacityfactor:

$$Nq = \frac{\frac{a^2}{20}}{20}, Wherea = e(0.75\pi - \phi/2)tan\phi$$

$$N_c = (N_q 1)cot\phi$$
 and
$$N = \frac{tan \varnothing K_{py}}{2} - \frac{1}{cos^2\phi}$$

 $_{Kpy}$ -passiveearthpressurecoefficient,dependenton $_{\phi}$

Terzaghineverexplainverywellhowheobtain Kpyusedtocompute Nγ. He did, however, give a curve of φversus Nγand three specific values

ofNat ϕ =0,340and480ThevaluesoftheveeringcapacityfactorsNq,Nc andN $_{\gamma}$ canbeobtainedfromTable9.2.Thevaluesof Nfor ϕ of,340and480 are the original Terzaghi values which were used by Bowles to back compute Kpy.Thebackcompoundvaluesof Kpy.arealsogiveninTable9.2.

Generalandlocalshearfailure: Thetypeoffailureanalyzedabove iscalledthegeneralshearfailure, and the bearing capacity factor Nq, Nc and Ny correspond to the general shear failure. In such a failure, the soil properties are assumed to be such that a slight downward movement of footing develops fully plastic zones and the soil bulges out. In the case of fairly soft or loose and compressible soil, large deformations may occur below the footing before the failure zones are fully developed. Such a failure is called a local

failure. Which is associated with considerable vertical soil movement before soil bulging takes place. In the absence of analytical solution, Terzaghi

has proposed the following local shear- failure soil parameters.

$$Cm = c^{\frac{2}{3}}$$

$$\tan \varnothing_{n} = \tan \frac{2}{2} \varnothing$$

The bearing capacity factors are determined with respect to these

reducedparameters Cmand Øm. The bearing capacity factors corresponding to the local shear failure are indicated with dashes Nq'and Ny'and the bearing capacity equation (Eq. 9.3) reduces.

to
$$q = \varsigma.\bar{N} + \sigma^- N + Q.5\gamma BN'$$

It is difficult to define the limiting conditions for which general or local shear failure should be assumed at a given site. However, the following points may be used as a guide:

- (i) Stress strain test (c- Øsoil) : General shear failure at low strain, say<5%,whileforlocalshearfailure,stressstraincurvecontinuestoraiseat strains of 10 to 20%
- (ii) Angleofshearresistance:For ∅>360,generalshearfailure∅>360,localshear failure.
- (iii) Penetrationtest:N≥30:Generalshearfailure

N≤5:Localshearfailure

- (iv) Plateloadtest:Shapeoftheloadsettlementcurvedecideswhetherit is general shear failure or local shear failure.
- (v) DensityIndex: ID>70:Generalshearfailure

ID<20:Localshearfailure

For purely cohesive soil, local shear failure may be assumed to occur when the soil is soft to medium, with an unconfined compressive strength $qu \! \leq \! 100 \; KN/m^2$ or C $\! \leq \! K/m^2$.

FIG.9.2 TERZAGHI'SBEARINGCAPACITY FACTORS

	Ge	General shear failure			Local shear failure		
ф	N _c	Nq	N ₁	N _c '	N _q '	N _Y	
0	5.7*	1.0	0.0	5.7	1.0	0.0	
5	7.3	1.6	0.5	6.7	1.4	0.2	
10	9.6	2.7	1.2	8.0	1.9	0.5	
15	12.9	4.4	2.5	9.7	2.7	0.9	
20	17.7	7.4	5.0	11.8	3.9	1.7	
25	25.1	12.7	9.7	14.8	5.6	3.2	
30	37.2	22.5	19.7	19.0	8.3	5.7	
34	52.6	36.5	35.0	23.7	11.7	9.0	
35	57.8	41.4	42.4	25.2	12.6	10.1	
40	95.7	81.3	100.4	34.9	20.5	18.8	
45	172.3	173.3	297.5	51.2	35.1	37.7	
48	258.3	287.9	780.1	66.8	50.5	60.4	
50	347.5	415.1	1153.2	81.3	65.6	87.1	

AssumptionsinTerzaghi'sAnalysis:

- 1. The soil is homogenous and isotropic and its shear strength is represented by Comomb's equation.
- 2. The strip footing has a rough base, and the problem is essentially two dimensional.
- 3. The elastic zone has straight boundaries inclined at $= \emptyset$ to the horizontal and the plastic zones fully develop.
- 4. PPconsists ofthree components which can be calculatedseparatelyandaddedalthoughthecriticalsurfaceforthesecomp onentsarenot identical.
- 5. Failure zones do not extend above the base is neglected and the effectofsoil around the footing is considered equivalent to a surcharge = $\sigma = \gamma D$.

Limitations: (1) As the soil compresses, ⊘changes; slight downward movement of footing may not develop fully the plastic zones. (2) Error due to assumption 4 is small and on the safe side (3) Error due to assumption 5 increases with depth of foundation, and hence the theory is suitable for shallow foundation only.

SpecializationofTerzaghi's equations:

In order to take into account the shape of the footing (i.e. strip, round, square etc.), Terzaghi used only shape factors with cohesion (s c) and base (s y)terms. Taking into account these factors, Terzaghi's original equation (Eq.24.12) can be expressed as under:

$$qf=CNcSc+\sigma^{-}Nq+0.5\gamma BN\gamma S\gamma$$

The values of \mathbf{s}_{c} and sy are given below.

Shape	Strip	Round	Square	Rectangle
sc	1.0	1.3	1.3	1+0.B/L

SΥ	1.0	0.6	0.8	0.8or1-0.3
				B/L

Based on these values, Terzaghi gave the following semi-empirical equations for square, circular and rectangular footings:

Frictionalcohesivesoil $(c-\emptyset soil)$ (a)

Forcircularfooting:

$$qf=1.3cNc+\sigma^{-}.Nq+0.3\gamma BN\gamma$$

WhereB=diameterofthefootin

g. For square footing: $qf = 1.3 \text{ cNc} + \sigma^{-}.\text{Nq} + 0.4 \text{ }\gamma \text{BN}\gamma$

WhereB=width(orlengthof footing)

Cohesivesoil $(c=\emptyset;c>0)$ (b)

Forcircularfooting $qf=1.3cNc+\sigma^{-}=7.4+\sigma^{-}$

This considerably greater than the value of qf=5.7+σ for strip footing.

For rectangular and square footing:

$$qf=cNc(1+0.3) + \sigma_{L}^{B}$$

Non-cohesivesoil $(\emptyset=c;0>c)$ (c)

Forstripfooting: $qf=\sigma^-Nq+0.5\gamma BN\gamma$

Forrectangularandsquarefooting:

$$qf=\sigma^-Nq+0.4\gamma BN\gamma qf=$$

$$\sigma$$
-Nq+0.3 γ BN γ

I.S.CODEMETHODFORCOMPUTINGBEARING CAPACITY:

1.General: IS code (IS: 6403-1981), recommends a bearing capacity equation which is similar in nature to those given by Meyerhof and Brinch Hansen. The code recognizes, depending upon the deformations associated with the load and the extent of development of failure surface, three types of failures of soil support beneath the foundations, They are: (a) general shear failure; (b) local shear failure; and (c) Punching shear failure. The first twotypes of failures have already been described. The punching shear failure, occurs on soils of high compressibility. In such failure, there is vertical shear around the footing, perimeter and compression of soil immediately under the footing, with soil on the sides of the footing remaining practically un-involved.

Ø soil**2.B** dreng capacity equation for strip footing for cultimate net bearing capacity of strip footing is given by the following equations:

(i) Forthecaseofgeneralshearfailure:

(ii) Forthecaseoflocalshearfailure:

$$q_{nf} = \frac{2}{3} cNc + \sigma^{-}(Nq'-1) \beta \gamma N \overline{\gamma}$$

Where σ^- = effective surcharge at the baselevel of foundation.

Nc,Nq,Ny=Bearingcapacityfactors.

These factors are computed from the following sequations.

$$Nc=(Nq-1)cot\phi$$

$$N=tan(45+)e^{0\phi} - tan\phi \atop c \qquad and \qquad N=2(N+1)cot\phi$$

 $_{1)tan\phi}$(Vesic)

These factors are given in Table 9.3, for various values of ϕ at 10 interval. Original Table by IS : 6403 – 1981 give these values at 50 interval of

					,		
φ°	Nc	Nq	Ny	φ°	Nc	Nq	Nγ
0	5.14	1.00	0.00				
1	5.38	1.09	0.07	26	22.25	11.85	12.54
2	5.63	1.20	0.15	27	23.94	13.20	14.47
3.	5.90	1.31	0.24	28	25.80	14.72	16.72
4.	6.19	1.43	0.34	29	27.86	10.44	19.34
5.	6.49	1.57	0.45	30	30.14	18.40	22.40
6.	6.81	1.72	0.57	31	32.67	20.63	25.99
7.	7.16	1.88	0.71	32	35.49	23.18	30.22
8	7.53	2.06	0.86	33	38.64	26.09	35.19
9	7.92	2.25	1.03	. 34	42.16	29.44	41.06
10	8.35	2.47	1.22	35	46.12	33.30	48.03
11	8.80	2.71	1.44	36	50.59	37.75	56.31
12	9.28	2.97	1.69	37	55.63	42.92	66.19
13	9.81	3.26	1.97	38	61.35	48.93	78.03
14	10.37	3.59	2.29	39	67.37	55.96	92.25
15	10.98	3.94	2.65	40	75.31	64.20	109.41
16	11.63	4.34	3.06	41	83.86	73.90	130.22
17	12.34	4.77	3.53	42	93.71	85.38	155.55
18	13.10	5.26	4.07	43	105.11	99.02	186.54
19	13.93	5.80	4.68	44	118.37	115.31	224.64
20	14.83	6.40	5.39	45	133.88	134.88	271.76
21	15.82	7.07	6.20	46	152.10	158.51	330.35
22	16.88	7.82	7.13	47	173.64	187.21	403.67
23	18.05	8.66	8.20	48	199.26	222.31	496.01
24	19.32	9.60	9.44	49	229.93	265.51	613.16
25.	20.72	10.66	10.88	50	266.89	319.07	762.89

Forobtaining Nc,Nq,Nycorresponding tolocalshearfailure, calculate $\emptyset'=\tan-1(0.67\emptyset)$ and readNc,NqandNyfromTable24.9 corresponding to the value of \emptyset' instead of \emptyset .

3. Shapefactor,depthfactorandinclinationfactor:Theabove bearingcapacityequations,applicableforstripfooting,shallbemodified to take into account, the shape of the footing, inclination of loading, depth of embedment and effect of water table. The modified bearing capacity formulae are given below:

(i) Forgeneralshearfailureqnf=cNc.sc.dc.ic+σ⁻(Nq-1)sq.dq.iqByNy.sy.dy.iyw'

(ii) Forlocalshearfailure

$$q = \frac{2}{n_f} - \frac{1}{3} cN_c sc. dc. ic + \sigma^-(N_q l) s. dq. iq + B_y y. N\gamma' s \gamma d\gamma i \gamma W'$$

The shape factors sc, sq and sy are given in table

24.10. The depth factors are given as under:

$$d=1+0.2 \stackrel{D}{.} \sqrt{N} \qquad - \qquad \qquad \\ c \qquad B \qquad \varnothing$$

$$d=d=1+0.1 \stackrel{D}{\sqrt{N}} \text{for} \varnothing \ge 100 \qquad \text{where N=tan2} (450+\varnothing/2)$$

$$q \qquad \gamma \qquad B \qquad \varnothing$$

Table 9.4 shape factors (IS: 6403 - 1981)

Shapeofbase	Shapefactors			
	SC	sq	sy	
1.Continuou sstrip	1.0	1.0	1.0	
2.Rectangle 3 Square	$(1+0.2) \frac{B}{L}$	(1+0.2) LB	(1-0.4) E	
3.Square 4.Circle	1.3	1.2	0.8	
1.011.010	1.3	1.2	0.6	

Note.Incaseofcircularfooting,useBasthe diameter.

The depth factors are to be applied only when the back filling is done with proper compaction. The inclination factors are given as under:

$$i = i = (1-)^{\infty} \frac{1}{90}^{\infty}$$
 and $i = (1-\infty \frac{2}{90})^{\infty}$ $\infty = inclination of the load to the vertical, in degrees,$

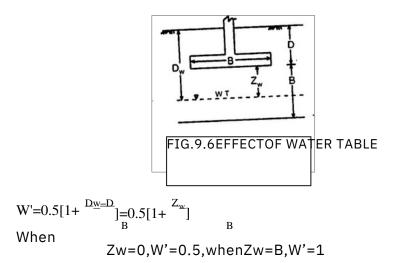
Where

4.Effect of water table: The effect of water table is taken into account in the formofacorrectionfactorW'appliedtothe'wedgeterm'inEqs.24.41and 24.42.ThevalueofW'maybechosenasindicatedbelow:

(a)If the water table is likely to permanently remain at or below a depth of(D+B) beneath the ground level surrounding the footing, then W'=1 (b)If the water table is located at a depth D or likely to rise to the base offooting or above, then the value of W' shall be taken as 0.5.

(c)Ifthe water tableislikely to permanentlygetlocatedatdepth D<D<

(D+B), the W' be obtained by linear interpolation. Thus, for the intermediate case, we get the following expression for W'.



The validity of the above equation is within the range D < Dw < (D+B). If we compare the above expression with Eq. 24.36, it is clear that W'is same as factor Rw.2

 $It may be noted that if the water table rises above the base of footing, \\ W' will remain at its minimum value of 0.5, but \\ \sigma^-(effective overburden pressure) will be computed of the basis of total unit weight of the portion of soil above the water table and submerged unit weight for the portion below the water table.$

 $5. Cohesionless\ soils\ (c=0): for\ cohesionless\ soils,\ having\ c=0,$ $Indian\ standard\ code\ recommends\ that\ the\ bearing\ capacity\ be$ $calculated \qquad \qquad (a)$ $basedonrelative density or (b) basedon standard penetration resistance value, and <math display="block">(c) basedon static conepenetration\ test.$

(a)Based on relative density: In this method, bearing capacity may be calculated by, together with relevant shear strength parameter. In these formulae, c is taken equal to zero. The relative density given in Table 9.5 is used as a guide to determine the method of analysis.

TABLE9.5METHODOFANALYSISBASEDONRELATIVE DENSITY

Relativedensity (DensityIndex)	VoidsRatio	Condition	Methodof analysis
(DensityIndex) 1. Greaterthan Le	ssthan0.5	Dense	Generalshear
70%		Loose	Local shear (as
2.Lessthan20% G	reater		wellaspunching shear)
	than 0.75		Interpolate
3.20%to70%	0.55to0.75	Medium	between(1)and (2)

(b) Basedonstandardpenetrationresistancevalue:Thestandard penetration resistance (24.14) is determined at a number of selected points at intervals of 75 cm in the vertical direction or change of strata if it takes place earlier and the average value beneath each point is determined between the level of base of the footing and the depth equal to 1.5 to 2 times the width of foundation. In computing the value, any individual value more than 50 percent of the average calculate shall be neglected and average recalculated (the values for all loose seams shall however be included).

Knowing the value of N, the value of \emptyset is read from fig. The ultimate net bearing capacity is then calculated from the formula:

qnf=
$$\sigma^{-}(N_{q}1)S$$
 + $_{q}d$ + $_{i_{q}}+_{q}BN_{2}$.s γ . $_{q}d\gamma$. $_{i}$.W' $_{\gamma}$

Where the shape factors, depth factors and inclination factors are determined as described earlier, and the bearing capacity factors Nq and Nyar etaken from Table 9.2.

(c)Basedonstateconepenetrationtest:Thestaticconepointresistanceqc isdeterminedasperIS:4968(Part–III)–1976atanumberofselected points at intervals of 10 to 15 cm. The observed values are corrected for the dead weight of sounding rods. Then the average value at each one of the locationisdeterminedbetweenthelevelofthebaseofthefootingandthe depthequalto 1 to 2 times the width of the footing. The determined for each one of the location and the minimum of the average value is used in the design.

The net ultimate bearingcapacityisshallowstripfooting on cohesionless soil deposit is then determined from Fig.

6. Cohesivesoils: $(\emptyset) = 0$: The net ultimate bearing capacity immediately after construction on fairly saturated homogenous cohesive soils can be calculated from the expression:

Where Nc=5.14 (for
$$\varnothing$$
=0)

Thevalueofcisobtainedfromunconfinedcompressivestrength test. Alternatively, cohesion c may be determined from the static cone point resistance qc using the empirical relationship given in Table.

Table 9.6 (Relationship between q cand c

SoilType	Point Resistance Value Q _c (kgf/cm²)	Range of undrained cohesion (kgf/cm²)
1.Normallyconsolidated clays	qc< 20	4ctoc4- 18 15
2.Overconsolidatedclays	q≥ 20	4ctoc4- 26 22

Note.1Kgf/Cm2=100kN/m2

Example 9.1. A square footing 2.5 m by 2.5 m is built in a homogenous bed ofsand ofunitweight 20 kN/m3 andhavinganangle ofshearing resistance of 360. The depth of the base of footing is 1.5 m below the ground

surface. Calculate the safe load that can be carried by a footing with a factor of safety of 3 against complete shear failure. Use Terzaghi's analysis.

Solution . Given : B = 2.5 m; D = 1.5m ; γ =20 kN / m3. Since the soil is dense,and \varnothing =360, the footingislikely to failby general shear failure.

From table the values of bearing capacity

factors are: Nc=65.4,Nq=49.4andNy=54.0

Also,
$$\sigma = \gamma D$$

Since $c=0,qf=\gamma DNq+0.4\gamma BN\gamma$

Or
$$qnf=\gamma D(Nq-1)+0.4\gamma BN\gamma=20\times1.5(49.4-1)+0.4\times20\times2.5\times54.0$$

874kN/m2

Maximumsafeload=B2xq s=(2.5)£874=5462.5kN

Example 9.2: What will be the maximum safe load for example 9.1 if the soilis loose sand of unit weight 16 kN/m3and the angle of shearing resistance is 250.

Solution : Since the soil is loose and \emptyset =280, the footing is likely to fail by local shear failure. From Table, for \emptyset =250.

Nq'=5.6andNy'=3.2
$$qnf = \gamma D(Nq-1) + 0.4\gamma BN\gamma' = 16 \times 1.5(5.6-1) + 0.4 \times 16 \times 2.5 \times 3.2$$
$$= 110.4 + 51.2 = 161.6kN/m^{-2}$$
$$q = \frac{q_{nf}}{s} + \gamma D = \frac{161.8}{3} + \frac{(16 \times 1.5)}{3} = 77.87kN/m^{-2}$$

m Safeload=B2xqs=(2.5)(77.87)=846.7kN.

Example :9.3 A strip footing, 1 m wide at its base is located at a depth of 0.8 m below the ground surface. The properties of the foundation soil are : y=15

kN/m3,c=30kN/m2andØ=200.Determinethesafebearingcapacity,using a factor of safety of 3. Use Terzaghi's analysis. Assmue that the soil fails by local shear.

Solution: The bearing capacity is given by, taking

$$q = {^{2}_{c}N + \gamma DN + 0.5\gamma BN'}$$

$$f \qquad 3 \qquad c \qquad q \qquad \gamma$$

 $For_{\emptyset=20}^{\circ}$, the bearing capacity factors taken from Tableare:

$$N_{c}=11.8; N=3.9; N=1.7$$

$$q_{f}=(1.8) \times 11.8 + (18 \times 0.8 \times .9) + (0.5 \times 18 \times 1 \times 1.7)$$

$$=236 + 56.2 + 15.3 = 307.5 \text{kN/m2}$$

$$q_{f}=q_{f}-\gamma D=307.5 - 18 \times 0.8 = 293.1 \text{kN/m}^{2}$$

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MACHINEFOUNDATION

IntroductiontoSoilDynamics:

Soildynamicsisdefinedasthatconstituentpartofsoilmechanics whichdealswithsoilunderdynamicconditions. Its tudies the effect of forces on soil in any way associated with causing motions in soil as well as with the mutual dynamic interaction of the foundation and soil (Jumikis, 1969). Most of the motions encountered in soil dynamics plane work are those of vibration,

linearmotion, motion brought about by impacts hockelastic waves; and seismic action of geophysical forces.

Thedesignoffoundationsofturbines, motors, generators
compressors, forge hammers and other machines, having a rhythmicapplication of unbalanced forces require special knowledge of theory
of harmonicvibrations. Inertial forces of rotating elements of machines contribute, besides their static loads, additional dynamic loads. The machinery vibration influences adversely the foundation supporting soil by densifying it which may in turn, cause differential settlement of

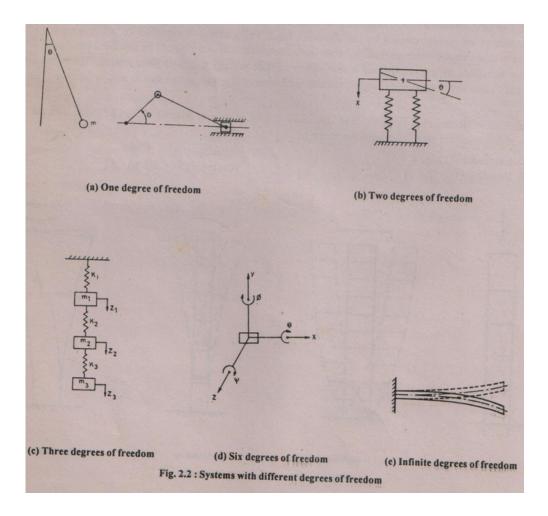
Termsassociated with soil dynamics

Vibrations:-Ifthemotionofthebodyisoscillatoryincharacter, it is called vibrations.

DegreesofFreedom:-

soil and foundation.

Thenumberofindependentwhicharerequiredtodefinetheposition of a system during vibration, is called degrees of freedom (Fig.).



Periodic Motion:- If motion repeats itself at regular intervals of time, it is called periodic motion.

FreeVibration:-

Ifasystemvibrateswithoutanexternalforce, then it is said to undergo free vibrations. Such vibrations can be caused by setting the system in motion initially and allowing it to move freely afterwards.

Natural Frequency:- This is the property of the system and corresponds to the number of free oscillations made by the system in unit time.

Forced Vibrations:- Vibrations that are developed by externally applied forces are called forced vibrations. These vibrations occurat thefrequency of the externally applied exciting force.

Forcing Frequency:- This refers to the periodicity of the external forces which acts on the system during forced vibration. This is also termed as operating frequency.

Frequency Ratio:- The ratio of the forcing frequency and natural frequency of the system is referred as frequency ratio.

AmplitudeofMotion:-

Themaximum displacement of a vibrating body from the mean position is amplitude of motion.

TimePeriod:-Timetakentocompleteonecycleofvibrationisknownastime period.

Resonance:- A system having ndegrees of freedom has nnatural

thequencies. If

frequencyofexcitationcoincideswithanyoneofthenaturalfrequenciesofthesy stem, the condition of resonance occurs. The amplitudes of motion are very excessive at resonance. Damping:- All vibration system offer resistance to motion due to their

own inherent properties. This resistance is called damping force and it depends on the condition of vibration, material and type of the system. If the force of damping is constant, it is termed Coulomb damping. If the damping force is proportional to the velocity, it is termed viscous damping. If the damping in a system isfree from its material property and is contributed by the geometry of the system, it is called geometrical or radiation damping.

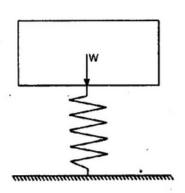
Principal Modes of Vibration:- In a principal mode, each point in the system vibrates with the same frequency. A system with n degrees of freedom possess n principal modes with n natural frequencies.

NormalModeof Vibration:- If theamplitudeofapointofthesystemvibrating inoneof the principal modes is made equal to unity, the motion is then called the normal mode of vibration.

Themassspringsystem:

Insoil dynamicsproblems, the analysis may be conveniently carried out by a single equivalent mass supported by a perfectly elastic system – the soil being replaced by the spring Fig. shows mass-spring system (or spring mass system), in which he weight . W-mg may be associated with the weight of the vibrating vibrator or foundations. The elastic spring

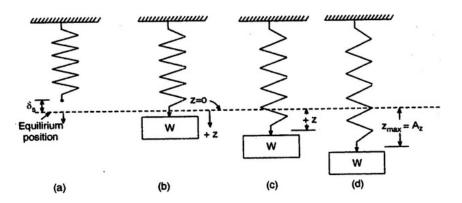
represents the real the soilsupport.Suchasystemhassixdegreesoffreedom, and has thus six natural frequencies.



Free-Vibrations. Let the mass spring system be set to vibration by an external force which is the removed. The system will continue to oscillate indefinitely with the same frequency and amplitude if external force or internal frictionisabsent. The time for one complete oscillation of the mass is called

the free period and distance up or down from the equilibrium position is calledthe amplitude.

Fig.showsasimplespringwithaspringconstantkkg/m.Whena weight W is attached to it (without any vibrations), it extends by an amount ðs[Fig. 28.2 (b)]



If the spring mass system is pulled down, by an external force, by a maximum distance Zmaxor Az(called the amplitude), and then released, the whole system vibrates with a certain frequency.Letz be the displacement of the mass at any instant, with respect to the equilibrium position, the force Fs is the spring () is then given by

$$F_s=k(\delta_s+z)=k\delta_{\frac{1}{2}}kz=W+kz$$

Theforceacts in the opposite direction to the motion at any instant. The gravity force W acts downward. Hence when the motion is downward, the netdownward force is equal to $W^{\downarrow}-(W+kz)T$. This must

beequalto mass ×accelertion.Hence,we get

$$W-(W+kz) = \frac{W}{g} \frac{d2z}{dt^2}$$

Or
$$-\frac{2}{\frac{1}{dt}z}+kz=0$$

Whichisusuallywritten as mz+kz=0

Wherem=massofthevibratingbody= W/g

z =acceleration

Eq. is called the equation of motion, which is similar to the following standard equation of motion :

$$z + \omega n2z = 0$$

Where ω_{r} -natural frequency of the system.

ComparingEqs.,

 $\omega_{n2} = \frac{k}{m}$ $\omega_{m2} = \sqrt{\frac{k}{m}} \sqrt{\frac{kg}{m}} rad/\frac{sec}{w}$

 $If \emph{\textit{f}} n is the natural frequency of the system in cycles per second, we have$

 $\frac{-1}{2\pi\sqrt{W}}$ cycles/sec

Vibratingspring-masssystemwithdamping .

If the spring mass system be provided with dash- pot, having c as the damping factor and z is the velocity of the vibration system at any instant, the force in the dash-pot, opposite the motion, will be equation to cz.

Hencetheequationofthemotionwill be

$$W \downarrow -(W+kz) T=cz T=mz mz$$

+ cz+kz=0

Comingthis with the standard equation for damping vibrations:

$$z$$
+2nz+ ω $z=0$

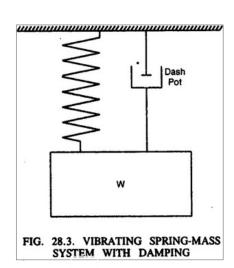
Weget

$$n=^{c}\frac{}{2m}$$

Or

$$\omega_n = \sqrt{\frac{k}{m}}$$

Eq.isthestandarddifferentialequationwhichcanbesolvedby putting



z=C'e.t...(i) $z'=C'\lambda e\lambda.t.....(ii)$ $z'=C'\lambda 2.e\lambda.t....(iii)$

PuttingtheseinEq., we get

$$m C' \lambda^{2e.t} + c C' e^{t} k C' e \lambda. t = 0$$

$$\lambda = -\frac{c}{2m} \pm \sqrt{()^{c} \frac{1}{2m} - (\frac{k}{m})} = -n \sqrt{n} 2 \qquad -\omega n 2$$

$$\lambda^{1} = -n + \sqrt{n} 2 - \omega n 2 \qquad \text{and} \qquad \lambda_{2} = -n + \sqrt{n} \frac{2}{m} = 0$$

Hence

Three cases may arise from Eq.

: Case(i) Real, if $n2>\omega n2$

Case(ii)Zero,if n2=on2

Case(iii)Imaginaryorcomplexif $n2 < \omega n2$

Case(ii)Gives a value of $\lambda = -n = \frac{c}{m} = \sqrt{\frac{k}{m}}$

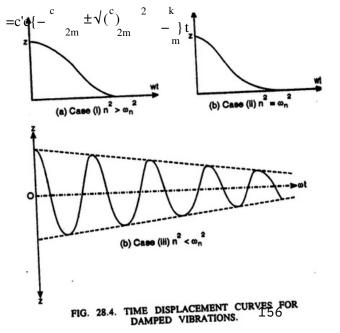
Eq. for case (ii) to $e\lambda.t=0$, indicating that for this condition there will be no oscillation, but only a rapid return back to the equilibrium position of the mass [Fig. 28.4 (b)]. The value of c for this condition is called critical damping cc.

$$Cc=2m\sqrt{\frac{k}{m}}=2\sqrt{mk}$$

Forcase,(i),theradicalisreal $(n2>\omega n2)$,and $c\geq 2\sqrt{mk}$.

Hencefrom(i), $z=C'e \lambda .t$

Eq. shows that z is not a periodic function of time. Therefore, the motion, when $n2 - \omega n2 > 0$ is a vibration, because it can only approach the equilibrium position at $t \to \infty$. However, the viscous resistance is so pronounced that the weight set in motion from its equilibrium does not vibrate but creeps gradually back to the equilibrium position at time



infinity For case (iii) when n2> $\omega n2$,

Let_{λ 1}and λ 2bethetworootsofEq.:

 $\lambda 1=-n+\omega di$

Now Eq.gives two particular solutions of Eq.Also, the sum of difference of these two solutions multiplied by any constant is also a solution:

$$mz1 = {}^{G}_{1}(e\lambda 1.t.e\lambda^{2.t})$$

$$z2$$

$$= {}^{G}_{2}(e^{1.t}-e\lambda^{2.t})$$
And

WhereC1andC2areconstants.

Substituting the values of $\inf_{\lambda} \lambda 2$ from Eq. and simplifying, we get

$$z_1=C_1e^{-nt}sin\omega dt$$
 and $z_2-Ce_2-nt cos\omega dt$

Summation of $z_{1+z_{2}=z_{1}}$ renders the general solution of Eq. in the following form.

$$z=e^{-nt}[C1\sin\omega dt+C2\cos\omega dt]$$

The quantity in the bracketpresentsthesimple harmonic motion of the case of vibration without damping while e-nt is the damping term fig. shows the timedisplacementcurveforthiscase. The period Tofthedamping vibration is given by

$$T = \omega = d \sqrt{\frac{2\pi}{2-n}}$$

The term $_{\omega d}$ is called the frequency of damped vibrations.

$$\omega_{\overline{d}} \sqrt{\omega_2 - n_2} = \sqrt{\frac{k}{m}} \frac{c_2}{4m_2}$$

Or

$$\omega d = \sqrt{\frac{k}{m}} \sqrt{1 - \frac{c^2 - \omega n}{4km}} \sqrt{1 - (\frac{c^2}{Cc})}$$

Forcedvibrations:

Forced vibrations of a system are generated and sustained by the application of an external periodic movement of the foundation of the system.

Forcedvibrationsconstitutethemostimportanttypeofvibrationin machine

foundation design. We shall consider the case of forced vibrations withdamping. Generally, for oscillating machinery (where the machinery vibrates becauseanunbalancedrationalforceexists),theforcecanbeexpressed as a sine or cosine function, such as F0 sin ωt. The equation of motion for such a case may be written as:

or

$$z+$$
 $\frac{c}{-z}$ $\frac{k}{z} = \frac{F_0}{m}$ sinwt

The solution of the above equation may be assumed in the following forms :

Bysuccessive differentiation, we obtain

$$z=$$
"- $A\omega 2\cos\omega t$ - $B\omega 2Sin\omega t$

Substitutinginto(a), we get.

$$(-A\omega 2\cos\omega t - B\omega 2\sin\omega t) + (-A\omega \sin\omega t + B\omega \cos\omega t) + (A\cos\omega t)$$

$$= \frac{m}{-\sin\omega t}$$

$$= \frac{F0}{-\sin\omega t}$$

$$= \sin\omega t$$

Equating the co-efficient of since to both sides,

$$-B\omega^2 - A\omega + B= F_0 \over m \qquad m$$

Similarly, equating the coefficients of cost of toboth sides,

$$-A\omega^2 - B\omega + A=0$$
 m

SolvingEqs.28.22(a)and(b)forcoefficientsA&B,we get

$$A = \frac{F0 c\omega}{(k-m\omega^2)^2 + (c\omega)^2}$$

$$B = -\frac{F0 - m\omega^2}{(k-m\omega^2)^2 + (c\omega)^2}$$

SubstitutingtheseinEq.wegetthesolutioninthe form

F0-c
$$\omega$$
 F(Km2 θ)sin ω t

$$\underline{z=-} \frac{\cos\omega t + (\cos\omega)2 + (k-m\omega^2)2}{(\cos\omega)2 + (k-m\omega^2)2}$$

The equation represents the components due to force dvibrations with the period of $T=\frac{2\pi}{\Box}$ he frequency of vibrations (in cycles per second) is given by

$$f = \frac{\omega}{2\pi}$$

Thefrequencyofvibration, as defined earlier, is given by

$$\omega = \sqrt{\frac{k}{m}}$$
 radians/sec

and

$$\int_{n}^{\infty} \frac{\mathbf{w}\underline{\mathbf{n}} = 1}{2\pi} \frac{\sqrt{\mathbf{k}}}{2\pi} \underline{\mathbf{m}}$$

Substituting in
$$_{-F0 c\omega}$$

$$=z \sin \emptyset \qquad \qquad _{-F \ 0(k-m\omega)}$$
 $(c\omega)^{2+(k-m\omega)^2} = z \sin \emptyset \qquad \qquad (c\omega)^{2+(k-m\omega)^2} = z \cos \emptyset$
and $(c\omega)^{2+(k-m\omega)^2} = z \cos \emptyset$

z₂cosØ

Weget
$$z=z2(\sin\varnothing\cos\omega t+\cos\varnothing\sin\omega t)=z2\sin(\omega t+$$

 \emptyset)

Where the angle Øis termed as the phase represent a pair of vectors which must be added to obtain the displacement, the solution for the displacement due to the forced vibrations of Eq. 28.24 becomes.

$$z = \sqrt{A2 + B2}F0\sin(\omega t + \emptyset)$$

SubstitutingthevaluesofAandB, and noting from Eq. 28.12 that

$$c=2\sqrt{mk} = \frac{2k}{\sqrt{m}} \sqrt{\frac{m^{2k}}{2}} - \frac{1}{\sqrt{m}} \text{ or } k = \frac{\omega_{n}\epsilon}{2}$$
We get
$$z = \frac{E0}{\sqrt{\frac{2c\omega^{2}}{cc\omega^{n}}} + \int 1 - (\frac{1}{\omega^{n}}) \int 1} \sin(\omega t + \omega)$$
Or
$$z = \frac{E0}{\sqrt{\frac{cf^{2}}{c}} + \frac{\sin(\omega t + \omega)}{cc\omega^{n}}}$$

The maximum deflection z_{max} is thus given by

$$zmax=Az=\frac{\underbrace{\sqrt{2c}_{cc} \cdot f_{h}}^{E0}}{\sqrt{2c}_{cc} \cdot f_{h}}^{2} + [1 - (\underbrace{f}_{fn})^{22}_{fn}]$$

$$= \underbrace{\delta}_{s} = static \text{ deflectionofs} \quad P \text{ ring}$$

But

m
$$\frac{Az \times ma}{\delta s} = \delta = s \qquad \frac{1}{\sqrt{2 - (f - f)^2 / (f - f)^2}}$$

Where

 $Az=z_{ma}x=$ maximumdynamicdeflectionofthesystem. Putting $Az=max \ \mu = magnification factor or dynamic$

amplification factor amplification factor

$$\frac{\omega}{\omega} = \frac{f}{\omega}$$

$$\omega = \frac{f}{\omega}$$

$$\omega = \frac{f}{\omega}$$

$$\omega = \frac{f}{\omega}$$

$$\omega = \frac{c}{\omega} = \xi = damping ratio, we get$$

$$0$$

$$1$$

$$\mu = \frac{\sqrt{(1-r^2)^2 + 4\xi^2 r^2}}{\sqrt{(1-r^2)^2 + 4\xi^2 r^2}}$$

Fig.28.5showsaplotbetweenthemagnification factor and the frequency ratio $r(=\frac{f}{f^n}=\frac{o}{o^n})$ for various of damping ratio ξ .

From Fig., it is observed that magnification factors uddenly shoot sup for the values of r between 06. To 1.5 At r = 1, resonance occurs for an undamped conditions, the magnification factor (and hence the amplitude)

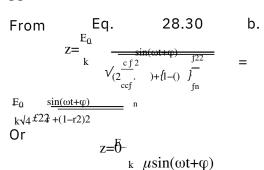
maximumatr<1.Thus,thesecurvesshowtheeffectofdampingonshifting thefrequencyformaximumamplificationawayfromthenatural foundation frequency.Theaimofthedesignershouldbesuchthatthefrequencyratio

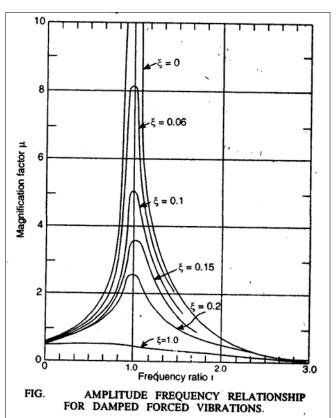
iseitherlessthan0.6ormore than1.5However,thefrequency fofther machine is always constant, and a foundation engineer has to manipulate the natural frequency for the machine foundation systemby suitably proportioning it.

Transmittedforce (FT)

In a damped forced vibratory system, the support is derived from the foundation by way of transmittinga force(FT) to foundation. transmittedforce(FT)canbe expressedas

FT





Where

$$\mu = \frac{1}{\sqrt{4£2r2+(1-r2)2}} =$$

magnificationfactor

SubstitutingthisvalueofzinEq,we get

$$F = c[(\mu)\sin(\omega t + \varphi)] + k(\mu)\sin(\omega t + \varphi)$$

$$T \qquad dt \qquad k \qquad k$$
or
$$F = c\theta\mu \cdot \cos(\omega t + \varphi)\omega + k(\theta)\sin(\omega t + \varphi)$$

$$T \qquad k \qquad k$$

$$= (c\theta\mu)\sqrt{c2.\varpi^2 + k^2} \qquad [\cos(\omega - t^- + -\varphi^- - -\beta^-)] \quad \text{where } \beta = FT$$

$$\tan_{-1}k \qquad c\omega$$

Hencethemagnitudeoftheforce _FTisgivenby

$$/Fl = (\underbrace{F_{\mu}}_{T}) \underbrace{\sqrt{2C} \omega = \underbrace{F_{\nu}}_{t} + \mu}_{k} \underbrace{\frac{c^{2} \delta_{0}}{0}}_{0} \underbrace{\frac{c^{2} \delta_{0}}{k^{2}}}_{k}$$
But $k = \underbrace{\frac{\omega_{0}}{c} + \frac{c^{2} \delta_{0}}{c}}_{2}$

Hence, from 3, $F = F_{\mu} \sqrt{1 + 4}$ $F = F_{\mu} \sqrt{1 + 4}$ $F = F_{\mu} \sqrt{1 + 4}$ $F = F_{\mu} \sqrt{1 + 4}$

$$T = 0$$
 $\frac{}{\omega 2nC2c}$ $T = 0$

Alsoratio
$$ET = T = \mu \sqrt{1 + 4r \xi 2} = Forcetransmissibility$$

Naturalfrequencyoffoundationsoilsystem:

In the previous discussion, we have used the term *m* as the mass of the vibration system. This includes the mass of a certain volume soil co-vibration with the system. The mass of co-vibrating soil is called the apparent soil mass, participating in the vibrations.

Thus, m=mv+ms

Wheremv=massofthevibrator

ms=apparentsoilmass(massoftheco-vibrating soil)

$$\omega_{n=} \sqrt{\frac{k}{m^{v}+m^{s}}} = \sqrt{\frac{kg}{w_{v+ws}}}$$

Or

$$f = 1 \frac{1}{m} \frac{k}{mv + ms} = 1 \sqrt{\frac{kg}{mv + ws}}$$

Where

Wv=Weightofthevibrator,and

Ws=Weightoftheapparentsoil mass.

Unfortunately, the size of the co-vibrating body of soil cannot be determined exactly as yetbecause it depends on frequency and is influencedby the size of the base area of the vibrator (foundation) and by the elastic properties of the soil (spacing).

We shall consider here three methods of determining the natural frequency of foundation soil system: (1) Barken's method (2) BalakrishnaRao's, (3) Pauw's method.

BARKEN'METHOD

Barken suggested the following equation for the natural frequency of system.

WhereCu=Co-efficientofelasticuniformcompressionof soil

A = contact area of foundation with soil m = mass of machine plus foundation

Theamplitudeofdisplacementisgiven by

Az=
$$\frac{F}{m\omega n^2(1-r^2)}$$

Where $A_{Z=Z}$ max=maximum displacement

$$F^{\underline{0}}$$
 exciting force: r=frequency ratio $\stackrel{\omega}{=}$ $\stackrel{\omega}{=}$

The above formulae for natural frequency takes no account of the mass of soil vibrating with the foundations.

Barkengavethefollowingequationfortheco-efficientofelastic uniform compression of soil, obtained from the solution of theory of elasticity problem concerning the distribution of normal stresses under the base contact area of a rigid plate:

$$\begin{array}{ccc} & \underline{e} & \underline{1} \\ \text{Cu=1.13} & \underline{1_7} \mu^2 & \sqrt{\text{A}} \\ \text{WhereE=Young'smodulusofsoil; } & \underline{\mu} \text{Poisson's ratio} \end{array}$$

Thus, Cu depends not only on elastic constants E and μ changes in inverse proportion to the square root of the base area of the foundation :

$$\begin{array}{c}
c u 2 & A 1 \\
c u 1 = \sqrt{A2}
\end{array}$$

TablegivestherecommendedvalueofC uforA=10m2forvarioussoils.

1	TABLE RECOMMENDED DESIGN VALUES OF THE CO-EFFICIENT OF ELASTIC UNIFORM COMPRESSION C_u (BARKEN, 1962)					
Soil group category	Soil group	Permissible load on soil under action of static load only (kg/cm²)	Coefficient of elastic uniform compression C _u (kg/m ²)			
I	Weak soils (clays and silty clays with sand, in a plastic state, clayey, and silty sands; also soils of categories II and III with laminae of organic silt and of peat)	up to 1.5	up to 3			
11	Soil of medium strength (clays and silty clays with sand, close to the plastic limit; sand)		3—5			
III	Strong soils (clays and silty clays with sands of hard consistency; gravels and gravelly sand, loess and loessial soils)	3.5—5	5—10			
IV	Rocks	Greater than 5	Greater than 10			

GENERALPRINCIPLESOFMACHINEFOUNDATION DESIGN

General:-

Formachinefoundationswhicharesubjectedtodynamicloadsinadditio nstostatic loads, the conventional considerations of bearing capacity and allowable settlement are insufficienttoensureasafedesign.Ingeneral,afoundationweighsseveraltime sasmuchas machine (Cozens, 1938; Rausch, 1959). Also the dynamic loads produced by the moving parts of the machine are small in comparison to the static weight of the machine and foundation. But the dynamic load acts respectively on the foundation soil system over long periods of time. Therefore, it is necessary that the soil behaviour be elastic under the vibration levels produced by the machine, otherwise **de¢**brmation will increase cycleofloadingandexcessivesettlementmayoccur. The most important param etersofthe design of a machine foundation are: (i) natural frequency of the machine-foundation-soil system; and (ii) amplitude of motion of the machine at its operating frequency. TypesofMachineandFoundations:-

There are various types of machines that generate different periodic forces. The main categories are:

Reciprocating Machines: These includes steam, diesel and gas engines, compressor and pumps. The basic mechanism of a reciprocating machine consists of a piston that moves within a cylinder, a connecting rod, a piston rod and a crank. The crank rotates with a constant angular velocity. Figure 10.1 shows the outline of a typical Gangsaw in which the out of balances forces may lead to vibration problems.

The operating speeds of reciprocating machines are usually smaller than 1000rpm. Large reciprocating engines, compressors and blowers generally operate at frequencies ranging within 50-250rpm.

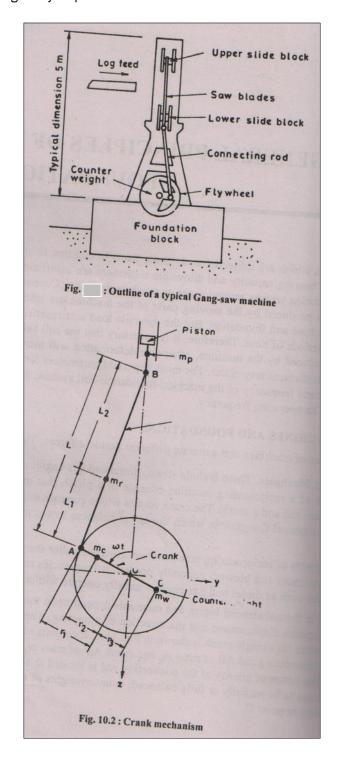
Reciprocating engines such as diesel and gas engines operate within 300-1000rpm.

Themagnitude of the unbalanced forces and moments depend upon then umber of cylinder in the machine, their size, piston displacement and the direction of mounting. The

mechanismdevelopingoutofbalanceinertiaforcesforasinglecrankisshownin Fig.10.2.It

consistsofapistonofmassmpmovingwithinacylinder,aconnectingrodABofma ssmrand crank AO of mass mcwhich rotatesabout point O at a frequency w. The centre of gravity of theconnectingrodislocatedatadistanceL1 frompointA.Iftherotatingmassesareto be

partially or fully balanced, counterweights of mass mwmay be located with their centre of gravity at point C.



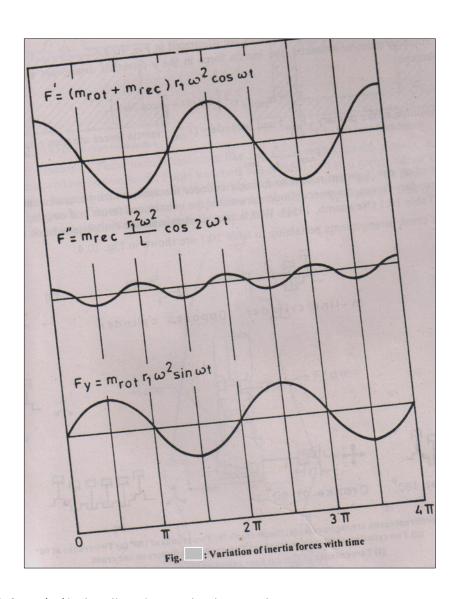
In order to simply the analysis of the motion of the connecting rod, the mass mr is replaced by two equivalent masses; one rotating with the crankpin A, the other translating

with the wrist pin B. The inertia forces can then be expressed in terms of the total rotating mass (mrot) and the total reciprocating mass (mrec). The total rotaing mass is assumed to be concentrated at the crank pin A.

$$m_{rot} = \frac{r_2}{m} + \frac{1}{2m} - \frac{5}{3m}$$

$$m - \frac{1}{r_1} = \frac{r_2}{r_1} = \frac{1}{r_1} = \frac{1}{m}$$

$$m_{rec} = ma$$
 $+\frac{L}{L}m$



Theinertiaforce(Fz)inthezdirectionmaybeshownto be

Fz=(m
$$_{\text{rot}} + m_{\text{rec}}$$
)rw2 coswt + m_{re} $\frac{r_1^2}{L}$ w2cos2wt

which has aprimarycomponent (F)actingatthefrequencyof rotation, and as econdary component (F") acting at twice the rotation frequency.

Andintheydirection

ThetimevariationsoftheseinertiaforcesareillustratedinFig.10.3

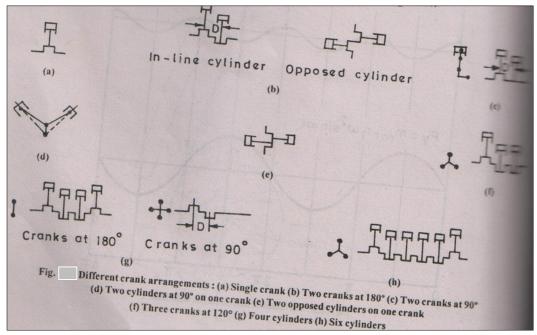
If the rotating mass is balanced, the inertia force in the y direction disappears and that in the z direction becomes

$$F=m rw(co2swt + cos2zwt)$$
_z
_{rec1}
_L

Theamplitudeoftheprimary(F'max)andsecondary(F"max)inertiaforc esarethen related as follows

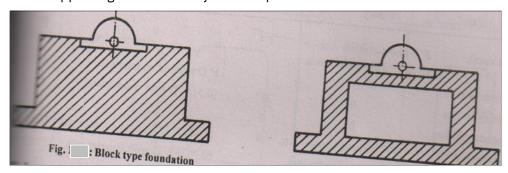
The preceding development relates to a single cylinder machine, which possess unbalanced primary and secondary forces. As more cylinders are added the unbalanced forces and couples are modified as shown in Table 10.1 (Newcomb, 1951). With a six cylinders machine complete balance is achieved.

Differentcrankarrangementspertainingtotableareshownin Fig.

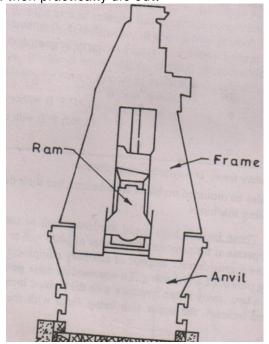


Reciprocating machines are very frequently encounteredin practice.
Usually the following two types of foundations are used for such machines.

- (a) Blocktypefoundationconsistingofapedestalofconcreteonwhichthema chine rests.
- (b)Box orCaissontype foundationconsistinga hollowconcrete blocksupporting the machinery on its top.



Impact Machines:- These include machines like forging hammer, punch presses and stamping machines which produce impact loads. Forge hammers are divided into two groups:drophammersfordiestampingandforgehammersproper. These mach inesconsist of falling ram, an anvil, and a frame. The speeds of operation usually range from 50 to 150 blows per minute. The dynamic loads attain a peak in a very short interval and then practically die out.



TableUnbalancedForcesandCouplesforDifferentCrankArrangement(Newcomb, 1 951)
Crack
Arrangement

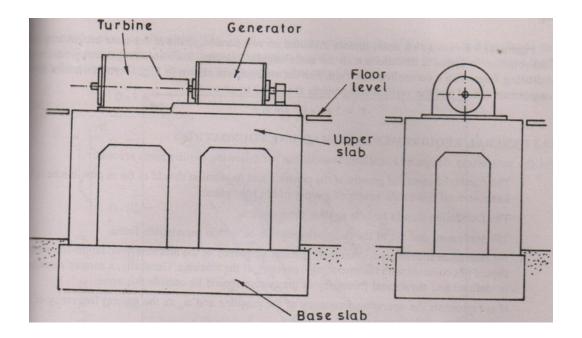
	Arrangement 				
		Forces		Couples	
	Fig.10.4	Primary	Secondary	Primary	Secondary
a.	Singlecrank	F'withoutcounterwts.	F"	0	0
		(0.5)F'with wts			
b.	Twocranks 1800		2F"	F'D without counter	0
	In-line	0	0	wts.	0
		0		(0.5)F'Dwithcounter	0
	cylinders			wts.	
	opposed			0	
	cylinders				
c.	-	1.41)F'withoutcounterwts	0	(1.41)F'Dwithoutcounterwt	F"D
				s.	
		(0.707)F'withcouter wts.		(0.707)F'Dwithcounter	
d.	Twocylinderon	F'withoutcounterw	1.41F"	wts.	0
	onecrank,	ts. 0 with counter			
	cylinder	wts.			
	at900				
e.	Twocylinderon	2F'withoutcounter	0	0	0
	one	wts. F' with			
		counter wts.			
	crank,				
	opposedcylinder s				
f.	Threecranksat	0	0	(3.46)F'Dwithoutcounterwt	(3.46)F"D
	1200			S.	
				(1.73)F'Dwithoutcounterwt	
g.	Four			S. 0	(4.0)F"D
		0	0	(1.41)F'Dwithoutcounterwts.	
	cylinders	0	0	(0.707)F'D with counter wts	
	cranks at				
	1800				

	crankat900				
h.	Sixcylinders	0	0	0	0

F'=primaryforce;F"=secondaryforces;D=cylinder-centre distance

Impactmachinesmayalsobemountedonblockfoundations, but their det ails would be quite different from these of reciprocating machines.

Rotary Machines:- These include high speed machines such as turbo generators, turbines and rotary compressors which operates at frequencies of the order of 3000rpm to 10000rpm. Associated with the semachinest here may be a considerable amoun to fauxiliary equipment such as condensers, coolers and pumps with connecting pipework and ducting. To accommodate these auxiliary equipments a common foundation arrangement is a two storey frame structure with the turbine located on the upper slab and the auxiliary equipment placed beneath, the upper slabbeing flush with the floor level of machine hall.



Rotatingmachineryisbalancedbeforeerection. However, inactual oper ationsome inbalance always exists. It means that the axis of rotation lies at certain eccentricity with respect to principal axis of inertia of the whole unit. Although the amount of eccentricity is smallinrotarymachinestheunbalanced which as ingle mass meisplaced on a rotating shaft at an eccentricity of rotating. The unbalanced forces produced by such a system in vertical and horizontal directions are given by

FV=meewsinwt

FH=meewcoswt

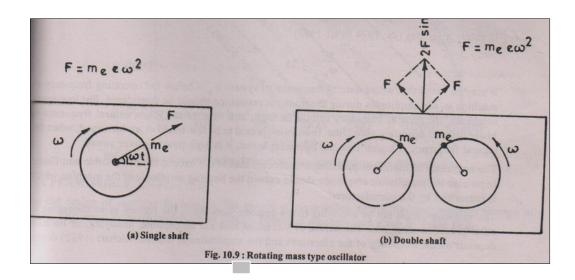


Figure. shows two equal masses mounted on two parallel shafts at the same eccentricity, the shaft rotating in opposite directions with the same angular velo city. Suchan arrangement produces an oscillating force with a controlled direction. For the arrangement shown in Fig. 10.9b, horizontal force components cancel and the vertical components are added to give

F=2mew2 sinwt

- 10.3 General Requirements of Machine Foundations:- For the satisfactorydesign of a machine foundation, the following requirements are met:
- Thecombinedcentreofgravityofthemachineandfoundationshouldasf aras possible be in the same vertical line as the centre of gravity of the base plane.
- 2. Thefoundationshouldbesafeagainst shearfailure.
- 3. Thesettlementandtiltofthefoundationshould be withinpermissible limits.
- 4. No resonance should occur; that is the natural frequency of the machine- foundation-soil system should not coincide with the the operating frequency of machine.Generally,azoneofresonanceisdefinedandthenaturalfreque ncyofthe system should lie outside this zone.

If w represents the operating frequency of the machine and wn as 178

the natural frequency of the system, then

a) Inreciprocatingmachines(IS:2974ptI-1982)

For important machines:
$$0.5 > \frac{w}{>2.0}$$

For ordinary machines: $0.6 = \frac{w}{>1.5}$

b) Inimpactmachines(IS:2974PtII-1980)

0.4>
$$\frac{}{}_{w_{n}}$$
 >1.5
c) (IS:2974PtIII-

$$0.8 > \frac{w}{wn} > 1.25$$

It may be noted that where frequency of system wn is below the operating frequency of machine w, the amplitudes during the transient resonance shouldbe considered. For low speed machines, the natural frequency should be high, and vice versa. When naturalfrequency islower than theoperating speed, thefoundation issaid tobelow tuned or under tuned, when the natural frequency is higher than the operating speed, it is high tuned or over tuned.

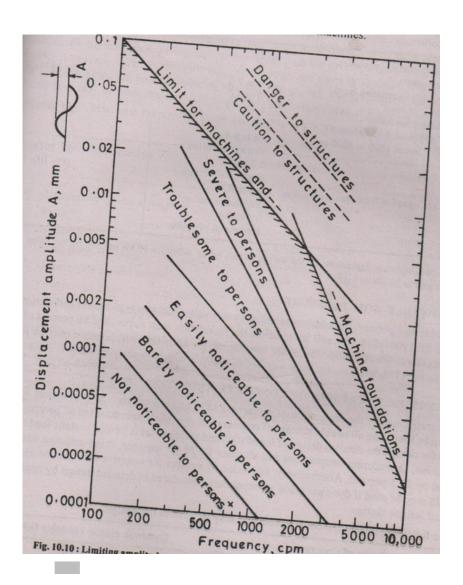
- 5. Theamplitudeofmotionatoperatingfrequencies should not exceed the permissible amplitude. In no case the permissible amplitude should exceed the limiting amplitude of the machine which is prescribed by the manufactured.
- The vibrations must not be annoying to the persons working in the 6.

 the factory or

damaging to other precision machines. The nature of vibrations that are perceptible,

annoyingorharmfuldependsonthefrequencyofthevibrationsandthea mplitudes of motion. Richart (1962) developed a plotfor vibrations that gives various limits

frequencyandamplitudefordifferentpurpose.Inthisfigure,theenvelop described by the shaded line indicates only a limit for safety and not a limit for satisfactory operation of machines.



PermissibleAmplitude:-

For the design of machine foundation, the values of permissible amplitudes suggested by Bureau of Indian Standards for the foundations of different types of machines are given in Table.

Table Value of permissible amplitude forfoundations of different machines:-

Sl. No.	Typeof machine	Permissbleamplitudemm	Reference
1.	Reciprocatingmachines	0.2	IS:2974(Pt-I)
2.	Hammer*		
	a)Forfoundationblock	1.0to2.0	IS:2974(Pt-II)
	b)Foranvil	1.0to3.0	
3.	Rotarymachines		
	a)Speed<1500rpm	0.2	IS:2974(Pt-IV)
	b)Speed1500to3000rpm	0.4to0.6	
		Verticalvibration	
		0.7to0.9	
		Horizontalvibration	
	c)Speed>300rpm	0.2to0.3	
		Verticalvibration	
		0.4to0.5	
		Horizontalvibration	

Permissble amplitude dependents of the weight of tup, lower value for 10kN tup and higher value for the tup weight equl to 30kN or higher.

AllowableSoilPressure:-

The allowable soil pressure should be evalutated by adequate subsoil exploration and testing inaccordancewith IS:1904-1978. The soilstressbelow the foundations hall not exceed 80 percent of the allowable soil pressure. When seismic forces are considered, the allowable soil pressure may be increased as specified in IS: 1893-1984. Permissible Stresses of Concrete and Steel:-

For the construction of the foundation of a machine M20 or M25 concrete in accordance with IS: 456-1978 shall be used. The allowable stresses of concrete and steel shall be reduced to 40 percent for concrete and 55% for steel, if the detailed design fo foundation and componets is limited to static load of foundation and machine. Considering tempreature and allother loading stogether, these assumed stresses may be expected to the construction of the foundation of a machine M20 or M25 concrete in accordance with IS: 456-1978 shall be used. The allowable stresses of concrete and steel shall be reduced to 40 percent for concrete and 55% for steel, if the detailed design for foundation and componets is limited to static load of foundation and machine. Considering

ceededby

33.5percent.Alternately,full value of stressesforconcreteand steelasspecifiedin IS:456
1978maybeusedifdynamic loadsareseparatelyconsideredindetaileddesignbyapplying suitable creep and fatigue factors.

Thefollowingdynamicmoduliofconcretemaybeusedinthe design:

Gradeofconcrete	Dynamicelasticmodulas (kN/m2)
M20	3.0×107
M25	3.4x107
M30	3.7x107

PermissibleStressesofTimber:-

Thetimberisgenerally used under the anvilof hammer foundation. Grade of timber is specified according to the size of defects like knots, checks etc. in the timber. Timber is thus classified into three grades select, Grade I and Grade II. The best quality timber having minimum or no defects at all is of the select grade. Grade I timbe is one having defects not larger than the specified ones. Grade II timber is poorer in quality than grade I. The permissble values of streees are given in Table for species of timber of grade I. In machine foundations timber of select grade is used. The permissble stresses of timber given in Table may be multified by 1.16 to get the permissble stresses of timber of select grade.

Table Minimum permissble stress limits (N/mm2) in three groups of structural timbers (For grade I Material)

Sl.	Strengthcharacter	Locationofuse	GroupA	GroupB	GroupC
No.				33.2.2.6.2	
i.	Bending andtension In	side(2)	18.0	12.0	8.5
ii.	alonggrain		1.05	0.64	0.49
iii	Shear(1)	Alllocations	11.7	7.8	4.9
iv.	Horizontal	Alllocations	4.0	2.5	1.1
V	Alonggrain	Inside(2)	12.6	9.8	5.6
	Compressionparallelt In	side(2)			
	o grain	Alllocationsand grade			
	Compression				
	perdendiculartograin				
	Modulasofelasticity (x				
	103N/mm2)				

- (i) Thevaluesofhorizontalsheartobeusedonlyforbeams.Inallothercas esshear along grain to be used.
- (ii) For working stresses for other locations of use, that is out side and wet, generally factors of 5/6 and 2/3 are applied.

The permissblebearing pressures on other elastic materials such as felt, cork and rubberaregenerallygiven by the manufactureres of these materials. No specific values are recommanded here since then vary in wide limits.

FOUNDATIONS OFROTARY MACHINES

General:-

The unprecedented burden cast by the importance to oil can be relived only by exploiting indigenous energy resources efficiently. Major power energy resource, in long term power plan, incoporate an optimal mix of thermal, hydel and nuclera generation. Power intensity is relatively high in our country due to various reasons including the substantial substitution among the forms of energy in the various important sectors along with the accelerated programme in rural electrification and assured

power supply for agriculturesectoretc. The aim of planning to generate power higher than the demand by at

least 10 percent, calls for a coordinated development of the power supply industry. As per the present ratio, the thermal sector caters 54 percent; hydro sector 43 percent and 3 percent catered by nuclear sector. The 15 year National Power Plan form 1980 onwards envisages the installation of additional generating capacity of almost 100,000 MW in the thermal, hydro and nuclear sectors taken together as against the existing generation capacity of 31,000MW. Large capacity thermal power station at coal pit heads called Super ThermalPowerstations(2000MWcapacityormore)because of their size and sop histicated technology, will account for a smuch as 50,000 MW to be commissioned during the enextfive year plan.

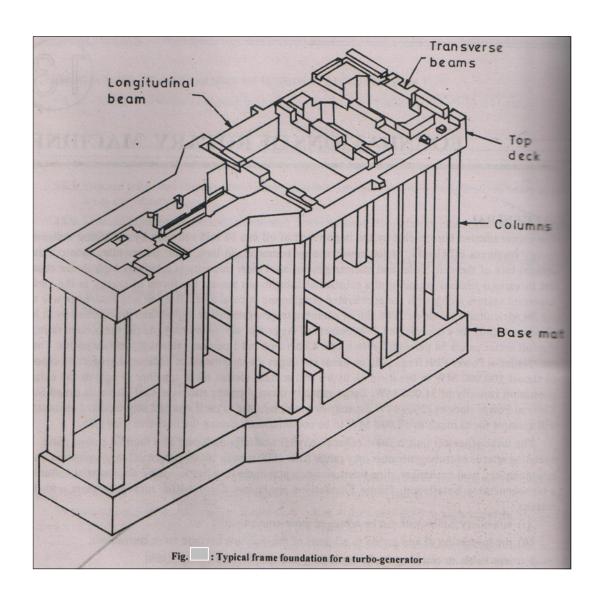
The turbogenerator unit is most expensive, vital and important part in a thermal power plant. The operating speeds of turbogenerators may range from 3000rpm to 10000rpm. Auxiliary equipments such as condenser, heat exchanger, pipelines , air vents and ducts for electric wiring are essential features of a turbogenerator installation. Frame foundations are commonly used for turbogenerators with four reason:

- a) auxiliaryequipmentcanbearrangedmoreconveniently,
- b) the inspection of and access to all parts of the machine become more convenient.
- c)less liabletocrackingduetosettlementandtemperaturechanges, and
- d) moreeconomicalduetothesavinginmaterialandfreedomtoaddmor e members to stiffen if needed.

The frame foundation is the assemblage of columns, longitudinal and transverse beam. The transverse beam smay be often eccentric with respect to the column centre lines and generally have varying cross-section due to several opening in the top deck and haunches at the junction with columns. The isometric view of a typical frame foundation is shown in Fig.

In a power-plant, the long term satisfactory performance of the turbogenerators is affected by their foundation, hence there is vital need to adequately design these foundations for all possible combinations of static and dynamic loads. Interaction with the mechanical engineer is also required for any adjustment in the layout of machinery and

auxiliaryfittings.



Specialconsiderations:-

Forbetterperformanceof aT.G.foundation, following points may be kept inview:

- i) The entire foundation should be separated from the main building in order to isolate the transfer of vibrations from the top deck of the foundation to the building floor of the machine room. A clear gap should be provided all round.
- ii) Other footing placed near to the machine foundation should be checked for non-uniform stresses imposed by adjacent footings. The pressure-bulbs under the adjacent footings should not interfere significantly with each other.
- iii) All the junctions of beams and columns of the foundation should be provided with adequate haunches in order to increase the general rigidly of the frame foundation.
- iv) The cross-sectional height of the cantilever elements at the embedment point should not be less than 60 to 75 percent of its span, being susceptible to excessive local vibrations.
- v) **\$he**uldhave transversebeams theiraxisverticalbelowthebearingtoavoid torsion. For the same reason the axes of columns and transverse beams should lie in the same vertical plane.
- vi) Theupperplatformshouldbeasrigidaspossibleinitsplane.
- vii) Permissible pressure on soil may be reduced by 20 percent to account for the vibration of the foundation slab. This slab has much smaller amplitudes of vibration than the upper platform.
- viii) The lower foundation slab should be sufficiently rigid to resist non-uniform settlement and heavy enough to lower the common centre of gravity of the machine and foundation. It is therefore made thicker than required by static computations. For 25MV machine its thickness is 2m and increase with the power of the machine to a maximum of 4m. Its weight should not be less than theweightofthemachineplustheweightof thefoundation excluding the base slab and condensers.
- ix) Specialreinforcementdetailingaslaiddownin the code IS-2974PtIIIshouldbe followed.

x) Special care in construction is called for to avoid cracking of concrete. The foundationslabshouldbecompletedinonecontinuouspouring.Inthi scasethe

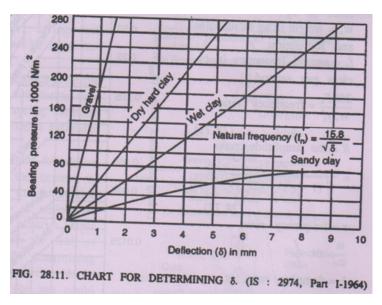
- joint between the two concretes, preferably at one-third column height, is specially treated to ensure 100 percent bond. Piles may be provided xi) to meet the bearing capacity requirement but then the consideration of effect subgrade is essential. Asfaraspossiblethefoundationshouldbedimensionedsuchthatthec entreof the gravity of the foundation with the machine should be in xii) vertical alignment with that of the base area in contact with the soil. Thegroundwatertableshouldbeaslowaspossibleanddeeperbyatleastone- fourth of xiii) the width of foundation below the base plane. This limits the vibrations propogation, ground-water being a good conductor to transmission. Soil-
- propogation, ground-water being a good conductor to wave transmission.

 Soilprofileandcharacteristicsofsoiluptoatleastthricethewidthofthetur bine foundation or till hard stratum is reached or uptopile depth, if piles are xiv) provided, should be investigated.

Design Criteria:-

ThedesignofaT.G.foundationisbasedonthefollowingdesign criteria:-

- i) From the point of view of vibration, the natural frequencies of foundation system should preferable be at a variance of at least 30 percent from the operating speed of the machine as well as critical speeds of the rotor. Thus resonanceisavoided.Anuncertaintyof10to20percentmaybeassum edinthe computed natural frequencies. However, it may not be necessary to avoid resonance in higher modes, if the resulting resonant amplitude is relatively insignificant.
 - Itispreferabletomaintainafrequencyseparationof50 percent.
- The amplitudes of vibration should be within permissible limits.Values of permissible amplitude are given in Table.



IndianStandardcodeofPracticeforDesignofFoundationsforReciprocating Type Machines:-

IScodeofpractice:(IS:2974,Part-I:1964)givesthefollowingcriteria:

- 1.The size of the foundationblock (in plan) should be larger than the bedplate of the machine with a minimum alround clearance of 15cm.
- 2.The width of the foundation should be at least equal to the distance of the centre of gravity of the crank shaft to the bottom of foundation in all vertical machines.
- 3. The depth of the foundation should be such as to rest the foundation on a good bearing strata and to ensure stability against rotation in a vertical plane.
- 4.The combined centre of gravity of machineand the foundation block shouldbe as much below the top of the foundation as possible.
- 5.Whenever possible, the operating frequency should be lower than thenaturalfrequencyofthefoundationsoilsystemandthefrequencyrati o should belessthan 0.5. Whentheoperating frequency ishigherthanthe naturalfrequencyofthefoundationsoilsystemof themachine,the

frequency ratios hould be more than 2 for important machines and more

than 1.5 for others.

Naturalfrequency:-Thenaturalfrequency(cyclespersecond)under the givenstressintensityisgiven by the following equation: $f_n = \frac{15.8}{\sqrt{\delta}}$

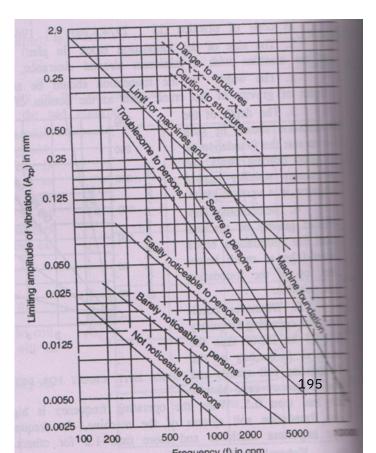
Where ð= elastic deflection of the foundation in millimeters, with respect to the entire area of foundation, to be determined from Fig.

The permissible bearing pressure, for use in Fig., under dynamic loads may be taken as $\frac{1}{5}$ of the permissible bearing pressure under static loads.

Amplitude of vibrations:- The permissible amplitude should not exceed the limiting amplitude for themachine prescribed by the manufacturers. Wheresuch data are not available, for relatively unimportant structures, the limiting amplitude should be determined from Fig.

The probable amplitude, in mm, of the machine at the operating frequency, is given by the following expression:

A=250F0
Where F0=dynamic force in kg Wv= weight in kg of machine and foundation
Fn= natural frequency in cycles per second
250F0
—=frequencyratio
wvfn²
R-theamplituderatio



$$= \sqrt{1 - r^{\frac{3}{2}} + (2r)^{2}}$$

r=frequencyratio

$$\frac{\omega}{\omega n}$$
 or $\frac{f}{fn}$ ξ =dam p ing ratio or dam p ing factor

The value of ξ shouldbedetermined from dynamic tests. When the value of ξ is not provided, it can be taken as 0.25.

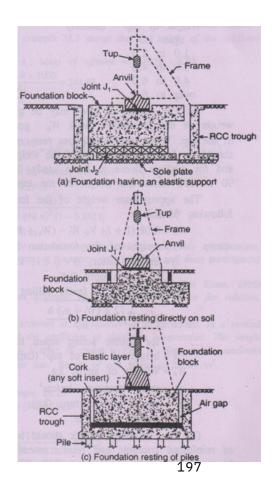
IndianStandardcodeofPracticeforDesignofFoundationsforImpact Type Machines:-

The design requirements of the impact types machines, such as dropandforgehammers, are design than those of the reciprocating type machines, discussed above. IS: 2974 (Part-II): 1966 covers the design requirements for the foundation of these machines.

Definitions:(i)Anvil:Anvilisabase-blockforahammeronwhichmaterial is forgedintotypeshapebyrepeatedstrikingofthetup.(ii)Tup:Tupisa weighted block which strikes the material being forged on the anvil.

- (iii)Foundation block: It is a mass of reinforced concrete on which the anvil rests.
- (iv)Protective cushing layer (joint J1):

 It is an elastic cushing of the suitalbe material and thickness provided between the anvil and the foundation block in order to prevent bouncing of anvil and creation of large impact stresses and consequent damages to the top



surface of the concrete in the

foundation block.

(v) Foundation support (Joint J2): It is a

supportforrestingthefoundation block. Theblockmayrestdirectlyon ground or on a resilient mounting such as timber sleepers, springs cork layer etc. The block may also be supported on pile foundations.

Design Criteria: (1)- The stresses produced at the time of impact in the foundationbase(soil,timber,sleeper,cork,springelementsorpiles)should be with in 0.8 times allowable static stresses. (2)The design of the entire

foundation system should be such that the

centresofgravityoftheanvil,andofthefoundationblock,aswellasthejoints at which the resultants of forces in the elestics joints J1 and J2 act, coincide

withthelineoffallofthehammertup. Whiledetermining the centre of gravity of the foundation blook, the weight of the frame of the tup could also be considered. (3) The maximum vertical vibrational amplitude of the

foundation

block should not be more than 1.2mm. In case of foundations on sand below the ground water, the permissble amplitude should not be more than 0.8mm.

(4) For the anvil, the permissble amplitude, which depends upon the weight of the tup should be taken from the following table:

Weight of tup	Maximum	permissble
amplitude Upto	1 t 1 mm	
2t	2mm	
Morethan 3t	3to4mm	

(5)The area of foundation block should be such that the safe loading intensityofsoilisneverexceededduringtheoperationofthehammer. The depth of the foundation block should be so designed that the block is safe both in punching shear and bending.

Weightoftup(tonnes)

Minimum depth of foundation blcok

Upto	1.0t	1.00m
	1.0to2.0	1.25m
	2.0to4.0	1.75m
	4.0to6.0	2.25m
	Overto6.0	2.50m

(6) The weight of an vilmay be generally kept at 25 times the weight of tup.

TheweightofthefoundationblcokWbgenerallyvariesfrom66to120times the weight of the tup. Where the foundations rest on stiff clays or compactsandydeposits,theweightshouldbefrom75to80timestheweight ofthe tup. For moderately firm to soft clays and for medium dense to loose sandy deposits, the weight of the block should be from 90 to 120 times the weight of the tup.

Theapproximateweightofthefoundationblcokmayalsobe determined from the folloiwng formula:

$$W = Q 8(1+1) V \oplus W - (W + W)_f$$

.....(28.73)

WhereWb=weightofthefoundationblock (kg)

If = impact factor, 0<If<1, and its average value for design purpose may be taken upto 0.6

√tb=√2ghforafreelyfallingtuptypehammer

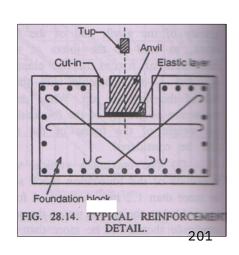
$$=0.65\sqrt{\frac{2g(\underline{W}t+\underline{)}Ps)h}{Wt}}$$

For double acting steam

hammers H= height of fall of

tup (cm)

Wa= weight of anvil, kg



Ps=steam pressure,

kg/cm2

Wt= weight of the tup,

(kg) Wf= weight of fram.

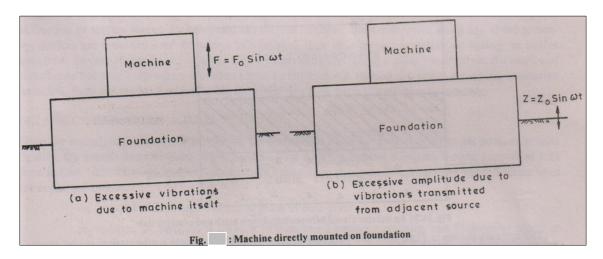
(7)The foundation block should be made of reinforced concrete and reinforcement should be arranged along the three axes and also diagonally to prevent shear, as shown in Fig. 28.14. More reinforcemnt should be provided at the top side of the foundaiton block than at the other side. Reinforcement at the top may be provided in the form of layers of grills made of 16mm diameter bars suitably spaced to allow easy pouring of concrete. The reinforcement provided should be at leat 25kg per m3 of concrete.

VIBRATIONISOLATIONANDSCREENING

General:-

Inmachinefoundations, following two types of the problems may arise:

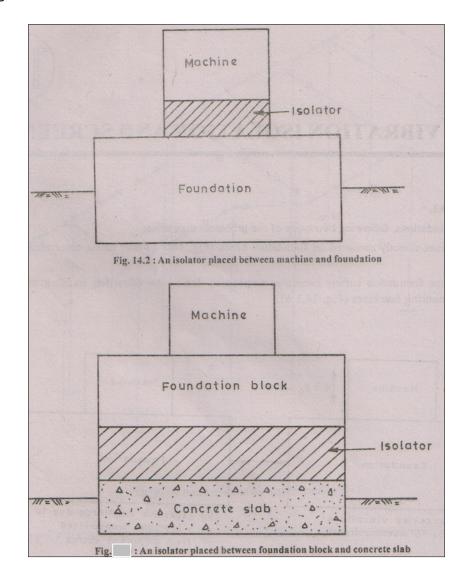
- Machinesdirectlymountedonfoundationblockmaycauseobjection able vibrations.
- ii) Machinefoundationsuffersexcessiveamplitudeduetothevibration s transmitted from the neighbouring machines.



Thefirstproblemmaybetackledbyisolatingthemachinesfromthefoundati
onthrough a suitably designed mounting system such that the
transmitted force is reduced which in turn will reduce the amplitude. This

type of isolationis termed as force isolation. This type of arrangement will pose is termed as motion isolation. For heavier machines, the isolating systemmaybeplacedbetweenthefoundationblockandconcreteslabasshown in Fig. Here

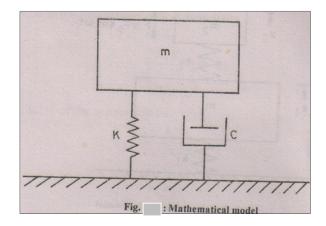
the machine are rigidly bolted to the foundation block which is isolated from the concrete slab throughthemountingsystem. The mounting system is an elastic layer which may be in the form of rubber pad, timber pad, cork pad or metal springs.



The systems shown in Fig. can be represented by a simple mathematical model shown in

Fig.Inthismrepresentsthemassofmachineormassofmachineplusfoundation block. The mounting system (i.e. the elastic layer) is characterised by a spring with a constant Kanddash potwith damping constant C. This mathematical representation involves one basic assumption that the underlying soil or rock posses infinite rigidity. This system is identical to the one shown in Fig. and the detailed analysis has already been presented considering both force 205

isolation and motion isolation separately.



A more realistic model will be that in which the soil or rock is considered as an elastic medium. This will make the system as a two-degree-freedom problem, the solutions of which are presented in the next section.

The second problem in which the vibration are transmitted from the

neighbouring machines can be solved by controlling the vibrating energy reaching the desired location. This is referred to as vibration screening. Effective screening of vibration may be achieved byproperinterception.Scattering,anddiffractionofsurfacewavesbyusingbarr trenches.sheetierssuchas pilewalls, and piles. If the screening devices are provided near the source of vibration, then it is termed as active screening or active isolation. In case screening devices are used by providing barriers at a point remote from the source of disturbance but near sitewherevibration has to be reduced, it is termed as passives creening or passiv eisolation. Both the methods of screening the vibrations have been discussed subsequently. ForceIsolation:- Since the underlying soil or rock supporting the foundation block (or base slab) does not possesinfinite rigidity, thefoundation soil should be represented by a springand not solely by a rigid support. Then the mathematical model becomes as shown in Fig. The various terms used are explained below:

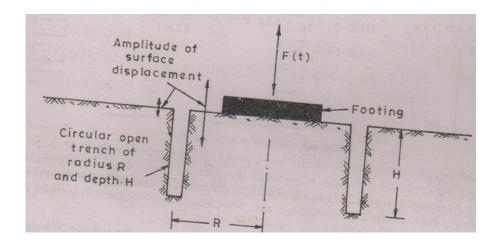
m2=Maissobátovaishiimetsobfducedbetweenmachineandfoundation block or mass of

machine plus mass of foundation block if isolator is placed between foundation block and mass slab. K1= Stiffnessofthesoil

K2= Stiffnessoftheisolator

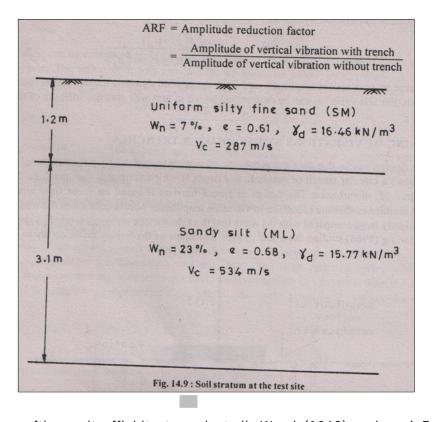
ScreeningofVibrationsbyuseofopen Trenches:- Active Screening: In this case the screening of vibrations is done near the source of vibration. Figure shows a circular trench of radius R and depth the which surrounds machinefoundationthatisthesourceofdisturbance. The design of trench barrie rsisbased on some field observations. Barkan (1962) mentioned that the vibration in

amplitudeoccursonlywhenthetrenchdimensionsaresufficientlylargecompar edwiththe wave length of the surface waves generated by the source of disturbance. Dolling (1966) studied the effect of size and shape of the trench on its ability to screen the vibrations.



The first comprehensive study of screening vibration by use of open trench was made by Woods and Richarts (1967) and Woods (1968). They conducted field tests by creating vertical vibrations with a small vibration resting on a small pad at a prepared site. The vibrator could create a maximum force of 80N. The soil conditions at the site were as shown in Fig. 14.9. The water table was below 14.3m depth. The depth H of trenches was varied from 150mm to 600mm, the radius R of annular trench varied from 150mm to 300mm, and the angular dimension 0 was varied from 900 to 3600 around the source of vibration. Frequencies of 200 to 350 Hz were used in the tests. Using velocity transducers,

pointsthroughoutthe test site before installation of the trench and after installation of the trench. Woods (1968) has introduced a term amplitude reduction factor which is defined as



SomeoftheresultsoffieldtestsconductedbyWoods(1968)areshowninF ig.inthe form of ARF contour diagrams. The dimensions of the trench are

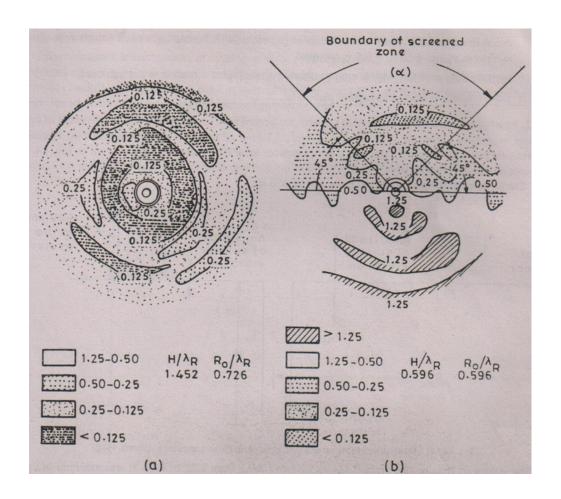
expressed in non-dimensional forms by dividing H and R by the wave λR of Rayleigh waves. λR is obtained by determining the number of

length

waves (n)_ occurring at distance x from the source (lengths λR for different frequencies are given in Table .

Table-Wavelengthandwavevelocityfor the Rayleighwave at the test site (Woods, 1968)

FrequencyHz	λR mm	VR m/x
200	687	137
250	513	128
300	421	126
350	336	117



Thefieldtests ofWoods(1968) thuscorrespondto

$$_{\lambda^R}^{\underline{\lambda}\underline{=}}$$
 0.222-0.910 and $_{\lambda^R}^{\underline{+}}$.222-1.82

For satisfactory screening of vibration, Woods (1968) recommended that the ARF should are the common of the comm

beless than or equal to 0.25. The conclusions made on the basis of this study to kee p ARF

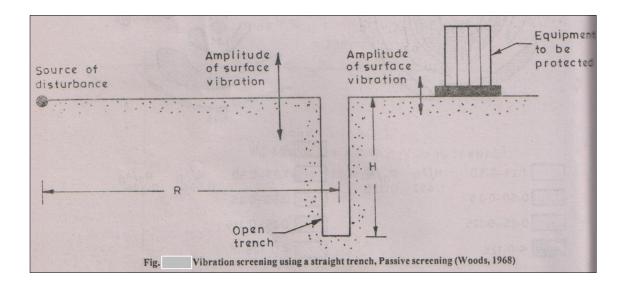
≤0.25are:

- i) For full circle trenches ($\vartheta=3600$), a minimum value of H/ λR =0.6 is required. The zone screened in this case extended to a distance of at least 10 wave lengths (10 λR) from the source of disturbance.
- ii) For partial circle trenches (900 < θ < 3600), the screened zone was defined as an area outside the trench extending to at least 10 wave lengths (10 λR) from the source and bounded on the sides by radial lines from the centre of source through points

450 from ends of trench. In this case also, a minimum value of $(H/\lambda R)=0.6$ is required.

- iii) Partial circle trenches with ϑ <900, effective screening of vibration is not achieved.
- iv) Trenchwidthisnotanimportantparameter.

Passive Screening:- Woods (1968) has also performed field tests to study the effectiveness of open tranches in passive screening. A typical layout ofthese test consisting of two vibration exciters (used one at a time for the tests),75t transducer location, and a trench is shown in Fig. The sizes of trenches ranged from 100mmx300mm mm deep to 2440 mmx3050mmx1220mmdeep. Frequencies of excitation varied form 200 to 350Hz.



 $\lambda R \sqrt{\hbar} \ln \frac{\partial}{\partial t} \log \Omega dt = 0.10$.

It was assumed in these tests that the zones screened by the trench would be symmetrical about the 00 line. Figure shows the ARF contour diagramforone of these tests.

Forsatisfactoryscreening, Woods (1968) recommended that the ARFshould beless than or equal to 0.25 in a semi-circular zone of radius (1/2) L behind the trench. The conclusions made on the basis of this field study to keep ARF \leq 0.25 are:

- i) $H\lambda R$ shouldbeatleast1.33
- ii) To maintain the same degree of screening, the least area of the trench in the vertical direction (i.e. LH-AT), should be as follows:

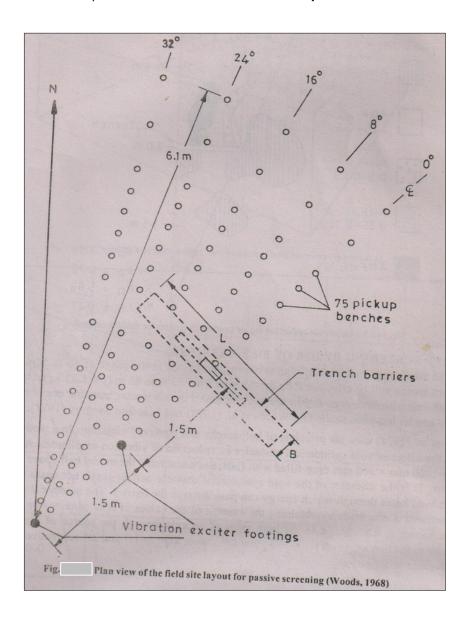
$$\frac{AT}{\lambda 2R} = 2.5at \frac{R}{\lambda_{R}} = 2.0$$

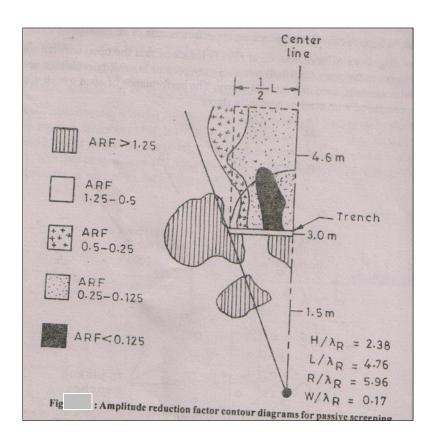
And

$$\frac{\Delta I}{\lambda 2R}$$
=6.0at $\frac{R}{\Delta}$ =7.0

iii) Trenchwidth hadpracticallynoinfluenceonthe effectivenessofscreening.

Experimental investigations of Sridharan et. al (1981) indicated that the open un filled trenches are the most effective. However, the open (unfilled) trenches may present instabilityproblemsnecessitatingtrenchesbackfilledwithsawdust,sandorbe ntoniteslurry. The performance of open trench with sawdust was found better as compared with sand or bentonite slurry.





PassiveScreeningbyuseofPileBarriers:-

There may be situations in which Rayleigh wavelengths may be in the range of 40 to 50m. For such a case, the open trench will be effective if λR). Open trenches (filled or its depth range from 53m the with such deep depths are not practical. For this pilesasanenergybarrierhasbeen

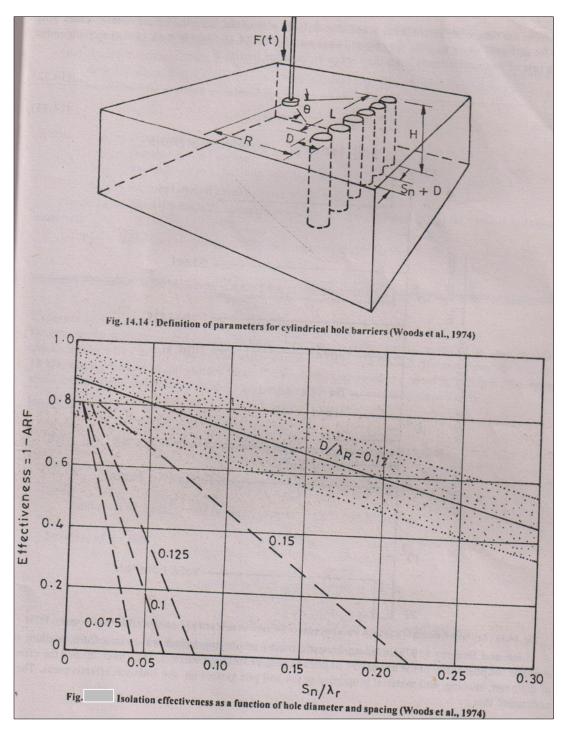
reason,possibleuseof rowsof studiedbyWoodset al. (1974) and Liao and Sangery (1978).

Woodset.al(1974)usedtheprincipleofholographyandobservedvibrationsi
namodel half-space to evaluate the effect of void cylindrical obstacles on
reduction of vibration amplitude. A box of size
1000mmx1000mmx300mm deep filled with fine sandconstituted
themodelhalf-

space.Inthisfigure,DisthediameterofthevoidcylindricalobstacleandSnis the net space between two consecutive void holes through which energy can pass through the barrier. The numerical evaluation of barrier effectiveness was made by obtaining the average of the values of ARF obtained on several lines beyond the barrier in a section ±150 of both

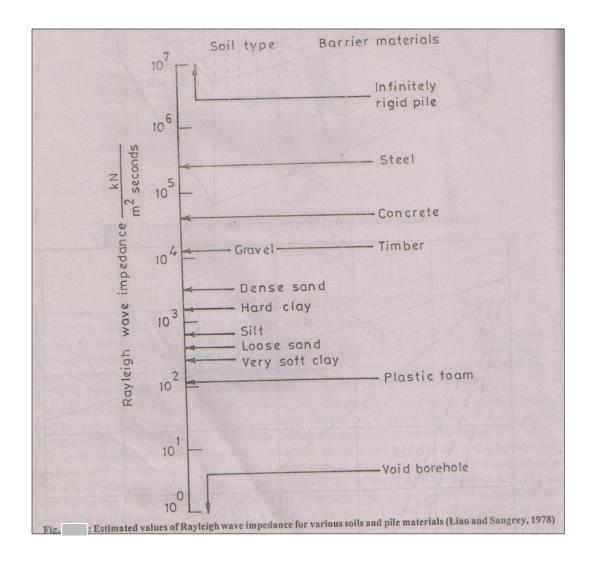
sidesof an axis through the source of disturbance and perpendicular to the barrier. In all tests, H/ $$\lambda R$$ and 2.5 respectively.

The isolation effectivenessis defined as



Using the data of different tests, a non-dimensional plot of the isolation effectiveness versus S/ λR ration for different values of D/ λR was plotted as shown in Fig. Woods et al. (1974) recommended thata row of void cylindricalholesmayactasan isolation barrierif

 $\sum_{\lambda \geq R6} 1 = \lambda$ And $\sum_{\lambda \leq R4} 1 = \lambda$



Liao and Sangrey (1978) used an acoustic model employing sound waves in a fluid medium to evaluate the possibility of the use of row of piles as passive isolation barriers. They have studied the effect of diameter, spacing and material properties of the soil pile system on the isolation effectiveness. They concluded that:

i) The Eqs. proposed by Woodsetal (1974) are generally valid.

- ii) $Sn=0.4\lambda R$ may be the upper limit for a barrier to have some effectiveness.
- iii) The effectiveness of the barrier is significantly affected by the material of the pile and void holes. Acoustically soft piles (IR<1) are more efficient than acoustically hard piles (IR>1). IR is impedance ratio which is defined as

Where, PP=Density of pilematerial

PS=Densityofsoilmedium

VRP=Rayleighwavevelocityinpilema

terial VRS=

Rayleighwavevelocityinsoilmedium

Figuregives ageneral range of the Ralyeighwave impendance (PVR) for various so ils and pile materials.

iv) Tworowsofbarriersaremoreeffective thansinglerowbarriers.